

Kind 2 User Documentation

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1 Kind 2

[Kind 2](#) is a multi-engine, parallel, SMT-based automatic model checker for safety properties of Lustre programs.

Kind 2 is a command-line tool. It takes as input a Lustre file annotated with properties to be proven invariant (see [Lustre Input](#)), and outputs which of the properties are true for all inputs, as well as an input sequence for those properties that are falsified. To ease processing by external tools, Kind 2 can output its results in JSON and XML formats (see [JSON / XML Output](#)).

By default Kind 2 runs a process for bounded model checking (BMC), two processes for k-induction (one for a fixed value of $k=2$, and other for increasing values of k), several processes for invariant generation, and a process for IC3 in parallel on all properties simultaneously. It incrementally outputs counterexamples to properties as well as properties proved invariant.

The following command-line options control its operation (run `kind2 --help` for a full list). See [Techniques](#) for configuration examples and more details on each technique.

`--enable {BMC|IND|IND2|IC3|INVGEN|INVGENOS|...}` Select model checking engines

By default, all four model checking engines are run in parallel. Give any combination of `--enable BMC`, `--enable IND`, `--enable IND2` and `--enable IC3` to select which engines to run. The option `--enable BMC` alone will not be able to prove properties valid, choosing `--enable IND` and `--enable IND2` only (or either of the two alone) will not produce any results. Any other combination is sound (properties claimed to be invariant are indeed invariant) and counterexample-complete (a counterexample will be produced for each property that is not invariant, given enough time and resources).

`--timeout <int>` (default 0 = none) – Run for the given number of seconds of wall clock time

`--smt_solver {Bitwuzla|cvc5|MathSAT|Yices|Yices2|Z3}` (default Z3) – Select SMT solver

`--bitwuzla_bin <file>` – Executable for Bitwuzla

`--cvc5_bin <file>` – Executable for cvc5

`--mathsat_bin <file>` – Executable for MathSAT 5

`--yices_bin <file>` – Executable for Yices 1 (native input)

`--yices2_bin <file>` – Executable for Yices 2 (SMT input)

`--z3_bin <file>` – Executable for Z3

`-v` Output informational messages

`-json` Output in JSON format

`-xml` Output in XML format

1.1 Try Kind 2 Online

Visit our [web interface](#) to try Kind 2 from your browser.

1.2 Download

If you use a Linux or a macOS computer, you can download an executable of the latest version of Kind 2 from [here](#). First make sure though that you have the required software described next.

1.3 Required Software

To run Kind 2 the following software must be installed on your computer:

- Linux or macOS, and
- a supported SMT solver
 - [Bitwuzla](#) (for inputs with only machine integers),
 - [cvc5](#),
 - [MathSAT 5](#),
 - [Yices 2](#),
 - [Yices 1](#), or
 - [Z3](#)

Z3 is the presently recommended SMT solver and the default option. For problems with only machine integers we recommend to use Bitwuzla in combination with Z3: select Bitwuzla as the main solver (`--smt_solver Bitwuzla`) but make sure the Z3 binary is also accessible to Kind 2.

1.4 VS Code Extension

You can also install our [extension](#) for Visual Studio Code which provides support for Kind 2. The extension contains Linux and macOS binaries for Kind 2 and Z3 ready to use. Windows is also supported through WSL2 (see [here](#) for more details).

1.5 Docker

Kind 2 is also available on [Docker Hub](#).

1.5.1 Retrieving / updating the image

Install [docker](#) and then run

```
docker pull kind2/kind2:dev
```

Docker will retrieve the layers corresponding to the latest version of the Kind 2 repository, develop version. If you are interested in the latest release, run

```
docker pull kind2/kind2
```

instead.

If you want to update your Kind 2 image to latest one, simply re-run the `docker pull` command.

1.5.2 Running Kind 2 through docker

To run Kind 2 on a file on your system, it is recommended to mount the folder in which this file is as a [volume](#). In practice, run

```
docker run -v <absolute_path_to_folder>:/lus kind2/kind2:dev <options> /lus/<your_
↪file>
```

where

- `<absolute_path_to_folder>` is the absolute path to the folder your file is in,
- `<your_file>` is the lustre file you want to run Kind 2 on, and
- `<options>` are some Kind 2 options of your choice.

N.B.

- the fact that the path to your folder must be absolute is [a docker constraint](#);
- mount point `/lus` is arbitrary and does not matter as long as it is consistent with the last argument `/lus/<your_file>`. To avoid name clashes with folders already present in the container however, it is recommended to use `/lus`;
- replace `kind2:dev` by `kind2` if you want to run the latest release of Kind2 instead of the develop version;
- `docker run` does **not** update your local Kind 2 image to the latest one: the appropriate `docker pull` command does.

1.5.3 Packaging your local version of Kind 2

In the `docker` directory at the top level of the Kind 2 repository, there is a `Dockerfile` you can use to build your own Kind 2 image. To do so, just run

```
docker build -t kind2-local -f ./docker/Dockerfile .
```

at the root of the repository. `kind2-local` is given here as an example, feel free to call it whatever you want.

Note that building your own local Kind 2 image **does require access to the Internet**. This is because of the packages the build process needs to retrieve, as well as for downloading the `z3` and `cvc5` solvers.

1.6 Building and installing

If you prefer, you can build Kind 2 directly from sources, either through the OPAM package manager (recommended) or directly using `dune`.

1.6.1 Using OPAM

Start by installing [OPAM 2.x](#) following the instructions on the website, and make sure OPAM has been initialized by running `opam init`. If you want to build the development version of Kind 2 that includes the most recent changes, as opposed to the latest release, then run

```
opam pin add -n kind2 https://github.com/kind2-mc/kind2.git
```

(You can always undo this change later using this command `opam unpin kind2`).

Otherwise, skip the step above and either run

```
opam install --update-invariant kind2
```

if you have OPAM 2.1 or later installed on your system, or run

```
opam depext kind2
opam install --unlock-base kind2
```

if you have an older version of OPAM (you can run `opam --version` to check the version).

This guides the installation of the ZeroMQ C library and any other required external dependencies using the default package manager for your OS (may ask `sudo` permission). It also builds and installs a compatible version of the OCaml compiler and libraries, and the `kind2` binary. Now you can start using `kind2`.

Other options using OPAM

By default, `kind2` will be installed into the `bin` directory of your current OPAM switch. Run

```
opam install kind2 --destdir=<DIR>
```

to install the Kind 2 binary into `<DIR>/bin`. This will also create directories `<DIR>/doc` and `<DIR>/lib`.

In alternative, you can clone <https://github.com/kind2-mc/kind2.git>, move to its top-level directory, and run

```
make install
```

to have OPAM install `kind2` and its dependencies.

Note that `z3` is available in OPAM so it is possible to install it too with OPAM by running:

```
opam install z3
```

Be aware, however, that this takes quite a bit of time (up to 25 minutes).

1.6.2 Direct Installation Using Dune

To build directly from sources you will also need the following software first:

- OCaml 4.09 or later,
- [Dune 2.7 or later](#),
- `dune-build-info`,
- [OCaml bindings for ZMQ](#),
- [Yojson](#),
- `num`,
- [Menhir](#) parser generator

First install this software on your system using your preferred method. Then clone the [Kind 2 git repository](#), move to the top-level directory of the repository, and run

```
dune build src @install
dune install --sections=bin --prefix <DIR>
```

to install the Kind 2 binary into `<DIR>/bin`.

You need a supported SMT solver in your `PATH` environment variable when running `kind2`.

1.7 Development

With OPAM 2.x you can create a local switch which will install all dependencies automatically.

```
opam switch create .  
make
```

Alternatively, you can install all dependencies in your current switch by running:

```
opam install . --deps-only  
make
```

For running the unit tests for front end, you can install ounit2 library using opam by running:

```
opam install ounit2
```

To run the ounit tests, you can use the following dune command:

```
dune test
```

1.8 Documentation

Documentation is available online in [HTML](#) or [PDF](#) forms.

In order to generate the documentation locally, you need:

- A GNU version of sed (gsed on OSX)
- [Python v3.5 or later](#)
- [Sphinx](#)

For HTML documentation, you additionally need:

- [sphinx-press-theme](#)

For PDF documentation, you additionally need:

- [latexmk](#)
- [XeTeX](#)
- [lmodern](#)

If you're on Debian/Ubuntu, assuming you have Python 3 installed, you can run the following:

```
sudo apt-get install python3-sphinx latexmk texlive-xetex lmodern  
pip3 install sphinx_press_theme
```

See `doc/usr/README.rst` for more information.

2 Techniques

This section presents the techniques available in Kind 2: how they work, and how they can be tweaked through various options:

- [k-Induction](#)
- [Invariant Generation](#)
- [IC3](#)

2.1 Compositional reasoning

When verifying a node n , compositional reasoning consists in abstracting the complexity of the subnodes of n by their contracts (see [Contract Semantics](#)). The idea is that the contract has typically a lot less state than the node it specifies, which in addition to its own state contains that of its subnodes recursively.

Compositional reasoning thus improves the scalability of Kind 2 by taking advantage of information provided by the user to abstract the complexity away. When in compositional mode (`--composition true`), Kind 2 will abstract all calls (to subnodes that have a contract with at least one guarantee or one mode) in the top node and verify the resulting, abstract system.

A successful compositional proof of a node does not guarantee the correctness of the concrete (unabstracted) node though, since the subnodes have not been verified. For this reason compositional reasoning is usually applied in conjunction with modular reasoning, discussed in the next section.

2.2 Modular reasoning

Modular reasoning is activated with the option `--modular true`. In this mode, Kind 2 will perform whatever type of analysis is specified by the other flags on **every node** of the hierarchy, bottom-up. The analysis is completed on every node even if some node is proved unsafe because of the falsification of one of its properties.

A timeout for each analysis can be specified using the `--timeout_analysis` flag. It can be used in conjunction with the global timeout given with the `--timeout` or `--timeout_wall` time.

Internally Kind 2 builds on previous analyses when starting a new one. For instance, by using the invariants previously discovered in subnodes of the node under analysis.

2.3 Refinement in compositional and modular analyses

An interesting configuration is

```
kind2 --modular true --compositional true ...
```

If `top` calls `sub` and we analyze `top`, it means we have previously analyzed `sub`. We are running in compositional mode so the call to `sub` is originally abstracted by its contract. Say the analysis fails with a counterexample. The counterexample might be spurious for the concrete version of `sub`: the failure would not happen if we used the concrete call to `sub` instead of the abstract one.

Say now that when we analyzed `sub`, we proved that it is correct. In this case Kind 2 will attempt to refine the call to `sub` in `top`. That is, undo the abstraction and use the implementation of `sub` in a new analysis.

Note that since `sub` is known to be correct, it is stronger than its contract. More precisely, it accepts fewer execution traces than its contract does. Hence anything proved with the abstraction of `sub` is still valid after refinement, and Kind 2 will use these results right away.

3 k-Induction

k-Induction is a well-known technique for the verification of transition systems. A k-induction engine is composed of two parts: base and step. Base performs bounded model checking on the properties, i.e. checks the **base case**. Step checks whether it is possible to reach a violation of one of the properties from a trace of states satisfying them: the **inductive step**.

In Kind 2 base and step run in parallel, and can be enabled separately. Running step alone with

```
kind2 --enable IND <file>
```

will not yield anything interesting, as step cannot falsify properties nor prove anything without base. To run the actual k-induction engine, you must enable base (BMC) and step (IND):

```
kind2 --enable BMC --enable IND <file>
```

3.1 Options

k-Induction can be tweaked with the following options.

`--bmc_max <int>` (default 0) – sets an upper bound on the number of unrolling base and step will perform. 0 is for unlimited.

`--ind_compress <bool>` (default false) – activates path compression in step, **i.e.** counterexamples with a loop will be dismissed. You can activate several path compression strategies:

- `--ind_compress_equal <bool>` (default true) – compresses states if they are equal modulo inputs
- `--ind_compress_same_succ <bool>` (default false) – compresses states if they have the same successors (experimental)
- `--ind_compress_same_pred <bool>` (default false) – compresses states if they have the same predecessors (experimental)

`--ind_lazy_invariants <bool>` (default false) – deactivates eager use of invariants in step. Instead, when a step counterexample is found each invariant is evaluated on the model until one blocks it. The invariant is then asserted to block the counterexample, and step starts a new check-sat.

4 Invariant Generation

The invariant generation technique currently implemented in Kind 2 is an improved version of [the one implemented in PKind](#). It works by instantiating templates on a set of terms provided by a syntactic analysis of the system.

The main improvement is that in Kind 2, invariant generation is modular. That is to say it can attempt to discover invariants for subnodes of the top node. The idea is that looking at small components and discovering invariants for them provides results faster than analyzing the system monolithically. To disable the modular behavior of invariant generation, use the option `--invgen_top_only true`.

There are two invariant generation techniques: one state (OS) and two state (TS). The former will only look for invariants between the state variables in the current state, while the latter tries to relate the current state with the previous state. The two are separated because as the system grows in size, two state invariant generation can become very expensive.

The one state and two state variants can be activated with `--enable INVGENOS` and `--enable INVGEN` respectively.

Note that, in theory, two state invariant generation is strictly more powerful than the one state version, albeit slower, since two state can also discover one state invariants. When both variants are running, Kind 2 optimizes two state invariant generation by forcing it to look only for two state invariants.

The bottom line is that running i) only two state invariant generation or ii) one state and two states will discover the same invariants. In the case of i) the same techniques seeks both one state and two state invariants at the same time, which is slower than ii) where one state and two state invariants are sought by different processes running in parallel.

4.1 Options

Invariant generation can be tweaked using the following options. Note that this will affect both the one state and two state process if both are running.

`--invgen_prune_trivial <bool>` (default `true`) – when invariants are discovered, do not communicate one-state invariants implied by previous one-state invariants, and two-state invariants implied by previous two-state invariants or the transition relation.

`--invgen_max_succ <int>` (default `1`) – the number of unrolling to perform on subsystems before moving on to the next one in the hierarchy.

`--invgen_lift_candidates <bool>` (default `false`) – if true, then candidate terms generated for subsystems will be lifted to their callers. **Warning** this might choke invariant generation with a huge number of candidates for large enough systems.

`--invgen_mine_trans <bool>` (default `false`) – if true, the transition relation will be mined for candidate terms. Can make the set of candidate terms untractable.

`--invgen_renice <int>` (only positive values) – the bigger the parameter, the lower the priority of invariant generation will be for the operating system.

4.2 Lock Step K-induction

Another improvement on the PKind invariant generation is the way the search for a k-induction proof of the candidate invariants is performed. In PKind, a bounded model checking engine is run up to a certain depth d and discovers falsifiable candidate invariants. The graph used to produce the potential invariants is refined based on this information. Once the bound on the depth is reached, an inductive step instance looks for actual invariants by unrolling up to d .

In Kind 2, base and step are performed in lock step. Once the candidate invariant graph has been updated by base for some depth, step runs at the same depth and broadcasts the invariants it discovers to the whole framework. It is thus possible to generate invariants earlier and thus speed up the whole analysis.

5 IC3

[IC3/PDR](#) is a recent technique by Aaron Bradley. IC3 alone can falsify and prove properties. To enable nothing but IC3, run

```
kind2 --enable IC3 <file>
```

The challenge when lifting IC3 to infinite state systems is the pre-image computation. If the input problem is in linear integer arithmetic, Kind 2 performs a fast approximate quantifier elimination. Otherwise, the quantifier elimination is delegated to an SMT solver, which is at this time only possible with Z3 or cvc5.

5.1 Options

`--qe_method {precise|impl|cooper}` (default `cooper`) – select the quantifier elimination strategy: `cooper` (default) for the built-in approximate method, `precise` or `impl` to delegate to the SMT solver. The `precise` strategy computes the exact pre-image, which is an expensive operation. The `impl` strategy under-approximates the result by computing a conjunctive implicant first. If the problem is not in linear integer arithmetic, `cooper` falls back to `impl`.

`--ic3_check_inductive <bool>` (default `true`) – Check if a blocking clause is inductive and communicate it as an invariant to concurrent verification engines.

`--ic3_block_in_future <bool>` (default `true`) – Block each clause not only in the frame it was discovered, but also in all higher frames.

`--ic3_fwd_prop_non_gen <bool>` (default `true`) – Attempt forward propagation of clauses before inductive generalization.

`--ic3_fwd_prop_ind_gen <bool>` (default `true`) – Inductively generalize clauses after forward propagation.

`--ic3_fwd_prop_subsume <bool>` (default `true`) – Check syntactic subsumption of forward propagated clauses

6 Lustre Input

Lustre is a functional, synchronous dataflow language. Kind 2 supports most of the Lustre V4 syntax and some elements of Lustre V6. See the file [examples/syntax-test.lus](#) for examples of all supported language constructs.

6.1 Properties and top-level node

To specify a property to verify in a Lustre node, add the following annotation in the body (i.e. between keywords `let` and `tel`) of the node:

```
--%PROPERTY ["<name>"] <bool_expr> ;
```

or, use a check statement:

```
check ["<name>"] <bool_expr> ;
```

where `<name>` is an identifier for the property and `<bool_expr>` is a Boolean Lustre expression.

Without modular reasoning active, Kind 2 only analyzes the properties of what it calls the top nodes. By default, any node that is not depended on by another node (i.e. called by that node) is a top node. Alternatively, nodes can be marked as main nodes by doing the following:

```
--%MAIN ;
```

to the body of that node.

You can also specify the main node in the command line arguments, with

```
kind2 --lustre_main <node_name> ...
```

Main nodes specified by the command line option override main nodes annotated in the source code. If any main nodes exist then only main nodes are analyzed (top nodes are not).

6.1.1 Example

The following example declares two nodes `greycounter` and `intcounter`, as well as an observer node `top` that calls these nodes and verifies that their outputs are the same. The node `top` is annotated with `--%MAIN ;` which makes it a main node. The line `--%PROPERTY OK;` means we want to verify that the Boolean stream `OK` is always true.

```
node greycounter (reset: bool) returns (out: bool);
var a, b: bool;
let
```

(continues on next page)

(continued from previous page)

```
a = false -> (not reset and not pre b);
b = false -> (not reset and pre a);
out = a and b;

tel

node intcounter (reset: bool; const max: int) returns (out: bool);
var t: int;
let
  t = 0 -> if reset or pre t = max then 0 else pre t + 1;
  out = t = 2;

tel

node top (reset: bool) returns (OK: bool);
var b, d: bool;
let
  b = greycounter(reset);
  d = intcounter(reset, 3);
  OK = b = d;

  --%MAIN ;

  --%PROPERTY OK;

tel
```

Kind 2 produces the following on standard output when run with the default options (kind2 <file_name.lus>):

```
kind2 v1.5.1

=====
Analyzing top
  with First top: 'top'
      subsystems
        | concrete: intcounter, greycounter

<Success> Property OK is valid by inductive step after 0.065s.

-----
Summary of properties:
-----
OK: valid (at 5)
=====
```

We can see here that the property OK has been proven valid for the system (by k-induction).

6.2 Contracts

A contract (A, G, M) for a node is a set of assumptions A , a set of guarantees G , and a set of modes M . The semantics of contracts is given in the [Contract Semantics](#) section, here we focus on the input format for contracts. Contracts are specified either locally, using the inline syntax, or externally in a contract node. Both the local and external syntax have a body composed of items, each of which define

- a ghost variable / constant,
- an assumption,
- a guarantee,
- a mode, or
- an import of a contract node.

They are presented in detail below, after the discussion on local and external syntaxes.

6.2.1 Inline syntax

A local contract is a special comment between the signature of the node

```
node <id> (...) returns (...);
```

and its body. That is, between the ; of the node signature and the let opening its body.

A local contract is a special block comment of the form

```
(*@contract  
  [item]+  
*)
```

or

```
/*@contract  
  [item]+  
*/
```

6.2.2 External syntax

A contract node is very similar to a traditional lustre node. The two differences are that

- it starts with `contract` instead of `node`, and
- its body can only mention contract items.

A contract node thus has form

```
contract <id> (<in_params>) returns (<out_params>) ;
let
  [item]+
tel
```

To use a contract node one needs to import it through an inline contract. See the next section for more details.

6.2.3 Contract items and restrictions

Ghost variables and constants

A ghost variable (constant) is a stream that is local to the contract. That is, it is not accessible from the body of the node specified. Ghost variables (constants) are defined with the `var` (`const`) keyword. Kind 2 performs type inference for constants so in most cases type annotations are not necessary.

The general syntax is

```
const <id> [: <type>] = <expr> ;
var <id> : <type> = <expr> ;
```

For instance:

```
const max = 42 ;
var ghost_stream: real = if input > max then max else input ;
```

Assumptions

An assumption over a node `n` is a constraint one must respect in order to use `n` legally. It cannot depend on outputs of `n` in the current state, but referring to outputs under a `pre` is fine.

The idea is that it does not make sense to ask the caller to respect some constraints over the outputs of `n`, as the caller has no control over them other than the inputs it feeds `n` with. The assumption may however depend on previous values of the outputs produced by `n`.

Assumptions are given with the `assume` keyword, followed by any legal Boolean expression:

```
assume <expr> ;
```

Guarantees

Unlike assumptions, guarantees do not have any restrictions on the streams they can depend on. They typically mention the outputs in the current state since they express the behavior of the node they specified under the assumptions of this node.

Guarantees are given with the `guarantee` keyword, followed by any legal Boolean expression:

```
guarantee <expr> ;
```

Modes

A mode (R,E) is a set of requires R and a set of ensures E. Modes are named to ease traceability and improve feedback. The general syntax is

```
mode <id> (  
  [require <expr> ;]*  
  [ensure <expr> ;]*  
) ;
```

For instance:

```
mode engaging (  
  require true -> not pre engage_input ;  
  require engage_input ;  
  -- No ensure, same as `ensure true ;`.  
) ;  
mode engaged (  
  require engage_input ;  
  require false -> pre engage_input ;  
  ensure output <= upper_bound ;  
  ensure lower_bound <= output ;  
) ;
```

Imports

A contract import merges the current contract with the one imported. That is, if the current contract is (A, G, M) and we import (A', G', M') , the resulting contract is $(A \cup A', G \cup G', M \cup M')$ where \cup is set union. However, each contract import introduces its own namespace to avoid name collisions.

When importing a contract, it is necessary to specify how the instantiation of the contract is performed. This defines a mapping from the input (output) formal parameters to the actual ones of the import.

When importing contract c in the contract of node n , the actual input parameters of the import of c cannot depend on outputs of n in the current state. The reason is that the distinction between inputs and outputs lets Kind 2 check that the assumptions requirements make sense, i.e. do not depend on outputs of n in the current state.

The general syntax is

```
import <id> ( <expr>,* <expr> ) returns ( <id>,* <id> ) ;
```

For instance:

```
contract spec (engage, disengage: bool) returns (engaged: bool) ;
let ... tel

node my_node (
  -- Flags are "signals" here, but `bool`s in the contract.
  engage, disengage: real
) returns (
  engaged: real
) ;
(*@contract
  var bool_eng: bool = engage <> 0.0 ;
  var bool_dis: bool = disengage <> 0.0 ;
  var bool_enged: bool = engaged <> 0.0 ;

  var never_triggered: bool = (
    not bool_eng -> not bool_eng and pre never_triggered
  ) ;

  assume not (bool_eng and bool_dis) ;
  guarantee true -> (
    (not engage and not pre bool_eng) => not engaged
  ) ;

  mode init (
    require never_triggered ;
```

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```
    ensure not bool_enged ;
  ) ;

  import spec (bool_eng, bool_dis) returns (bool_enged) ;
*)
let ... tel
```

Mode references

Once a mode has been defined it is possible to refer to it with

```
::<scope>::<mode_id>
```

where `<mode_id>` is the name of the mode, and `<scope>` is the path to the mode in terms of contract imports.

In the example from the previous section for instance, say contract `spec` has a mode `m`. The inline contract of `my_node` can refer to it by

```
::spec::m
```

To refer to the `init` mode:

```
::init
```

A mode reference is syntactic sugar for the `requires` of the mode in question. So if mode `m` is

```
mode m (
  require <r_1> ;
  require <r_2> ;
  ...
  require <r_n> ; -- Last require.
  ...
) ;
```

then `::<path>::m` is exactly the same as

```
(<r_1> and <r_1> and ... and <r_n>)
```

N.B.: a mode reference

- is a Lustre expression of type `bool` just like any other Boolean expression. It can appear under a `pre`, be used in a node call or a contract import, etc.
- is only legal **outside** the mode item itself. That is, no self-references are allowed. Forward references are allowed.

An interesting use-case for mode references is that of checking properties over the specification itself. One may want to do so to make sure the specification behaves as intended. For instance

```

mode m1 (...);
mode m2 (...);
mode m3 (...);

guarantee true -> ( -- `m3` cannot succeed to `m1`.
  (pre ::m1) => not ::m3
) ;
guarantee true -> ( -- `m1`, `m2` and `m3` are exclusive.
  not (::m1 and ::m2 and ::m3)
) ;

```

6.2.4 Merge, When, Activate and Restart

Note: the first few examples of this section illustrating (unsafe) uses of `when` and `activate` are **not legal** in Kind 2. They aim at introducing the semantics of lustre clocks. As discussed below, they are only legal when used inside a merge, hence making them safe clock-wise.

Also, `activate` and `restart` are actually not a legal Lustre v6 operator. They are however legal in Scade 6.

A merge is an operator combining several streams defined on **complementary** clocks. There is two ways to define a stream on a clock. First, by wrapping its definition inside a `when`.

```

node example (in: int) returns (out: int) ;
var in_pos: bool ; x: int ;
let
  ...
  in_pos = in >= 0 ;
  x = in when in_pos ;
  ...
tel

```

Here, `x` is only defined when `in_pos`, its clock, is true. That is, a trace of execution of `example` sliced to `x` could be

step	in	in_pos	x
0	3	true	3
1	-2	false	//
2	-1	false	//
3	7	true	7
4	-42	true	//

where // indicates that x undefined.

The second way to define a stream on a clock is to wrap a node call with the activate keyword. The syntax for this is

```
(activate <node_name> every <clock>)(<input_1>, <input_2>, ...)
```

For example, consider the following node:

```
node sum_ge_10 (in: int) returns (out: bool) ;
var sum: int ;
let
  sum = in + (0 -> pre sum) ;
  out = sum >= 10 ;
tel
```

Say now we call this node as follows:

```
node example (in: int) returns (...) ;
var tmp, in_pos: bool ;
let
  ...
  in_pos = in >= 0 ;
  tmp = (activate sum_ge_10 every in_pos)(in) ;
  ...
tel
```

That is, we want sum_ge_10(in) to tick iff in is positive. Here is an example trace of example sliced to tmp; notice how the internal state of sub (i.e. pre sub.sum) is maintained so that it does refer to the value of sub.sum at the last clock tick of the “activate”:

step	in	in_pos	tmp	sub.in	pre sub.sum	sub.sum
0	3	true	false	3	nil	3
1	2	true	false	2	3	5
2	-1	false	nil	nil	5	nil
3	2	true	false	2	5	7
4	-7	false	nil	nil	7	nil
5	35	true	true	35	7	42
6	-2	false	nil	nil	42	nil

Now, as mentioned above the merge operator combines two streams defined on **complimentary** clocks. The syntax of merge is:

```
merge( <clock> ; <e_1> ; <e_2> )
```

where e_1 and e_2 are streams defined on <clock> and not <clock> respectively, or on not

<clock> and <clock> respectively.

Building on the previous example, say add two new streams `pre_tmp` and `safe_tmp`:

```
node example (in: int) returns (...);
var tmp, in_pos, pre_tmp, safe_tmp: bool;
let
  ...
  in_pos = in >= 0;
  tmp = (activate sum_ge_10 every in_pos)(in);
  pre_tmp = false -> pre safe_tmp;
  safe_tmp = merge( in_pos; tmp; pre_tmp when not in_pos );
  ...
tel
```

That is, `safe_tmp` is the value of `tmp` whenever it is defined, otherwise it is the previous value of `safe_tmp` if any, and `false` otherwise. The execution trace given above becomes

step	in	in_pos	tmp	pre_tmp	safe_tmp
0	3	true	false	false	false
1	2	true	false	false	false
2	-1	false	nil	false	false
3	2	true	false	false	false
4	-7	false	nil	false	false
5	35	true	true	false	true
6	-2	false	nil	true	true

Just like with uninitialized pres, if not careful one can easily end up manipulating undefined streams. Kind 2 forces good practice by allowing `when` and `activate ... every` expressions only inside a `merge`. All the examples of this section above this point are thus invalid from Kind 2's point of view.

Rewriting them as valid Kind 2 input is not difficult however. Here is a legal version of the last example:

```
node example (in: int) returns (...);
var in_pos, pre_tmp, safe_tmp: bool;
let
  ...
  in_pos = in >= 0;
  pre_tmp = false -> pre safe_tmp;
  safe_tmp = merge(
    in_pos;
    (activate sum_ge_10 every in_pos)(in);
    pre_tmp when not in_pos
  );
tel
```

(continues on next page)

```
...
tel
```

Kind 2 supports resetting the internal state of a node to its initial state by using the construct `restart/every`. Writing

```
(restart n every c)(x1, ..., xn)
```

makes a call to the node `n` with arguments `x1, ..., xn` and every time the Boolean stream `c` is true, the internal state of the node is reset to its initial value.

In the example below, the node `top` makes a call to `counter` (which is an integer counter modulo a constant `max`) which is reset every time the input stream `reset` is true.

```
node counter (const max: int) returns (t: int);
let
  t = 0 -> if pre t = max then 0 else pre t + 1;
tel

node top (reset: bool) returns (c: int);
let
  c = (restart counter every reset)(3);
tel
```

A trace of execution for the node `top` could be:

step	reset	c
0	false	0
1	false	1
2	false	2
3	false	3
4	true	0
5	false	1
6	false	2
7	true	0
8	true	0
9	false	1

Note: This construction can be encoded in traditional Lustre by having a Boolean input for the reset stream for each node. However providing a built-in way to do it facilitates the modeling of complex control systems.

Restart and activate can also be combined in the following way:

```
(activate (restart n every r) every c)(a1, ..., an)
(activate n every c restart every r)(a1, ..., an)
```

These two calls are the same (the second one is just syntactic sugar). The (instance of the) node `n` is restarted whenever `r` is true and the resulting call is activated when the clock `c` is true. Notice that the restart clock `r` is also sampled by `c` in this call.

6.2.5 Enumerated data types in Lustre

```
type my_enum = enum { A, B, C };
node n (x : my_enum, ...) ...
```

Enumerated datatypes are encoded as subranges so that solvers handle arithmetic constraints only. This also allows to use the already present quantifier instantiation techniques in Kind 2.

6.2.6 N-way merge

As in Lustre V6, merges can also be performed on a clock of a user defined enumerated datatype.

```
merge c
  (A -> x when A(c))
  (B -> w + 1 when B(c));
```

Arguments of merge have to be sampled with the correct clock. Clock expressions for merge can be just a clock identifier or its negation or `A(c)` which is a stream that is true whenever `c = A`.

Merging on a Boolean clock can be done with two equivalent syntaxes:

```
merge(c; a when c; b when not c);

merge c
  (true -> a when c)
  (false -> b when not c);
```

6.3 Partially defined nodes

Kind 2 allows nodes to define their outputs only partially. For instance, the node

```
node count (trigger: bool) returns (count: int ; error: bool) ;
(*@contract
  var once: bool = trigger or (false -> pre once) ;
  guarantee count >= 0 ;
  mode still_zero (
```

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```
    require not once ;
    ensure count = 0 ;
  ) ;
mode gt (
  require not ::still_zero ;
  ensure count > 0 ;
) ;
*)
let
  count = (if trigger then 1 else 0) + (0 -> pre count) ;
tel
```

can be analyzed: first for mode exhaustiveness, and the body is checked against its contract, although it is only partially defined. Here, both will succeed.

6.4 The imported keyword

Nodes (and functions, see below) can be declared `imported`. This means that the node does not have a body (`let ... tel`). In a Lustre compiler, this is usually used to encode a C function or more generally a call to an external library.

```
node imported no_body (inputs: ...) returns (outputs: ...) ;
```

In Kind 2, this means that the node is always abstract in the contract sense. It can never be refined, and is always abstracted by its contract. If none is given, then the implicit (rather weak) contract

```
(*@contract
  assume true ;
  guarantee true ;
*)
```

is used.

In a modular analysis, `imported` nodes will not be analyzed, although if their contract has modes they will be checked for exhaustiveness, consistently with the usual Kind 2 contract workflow.

6.4.1 Partially defined nodes VS imported

Kind 2 allows partially defined nodes, that is nodes in which some streams do not have a definition. At first glance, it might seem like a node with no definitions at all (with an empty body) is the same as an `imported` node.

It is not the case. A partially defined node still has a (potentially empty) body which can be analyzed. The fact that it is not completely defined does not change this fact. If a partially defined node is at the top level, or is in the cone of influence of the top node in a modular analysis, then its body **will** be analyzed.

An `imported` node on the other hand explicitly does not have a body. Its non-existent body will thus never be analyzed.

6.5 Functions

Kind 2 supports the `function` keyword which is used just like the `node` one but has slightly different semantics. Like the name suggests, the output(s) of a `function` should be a non-temporal combination of its inputs. That is, a function cannot depend on the `->`, `pre`, `merge`, `when`, `conduct`, or `activate` operators. A function is also not allowed to call a node, only other functions. In Lustre terms, functions are stateless.

In Kind 2, these restrictions extend to the contract attached to the function, if any. Note that besides the ones mentioned above, no additional restrictions are enforced on functions compared to nodes. In particular, functional congruence is not enforced on partially defined functions, imported functions, and functions abstracted by their contracts. That is, Kind 2 might return a counterexample where two calls to an abstract function with the same input values provide different output values. To prevent this kind of counterexamples from happening, Kind 2 offers an option called `--enforce_func_congruence` which enforces abstract functions to behave as mathematical functions. The downside of using this option is that the IC3 engine is forced to shut down because its current implementation cannot reason about the resulting system.

6.5.1 Benefits

Functions are interesting in the model-checking context of Kind 2 mainly as a mean to make an abstraction more precise. A realistic use-case is when one wants to abstract non-linear expressions. While the simple expression $x*y$ seems harmless, at SMT-level it means bringing in the theory of non-linear arithmetic.

Non-linear arithmetic has a huge impact not only on the performances of the underlying SMT solvers, but also on the SMT-level features Kind 2 can use (not to mention undecidability). Typically, non-lineary arithmetic tends to prevent Kind 2 from performing satisfiability checks with assumptions, a feature it heavily relies on.

The bottom line is that as soon as some non-linear expression appear, Kind 2 will most likely fail to analyze most non-trivial systems because the underlying solver will simply give up.

Hence, it is usually **extremely rewarding** to abstract non-linear expressions away in a separate function equipped with a contract. The contract would be a linear abstraction of the non-linear expression that is precise enough to prove the system using correct. That way, a compositional analysis would i) verify the abstraction is correct and ii) analyze the rest of the system using this abstraction, thus making the analysis a linear one.

Using a function instead of a node simply results in a better abstraction. Kind 2 will encode, at SMT-level, that the outputs of this component depend on the current version of its inputs only, not on its previous values.

6.6 If statements and frame conditions

Within node definitions, Kind 2 has support for two features that allow the programmer to use a more imperative style– (1) if statements and (2) frame conditions.

6.6.1 If statements

Kind 2 has always supported conditional expressions of the form `x = if condition then expr1 else expr2`, where the if/then/else expression either evaluates to `expression1` or `expression2`, depending on the value of `condition`. However, in some circumstances, it may be more natural to use if statements that serve as control flow (rather than evaluate to a value). For example, Kind 2 now supports statements of the form:

```
if condition
then
  y1 = expr1;
  y2 = expr2;
else
  y1 = expr3;
  y2 = expr4;
fi
```

In the above block, if `condition` is true, then `y1` and `y2` will be set to `expr1` and `expr2`, respectively. Otherwise, `y1` and `y2` will be set to `expr3` and `expr4`. The if statement is closed with the `fi` token. As with other mainstream programming languages, Kind 2 allows for arbitrary nesting of if statements, as well as writing if statements that do not have an else block.

Note: If statements are syntactic sugar for conditional expressions. The if statement above is equivalent to:

```
y1 = if condition then expr1 else expr3;
y2 = if condition then expr2 else expr4;
```

6.6.2 Frame conditions

Kind 2 also has support for code blocks with frame conditions. At the beginning of the block (denoted by the `frame` keyword), the user specifies a list of variables that they wish to define within the frame block. All variables defined within the frame block must be present in this list. Then, initial values are optionally specified for these variables. Variables are defined within the frame block body (denoted by the `let` and `tel` keywords). It is possible to leave variables (partially or fully) undefined: On the first timestep, each variable is set equal to its initialization value, if one exists. On other timesteps, each undefined variable stutters (it is set equal to its value on the previous timestep).

The following example involves three variables `y1`, `y2`, and `y3`. Since `y1` is left undefined within the frame block body, it will always be equal to 0 (its initialization value). `y2` will have value 100, 0, 1, 2, 3, ... because it is set equal to its initialization value (100) on the first timestep, but on other timesteps it is set equal to `counter()`. Even though `y3` is fully defined within the frame block (with no unguarded pre expressions), its initialization value is still used, so it is equal to 5, 1, 2, 3,

```
node example() returns (y1, y2, y3: int);
let
  frame ( y1, y2, y3 )
    (* Initializations *)
    y1 = 0; y2 = 100; y3 = 5;

    (* Body *)
    let
      y2 = pre counter();
      y3 = counter();
    tel
  tel

node counter() returns (y: int);
let
  y = 0 -> pre y + 1;
tel
```

Frame conditions are especially useful when combined with the `if` statements described in the previous subsection, as variables can be left undefined in some branches of the `if` statement.

```
node example() returns (y1, y2: int);
let
  frame ( y1, y2 )
    (* Initializations *)
    y1 = 0;
    y2 = 100;
```

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```

(* Body *)
let
  if (counter() < 10)
  then
    y1 = counter();
  else
    y2 = counter() * 2;
  fi
tel
tel

node counter() returns (y: int);
let
  y = 0 -> pre y + 1;
tel

```

In the above example, y_1 is left undefined in the `else` branch of the `if` statement, and y_2 is left undefined in the `then` branch. y_1 is initialized on the first timestep, set to be equal to `counter()` on the second through tenth timesteps, and then stutters (staying at 9) for the remaining timesteps. On the other hand, y_2 starts at its initialization value (100) and stutters there for the first 10 timesteps, and then is set to `counter() * 2` for the remaining timesteps.

Note that variables do not have to have initializations. When no initialization is given, a variable's initial value is equal to the initial value of the expression defined in the frame block body. If the corresponding expression is undefined in the first timestep, then the variable is also undefined in the first timestep. For example, the following code is supported because even though y_1 and y_2 do not have an initializations, they are present in the list of variables `frame (y1, y2)`. The initial value of y_1 is 0 (the initial value assigned by `counter()`), and the initial value of y_2 is undefined (due to the unguarded `pre`).

```

frame ( y1, y2 )
let
  y1 = counter();
  y2 = pre counter();
tel

node counter() returns (y: int);
let
  y = 0 -> pre y + 1;
tel

```

Also, it is still possible to assign to multiple variables at once (equations of the form $y_1, y_2 = (\text{expr1}, \text{expr2});$) in either the initializations or the frame block body.

The frame block semantics may introduce unguarded pre expressions. For example, the definition of `y` in the following code block is equivalent to `y = pre y`. So, Kind 2 will produce two warning messages. The first will state that `y` is uninitialized in the frame block, and the second will state that there is an unguarded pre (due to this lack of initialization).

```
frame ( y )
let
tel
```

Similarly, in the following code block, the definitions of `y1` and `y2` are equivalent to `y1 = if cond then 0 else pre y1` and `y2 = if cond then pre y2 else 1`, respectively. This situation (and any other situation where the frame block semantics result in the generation of an unguarded pre) will also generate the two warnings as discussed in the previous paragraph.

```
frame (y1, y2)
if cond
then
  y1 = 0;
else
  y2 = 1;
```

6.6.3 Restrictions

A frame block cannot be nested within an if statement or another frame block, as demonstrated in the following examples:

```
if condition
then
  frame ( y1, y2 )
  y1 = init1; y2 = init2;
  let
    y1 = 10;
  tel
fi
```

```
frame ( y1, y2 )
y1 = init1; y2 = init2;
let
  y1 = expr1;
  frame ( y2 )
  y2 = init3;
  let
    y2 = expr2;
  tel
tel
```

Assertions, MAIN annotations, and PROPERTY annotations also cannot be placed within if statements or frame blocks.

Since an initialization only defines a variable at the first timestep, it need not be stateful. Therefore, a frame block initialization cannot contain any pre or \rightarrow operators. This restriction also ensures that initializations are never undefined.

7 Machine Integers

Kind2 supports both signed and unsigned versions of C-style machine integers of width 8, 16, 32, and 64.

7.1 Declarations

Machine integer variables can be declared as global, local, or as input/output of nodes. Signed machine integers are declared as type `intN` and unsigned machine integers are declared as type `uintN` where `N` is the width (8, 16, 32, or 64).

The following

```
x : uint8;  
y : int16;
```

declares a variable `x` of type unsigned machine integer of width 8, and variable `y` of type signed machine integer of width 16.

7.2 Values

Machine integers values can be constructed using implicit conversion functions applied to integer literals. The implicit conversion functions are of the form `uintN` for unsigned machine integers and `intN` for signed machine integers.

The following

```
x = uint8 27;  
y = int16 -5012;
```

defines `x` to have value 27, and `y` to have value -5012, given that `x` is a variable of type `uint8` and `y` is a variable of type `int16`.

7.3 Semantics

Machine integers of width `x` represent binary numbers of size `x`. Signed machine integers are represented using 2's complement.

The bounds of machine integers are specified here for convenience:

```
uint8 : 0 to 255  
uint16 : 0 to 65535
```

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```
uint32 : 0 to 4294967295
uint64 : 0 to 18446744073709551615
int8    : -128 to 127
int16   : -32768 to 32767
int32   : -2147483648 to 2147483647
int64   : -9223372036854775808 to 9223372036854775807
```

When the conversion functions are used for literals that are out of this range, they are converted to a machine integer that is in range using the modulo operation, as in C. For instance, in the following

```
x = uint8 256;
y = int16 32768;
```

x evaluates to 0 and y to -3268, given that x is a variable of type `uint8` and y is a variable of type `int16`.

Conversions are allowed between machine integers of different widths, as long as both types are either signed or unsigned. Values remain unchanged when converted from a smaller to a larger width; values are adjusted modulo the range of the destination type when converted from larger to smaller width. The following code illustrates this.

```
a : int8;
b : int16;
c : uint16;
d : uint8;
a = int8 120;
b = int16 a; -- b == int16 120
c = uint16 300;
d = uint8 c; -- c == uint8 44
```

7.4 Operations

Kind2 allows the following operations over the machine integer types.

7.4.1 Arithmetic Operations

Addition (+), subtraction (-), multiplication (*), division (`div`), modulo (`mod`), and unary negation (-) are allowed on either signed or unsigned machine integers, and return a machine integer with the same sign and same width as the input(s).

```
a, a1, a2 : uint8;
b : uint16;
c : uint32;
```

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```

d : uint64;
e, f : int8;
a1 = (uint8 5);
a2 = (uint8 22);
a = a1 + a2;
b = (uint16 20) * (uint16 200);
c = (uint32 500) div (uint32 5);
d = (uint64 25) mod (uint64 10);
e = (int8 -5) + (- (int8 10));
f = (int8 10) - (int8 -5);

```

7.4.2 Logical Operations

Conjunction (`&&`), disjunction (`||`), and negation (`!`) are performed in a bitwise fashion over the binary equivalent of their machine integer inputs. Conjunction and disjunction are binary, while negation is unary. All 3 operations return a machine integer that has the same sign and same width as its input(s).

```

a, b, b1, b2, c : uint8;
a = (uint8 0) && (uint8 45); --a = (uint8 0)
b1 = (uint8 255);
b2 = (uint8 45);
b = b1 && b2; --b = (uint8 45)
c = !(uint8 0); --c = (uint8 255)

```

7.4.3 Shift Operations

Left shift (`lsh`) and right shift (`rsh`) operations are binary operations: the first input is either signed or unsigned, the second input is unsigned, and the sign of the output matches that of the first input; both inputs and the output have the same width.

Right shifting when the first operand is signed, results in an arithmetic right shift, where the bit shifted in matches the sign bit.

A left shift is equivalent to multiplication by 2, and a right shift is equivalent to division by 2, as long as the result can fit into the machine integer of the same width. In other words, the left shift operator shifts towards the most-significant bit and the right shift operator shifts towards the least-significant bit.

```

a, b, c : bool;
a = (uint8 0) lsh (uint8 10) = (uint8 0); --true
b = (uint8 255) rsh (uint8 12) = (uint8 255); --true
c = (int8 -1) lsh (uint8 1) = (int8 -2); --true

```

7.4.4 Comparison Operations

The following comparison operations are all binary: $>$, $<$, $>=$, $<=$, $=$. They input machine integers of the same size and sign, and output a boolean value.

```
a : bool;  
a = (int8 -12) < (int8 12); --true
```

7.5 Limitations

Currently, only SMT solvers `cvc5` and `Z3` support logics that allows the usage of integers and machine integers together. To use any of the other supported SMT solvers, the Lustre input must contain only machine integers.

Moreover, `IC3` requires either `cvc5` or `Z3` to run on models with machine integers. If none of them is available, Kind 2 runs with the `IC3` model checking engine disabled.

8 Arrays

Experimental feature

8.1 Lustre arrays

Kind 2 supports the traditional Lustre V5 syntax for arrays.

8.1.1 Declarations

Array variables can be declared as global, local or as input/output of nodes. Arrays in Lustre are always indexed by integers (type `int` in Lustre), and the type of an array variable is written with the syntax `t ^ <size>` where `t` is a Lustre type and `<size>` is an integer literal or a constant symbol.

The following

```
A : int ^ 3;
```

declares an array variable `A` of type array of size 3 whose elements are integers. The size of the array can also be given by a defined constant.

```
const n = 3;
...
A : int ^ n;
```

This declaration is equivalent to the previous one for `A`.

An interesting feature of these arrays is the possibility for users to write generic nodes and functions that are parametric in the size of the array. For instance one can write the following node returns the last element of an array.

```
node last (const n: int; A: int ^ n) returns (x: int);
let
  x = A[n-1];
tel
```

It takes as input the size of the array and the array itself. Note that the type of the input `A` depends on the value of the first constant input `n`. In Lustre, calls to such nodes should of course end up by having concrete values for `n`, this is however not the case in Kind 2 (see [Extension to unbounded arrays](#)).

Arrays can be multidimensional, so a user can declare e.g. matrices with the following

```
const n = 4;
const m = 5;
...
M1 : bool ^ n ^ m;
M2 : int ^ 3 ^ 3;
```

Here M1 is a matrix of size 4x5 whose elements are Boolean, and M2 is a square matrix of size 3x3 whose elements are integers.

Remark

M1 can also be viewed as an array of arrays of Booleans.

Kind 2 also allows one to nest datatypes, so it is possible to write arrays of records, records of arrays, arrays of tuples, and so on.

```
type rational = { n: int; d: int };
rats: rational^array_size;
mm: [int, bool]^array_size;
```

In this example, `rats` is declared as an array of record elements and `mm` is an array of pairs.

8.1.2 Definitions

In the body of nodes or at the top-level, arrays can be defined with literals of the form

```
A = [2, 5, 7];
```

This defines an array `A` of size 3 whose elements are 2, 5 and 7. Another way to construct Lustre arrays is to have each elements be the same value. This can be done with expressions of the form `<value> ^ <size>`. For example the two following definitions are equivalent.

```
A = 2 ^ 3;
A = [2, 2, 2];
```

Arrays are indexed starting at 0 and the elements can be accessed using the selection operator `[]`. For instance the result of the evaluation of the expression `A[0]` for the previously defined array `A` is 2.

The selection operators can also be applied to multidimensional arrays. Given a matrix `M` defined by

```
M = [[1, 2, 3],
      [4, 5, 6],
      [7, 8, 9]];
```


then the expression $M[1][2]$ is valid and evaluates to 6. The result of a single selection on an n -dimensional array is an $(n-1)$ -dimensional array. The result of $M[2]$ is the array $[7, 8, 9]$.

8.1.3 Unsupported features of Lustre V5

Kind 2 currently **does not support** the following features of [Lustre V5](#):

- Array concatenation like $[0, 1] \mid [2, 3, 4]$
- Array slices like $A[0..3]$, $A[0..3 \text{ step } 2]$, $M[0..1][1..2]$ or $M[0..1, 1..2]$
- The operators are not homomorphically extended. For instance `or` has type `bool -> bool -> bool`, given two arrays of Booleans A and B , the expression $A \text{ or } B$ will be rejected at typing by Kind 2
- Node calls don't have an homomorphic extension either

8.2 Extension to unbounded arrays

Kind 2 provides an extension of Lustre to express equational constraints between unbounded arrays. This syntax extension allows users to inductively define arrays, give whole array definitions and allows to encode most of the other unsupported array features. This extension was originally suggested by [Esterel](#).

Remark

Here, by unbounded we mean whose size is an unbounded constant.

In addition, we also enriched the specification language of Kind 2 to support (universal and existential) quantifiers, allowing one to effectively model parameterized system.

8.2.1 Whole array definitions

Equations in the body of nodes can now take the following forms

- $A = \langle \text{term} \rangle$; This equation defines the values of the array A to be the same as the values of the array expression $\langle \text{term} \rangle$.
- $A[i] = \langle \text{term}(i) \rangle$; This equation defines the values of all elements in the array A . The index i has to be a symbol, it is bound locally to the equation and shadows all other mentions of i . Index variables that appear on the left hand side of equations are **implicitly universally quantified**. The right hand side of the equation, $\langle \text{term}(i) \rangle$ can depend on this index. The meaning of the equation is that, for any integer i between 0 and the size of A , the value at position i is defined as the term $\langle \text{term}(i) \rangle$.

Semantically, a whole array equation is equivalent to a quantified equation. Let A be an array of size an integer constant n , then following equation is legal.

```
A[i] = if i = 0 then 2 else B[i - 1] ;
```

It is equivalent to the formula $i \in [0; n]. (i = 0 \rightarrow A[i] = 2) \wedge (i > 0 \rightarrow A[i] = B[i-1])$.

Multidimensional arrays can also be redefined the same way. For instance the equation

```
M[i][j] = if i = j then 1 else 0 ;
```

defines M as the identity matrix

```
[ [ 1 , 0 , 0 , ..., 0 ],  
  [ 0 , 1 , 0 , ..., 0 ],  
  [ 0 , 0 , 1 , ..., 0 ],  
  ..... ,  
  [ 1 , 0 , 0 , ..., 1 ] ]
```

It is possible to write an equation of the form

```
M[i][i] = i;
```

but in this case the second index *i* shadows the first one, hence the definition is equivalent to the following one where the indexes have been renamed.

```
M[j][i] = i;
```

8.2.2 Inductive definitions

One interesting feature of these equations is that we allow definitions of arrays inductively. For instance it is possible to write an equation

```
A[i] = if i = 0 then 0 else A[i-1] ;
```

This is however not very exciting because this is the same as saying that A will contain only zeros, but notice we allow the use of A in the right hand side.

Dependency analysis

Inductive definitions are allowed under the restriction that they should be well founded. For instance, the equation

```
A[i] = A[i];
```

is not and will be rejected by Kind 2 the same way the equation $x = x$; is rejected. Of course this restriction does not apply for array variables under a pre, so the equation $A[i] = \text{pre } A[i]$; is allowed.

In practice, Kind 2 will try to prove statically that the definitions are well-founded to ensure the absence of dependency cycles. We only attempt to prove that definitions for an array A at a given index i depends on values of A at indexes strictly smaller than i.

For instance the following set of definitions is rejected because e.g. $A[k]$ depends on $A[k]$.

```
A[k] = B[k+1] + y;  
B[k] = C[k-1] - 2;  
C[k] = A[k] + k;
```

On the other hand this one will be accepted.

```
A[k] = B[k+1] + y;  
B[k] = C[k-1] - 2;  
C[k] = ( A[k-1] + B[k] ) * k ;
```

Because the order is fixed and that the checks are simple, it is possible that Kind 2 rejects programs that are well defined (with respect to our semantic for whole array updates). It will not, however, accept programs that are ill-defined.

For instance each of the following equations will be rejected.

```
A[i] = if i = 0 then 0 else if i = 1 then A[0] else A[i-1];
```

```
A[i] = if i = n then 0 else A[i+1];
```

```
A[i] = if i = 0 then 0 else A[0];
```

Examples

This section gives some examples of usage for inductive definitions and whole array updates as a way to encode unsupported features and as way to encode complicated functions succinctly.

Sum of the elements in an array

The following node returns the sum of all elements in an array.

```
node sum (const n: int; A: int ^ n) returns (s: int);  
var cumul: int ^ n;  
let  
  cumul[i] = if i = 0 then A[0] else A[i] + cumul[i-1];  
  s = cumul[n-1];  
tel
```

We declare a local array `cumul` to store the cumulative sum (i.e. `cumul[i]` contains the sum of elements in `A` up to index `i`) and the returned value of the node is the element stored in the last position of `cumul`.

Note that this node is parametric in the size of the array.

Array slices

Array slices can be trivially implemented with the features presented above.

```
node slice (const n: int; A: int ^ n; const low: int; const up: int)
returns (B : int ^ (up-low));
let
  B[i] = A[low + i];
tel
```

Homomorphic extensions

Encoding an homomorphic or on Boolean arrays is even simpler.

```
node or_array (const n: int; A, B : bool^n) returns (C: bool^n);
let
  C[i] = A[i] or B[i];
tel
```

Defining a generic homomorphic extension of node calls is not possible because nodes are not first order objects in Lustre.

Parameterized systems

It is possible to describe and check properties of parameterized systems. Contrary to the Lustre compilers, Kind 2 does not require the constants used as array sizes to be instantiated with actual values. In this case the properties are checked for any array sizes.

```
node slide (const n:int; s: int) returns(A: int^n);
let
  A[i] = if i = 0 then s else (-1 -> pre A[i-1]);

  --%PROPERTY n > 1 => (true -> A[1] = pre s);
tel
```

This node stores in an array `A` a sliding window over an integer stream `s`. It saves the values taken by `s` up to `n` steps in the past, where `n` is the size of the array.

Here the property says, that if the array A has at least two cells then its second value is the previous value of s.

8.2.3 Quantifiers in specifications

To better support parameterized systems or systems with large arrays, we expose quantifiers for use in the language of the specifications. Quantifiers can thus appear in **properties**, **contracts** and **assertions**.

Universal quantification is written with:

```
forall ( <x : type>;+ ) P(<x>+)
```

where x are the quantified variables and type is their type. P is a formula or a predicate in which the variable x can appear.

For example, the following

```
forall (i, j: int) 0 <= i and i < n and 0 <= j and j < n => M[i][j] = M[j][i]
```

is a formula that specifies that the matrix M is symmetric.

Remark

Existential quantification takes the same form except we use `exists` instead of `forall`.

Quantifiers can be arbitrarily nested and alternated at the propositional level.

Example

The same parameterized system of a sliding window, slightly modified to express the property that A contains in each of its cells, an uninitialized value (i.e. value -1), or one of the previous values of the stream s.

```
node slide (const n:int; s: int) returns(ok: bool^n);
var A: int^n;
let
  A[i] = if i = 0 then s else (-1 -> pre A[i-1]);
  ok[i] = A[i] = -1 or A[i] = s or (false -> pre ok[i]);

  --%PROPERTY forall (i: int) 0 <= i and i < n => ok[i];
tel
```

8.2.4 Limitations

One major limitation that is present in the arrays of Kind 2 is that one cannot have node calls in inductive array definitions whose parameters contain unbounded array indices.

For instance, it is currently not possible to write the following in Kind 2 where A and B are arrays, n is a symbolic constant, and some_node takes values as inputs.

```
node some_node (x: int) returns (y: int);
...

A, B: int^n;
...

A[i] = some_node(B[i]);
```

Another limitation is that quantified variables cannot appear in the parameters of a node call. These limitation exists only for technical implementation reasons.

8.2.5 Command line options

We provide different encodings of inductive array definitions in our internal representation of the transition system. The command line interface exposes different options to control which encoding is used. This is particularly relevant for SMT solvers that have built-in features, whether it is support for the theory of arrays, or special options or annotations for quantifier instantiation.

These options are summed up in the following table and described in more detail in the rest of this section.

Option	Description
-smt_arrays	Use the builtin theory of arrays in solvers
-inline_arrays	Instantiate quantifiers over array bounds in case they are statically known
-arrays_rec	Define recursive functions for arrays (for cvc5)

The default encoding will use quantified formulas for inductive definitions and whole array updates.

For example if we have

```
A : int^6;
...
A[k] = x;
```

we will generate internally the constraint

$$k: \text{int. } 0 \leq k < 6 \Rightarrow (\text{select } A \text{ } k) = x$$

These form of constraint are handled in an efficient way by cvc5 (thanks to finite model finding).

`--smt_arrays`

By default arrays are converted using ah-hoc selection functions to avoid stressing the theory of arrays in the SMT solvers. This option tells Kind 2 to use the builtin theory of arrays of the solvers instead. If you want to try it, it's probably a good idea to use it in combination of `--smtlogic detect` for better performances.

`--inline_arrays`

By default, Kind 2 will generate problems with quantifiers for arrays which should be useful for problems with large arrays. This option tells Kind 2 to instantiate these quantifiers when it can reasonably do so. Only cvc5 has a good support for this kind of quantification so you may want to use this option with the other solvers.

The previous example

```
A : int^6;  
...  
A[k] = x;
```

will now be encoded by the constraint

$$\begin{aligned} &(\text{select } A \ 0) = x \quad (\text{select } A \ 1) = x \quad (\text{select } A \ 2) = x \quad (\text{select } A \ 3) = x \quad (\text{select } A \ 4) \\ &= x \quad (\text{select } A \ 5) = x \end{aligned}$$

`--arrays_rec`

This uses a special kind of encoding to tell cvc5 to treat quantified definitions of some uninterpreted functions as recursive definitions.

9 JSON / XML Output

Kind 2 can output its results in two structured formats: [JSON](#) and [XML](#). They facilitate the processing of Kind 2's results by external tools. The next sections describe each of these output formats in detail.

9.1 JSON format

The JSON output is activated by running Kind 2 with the `-json` option. Its syntax is fully specified by the JSON schema available in the [schemas/kind2-output.json](#) file.

The root element of a JSON output document is either a [Log Object](#) if Kind 2 terminates early with an error, or an array of [Results Objects](#) if Kind 2 succeeds generating some result. Every [Results Object](#) (including [Log Object](#)) is identified and distinguished from other [Results](#) objects by a property of type string called `objectType`.

In a successful execution, a [Kind2 Options Object](#) specifies the options used by the tool, and any [Log](#) message is added to the array as it is written. When Kind 2 is run as an [interpreter](#), the array includes one [Execution Object](#) that contains a description of the computed values for the output and state variables. Otherwise, Kind 2 works as a model checker and performs a series of analyses. The beginning of a main analysis is indicated by an [AnalysisStart Object](#), and its end by an [AnalysisStop Object](#). Within these delimiters, a [Property Object](#) describes the result for a particular property of the input model under the parameters of the analysis. When the verbose mode is enabled, statistics and progress info of the analysis is also recorded along through [Stat](#) and [Progress](#) objects.

Similarly to main analyses, when a post-analysis is enabled, the beginning of the post-analysis is indicated by an [PostAnalysisStart Object](#), and its end by an [PostAnalysisEnd Object](#).

9.1.1 Log Object

A Log object records an informative message from the tool. The value of its `objectType` property is `log`. The list of properties of a Log object are:

Key	Type	Description
<code>level</code>	<code>string</code>	A level that gives a rough guide of the importance of the message. Can be fatal, error, warn, note, info, debug, or trace.
<code>source</code>	<code>string</code>	The name of the Kind 2 module which wrote the log.
<code>file</code>	<code>string</code>	Associated input file, if any.
<code>line</code>	<code>integer</code>	Associated line in the input file, if any.
<code>column</code>	<code>integer</code>	Associated column in the input file, if any.
<code>value</code>	<code>string</code>	The log message.

9.1.2 Results Objects

A `Result` object can be one of the following objects: a [Log Object](#), a [Kind2 Options Object](#), an [AnalysisStart Object](#), an [AnalysisStop Object](#), a [Property Object](#), a [Stat Object](#), a [Progress Object](#), a [PostAnalysisStart Object](#), or a [PostAnalysisEnd Object](#).

9.1.3 Kind2 Options Object

A `Kind2 options` object describes the options used by the tool in the current execution. The value of its `objectType` property is `kind2Options`. The list of properties of a `Kind2 options` object are:

Key	Type	Description
<code>enabled</code>	<code>array</code>	List of Kind 2 module names that are enabled.
<code>timeout</code>	<code>number</code>	The wallclock timeout used for all the analyses.
<code>bmcMax</code>	<code>integer</code>	Maximal number of iterations for BMC and K-induction.
<code>compositional</code>	<code>boolean</code>	Whether compositional analysis is enabled or not.
<code>modular</code>	<code>boolean</code>	Whether modular analysis is enabled or not.

9.1.4 AnalysisStart Object

An `AnalysisStart` object indicates the beginning of a main analysis. The value of its `objectType` property is `analysisStart`. The list of properties of an `AnalysisStart` object are:

Key	Type	Description
<code>top</code>	<code>string</code>	Name of the current top-level component.
<code>concrete</code>	<code>array</code>	Names of the subcomponents whose implementation is used in the analysis.
<code>abstract</code>	<code>array</code>	Names of the subcomponents whose contract is used in the analysis.
<code>assumptions</code>	<code>array</code>	Array of pairs (name of subcomponent, number of considered invariants).

9.1.5 AnalysisStop Object

An `AnalysisStop` object indicates the end of a main analysis. The value of its `objectType` property is `analysisStop`. No properties are associated.

9.1.6 Property Object

A Property object describes the result for a particular property of the input model. The result should be considered in the context of the analysis in which the property object is contained. The value of its objectType property is property. The list of properties of an AnalysisStart object are:

Key	Type	Description
name	string	Property identifier or description.
scope	string	Name of the component where the property was analyzed.
line	integer	Associated line in the input file, if any.
column	integer	Associated column in the input file, if any.
source	string	Origin of the property. Can be Assumption if it comes from an assumption check, Guarantee if it comes from the check of a guarantee, Ensure if it comes from a check of a require-ensure clause in a contract mode, OneModeActive if it comes from an exhaustiveness check of the state space covered by the modes of a contract, and PropAnnot if it comes from the check of a property annotation.
runtime	object	The runtime of the analysis (in seconds), and whether the time-out expired
k	integer	The value of k in a k-inductive proof, if any.
trueFor	integer	The largest value of k for which the property was proved to be true, if any.
answer	object	The source of the answer, and the result value of the check. The result can be valid, falsifiable, or unknown.
counterExample	object	Counterexample to the property satisfaction (only available when answer is falsifiable). It describes a sequence of values for each stream that leads the system to the violation of the property. It also gives the list of contract modes that are active at each step, if any.

9.1.7 Stat Object

An Stat object provides statistics info about the current analysis. The value of its objectType property is stat. The list of properties of a Stat object are:

Key	Type	Description
source	string	Name of the Kind 2 module which reported the info.
sections	array	List of statSection objects, each of them with a section name and a list of statItem objects. Each statItem has a name, a type, and a value. See schemas/kind2-output.json for further details.

9.1.8 Progress Object

An Progress object reports the current value of k for k-inductive-based analyses. The value of its objectType property is progress. The list of properties of a Progress object are:

Key	Type	Description
source	string	Name of the k-inductive-based analysis.
k	integer	Value for k.

9.1.9 PostAnalysisStart Object

An PostAnalysisStart object indicates the beginning of a post-analysis. The value of its objectType property is postAnalysisStart. The list of properties of an PostAnalysisStart object are:

Key	Type	Description
name	string	Name of the post-analysis

The post-analyses currently available are [Test Generation](#) (testgen), [Proof Certificates](#) (certification), [Contract Generation](#) (contractgen), [Compilation to Rust](#) (rustgen), [Invariant Printing](#) (invprint), and [Inductive Validity Core](#) (ivc).

9.1.10 PostAnalysisEnd Object

An `PostAnalysisEnd` object indicates the end of a post-analysis. The value of its `objectType` property is `postAnalysisEnd`. No properties are associated.

9.1.11 Execution Object

An `Execution` object describes the sequences of values for the output and state variables of an input model computed from its simulation (see the [interpreter](#) mode). The value of its `objectType` property is `execution`. It only has one object property called `trace` which follows the same format than property `counterExample` in [Property Object](#).

9.1.12 ModelElementSet Object

A `ModelElementSet` object describes a set of model elements (a model element can be an equation, a node call, an assumption, a guarantee, etc). It is used to describe a core that we can get from an [Inductive Validity Core](#) (`ivc`) or [Minimal Cut Set](#) (`mcs`) analysis. The result should be considered in the context of the analysis or post-analysis in which the `ModelElementSet` object is contained. The value of its `objectType` property is `modelElementSet`.

Key	Type	Description
<code>class</code>	<code>string</code>	Class of the core. Can be <code>must</code> , <code>must complement</code> , <code>ivc</code> , <code>ivc complement</code> , <code>mcs</code> or <code>mcs complement</code> .
<code>size</code>	<code>integer</code>	Number of model elements in the core.
<code>property</code>	<code>string</code>	The property associated with the core. If all properties are considered, this field is missing.
<code>runtime</code>	<code>object</code>	The runtime for computing the core (in seconds).
<code>nodes</code>	<code>array</code>	For each node, contains an object that enumerates the model elements of the node that are part of the core.
<code>counterExample</code>	<code>object</code>	Counterexample to the property satisfaction (only when relevant, that is, when class is <code>mcs</code> or <code>mcs complement</code>). See the property object for more info.

9.2 XML format

The XML output is activated by running Kind 2 with the `-xml` option. Its syntax is fully specified by the XML schema available in the [schemas/kind2-output.xsd](#) file.

The root element of a XML output document is either a [Log Element](#) if Kind 2 terminates early with an error, or a [Results Element](#) if Kind 2 succeeds generating some result.

9.2.1 Log Element

A Log element is a simple element that records an informative message from the tool. The list of attributes of a Log element are:

Attribute	Base Type	Description
class	xs:string	A level that gives a rough guide of the importance of the message. Can be fatal, error, warn, note, info, debug, or trace.
source	xs:string	The name of the Kind 2 module which wrote the log.
line	xs:integer	Associated line in the input file, if any.
column	xs:integer	Associated column in the input file, if any.

9.2.2 Results Element

A Results element is a sequence of zero or more of the following elements: a [Log Element](#), an [AnalysisStart Element](#), an [AnalysisStop Element](#), a [Property Element](#), a [Stat Element](#), a [Progress Element](#), a [PostAnalysisStart Element](#), a [PostAnalysisEnd Element](#), or an [Execution Element](#).

The list of attributes of a Results element are:

Attribute	Base Type	Description
enabled	xs:string	List of comma-separated Kind 2 enabled module names.
timeout	xs:decimal	The wallclock timeout used for all the analyses.
bmc_max	xs:integer	Maximal number of iterations for BMC and K-induction.
compositional	xs:boolean	Whether compositional analysis is enabled or not.
modular	xs:boolean	Whether modular analysis is enabled or not.

9.2.3 AnalysisStart Element

An AnalysisStart element is an empty element that indicates the beginning of a main analysis.

The list of attributes of an AnalysisStart element are:

Attribute	Base Type	Description
top	xs:string	Name of the current top-level component.
concrete	xs:string	Names of the subcomponents whose implementation is used in the analysis (comma-separated list).
abstract	xs:string	Names of the subcomponents whose contract is used in the analysis (comma-separated list).
assumptions	xs:string	Comma-separated list of pairs (subcomponent name, number of considered invariants).

9.2.4 AnalysisStop Element

An `AnalysisStop` element is an empty element that indicates the end of a main analysis. No attributes.

9.2.5 Property Element

A `Property` element describes the result for a particular property of the input model. The result should be considered in the context of the analysis in which the property element is contained. The list of attributes of a `Property` element are:

Attribute	Base Type	Description
<code>name</code>	<code>xs:string</code>	Property identifier or description.
<code>scope</code>	<code>xs:string</code>	Name of the component where the property was analyzed.
<code>file</code>	<code>xs:string</code>	Associated input file, if any.
<code>line</code>	<code>xs:integer</code>	Associated line in the input file, if any.
<code>column</code>	<code>xs:integer</code>	Associated column in the input file, if any.
<code>source</code>	<code>xs:string</code>	Origin of the property. Can be <code>Assumption</code> if it comes from an assumption check, <code>Guarantee</code> if it comes from the check of a guarantee, <code>Ensure</code> if it comes from a check of an ensure clause in a contract mode, <code>OneModeActive</code> if it comes from an exhaustiveness check of the state space covered by the modes of a contract, and <code>PropAnnot</code> if it comes from the check of a property annotation.

A `Property` element contains one `Answer` element, which includes the result for the property check (`valid`, `falsifiable`, or `unknown`), and identifies the Kind 2 module responsible for the answer. If the result is `valid`, or `falsifiable`, it also contains a `Runtime` element, which reports the runtime of the analysis (in seconds), and whether the timeout expired or not. If the result is `valid`, a `K` element gives the value of `k` for which the property was proved valid. If the result is `falsifiable`, a `Counterexample` element describes a sequence of values for each stream that leads the system to the violation of the property. It also gives the list of contract modes that are active at each step, if any. If the result is `unknown`, the `Property` element may contain a `TrueFor` element specifying the largest value of `k` for which the property was proved to be true.

9.2.6 Stat Element

An `Stat` element provides statistics info about the current analysis. It has only one attribute of type `xs:string`, `source`, which is the name of the Kind 2 module which reported the piece of information. Its content consists in one or more `Section` elements. Each section has one `name` element, and one or more `item` elements. Each `item` element has one `name` element, and either a `value` element or a `valuelist` element. A `valuelist` has one or more `value` elements, and each `value` element has a `type` attribute (currently `int` or `float`), and its content is the actual value.

9.2.7 Progress Element

A `Progress` element is a simple element that reports the current value of `k` for a `k`-inductive-based analysis. It has only one attribute of type `xs:string`, `source`, which is the name of the `k`-inductive-based analysis.

9.2.8 PostAnalysisStart Element

An `PostAnalysisStart` element is an empty element that indicates the beginning of a post-analysis. It has only one attribute of type `xs:string`, the name of the post-analysis. The post-analyses currently available are [Test Generation](#) (`testgen`), [Proof Certificates](#) (`certification`), [Contract Generation](#) (`contractgen`), [Compilation to Rust](#) (`rustgen`), [Invariant Printing](#) (`invprint`), and [Inductive Validity Core](#) (`ivc`).

9.2.9 PostAnalysisEnd Element

An `PostAnalysisEnd` element is an empty element that indicates the end of a post-analysis. No attributes.

9.2.10 Execution Element

An `Execution` element describes the sequences of values for the output and state variables of an input model computed from the simulation of its execution (see the [interpreter](#) mode).

9.2.11 ModelElementSet Element

A `ModelElementSet` element describes a set of model elements (a model element can be an equation, a node call, an assumption, a guarantee, etc). It is used to describe a core that we can get from an [Inductive Validity Core](#) (`ivc`) or [Minimal Cut Set](#) (`mcs`) analysis. The result should be considered in the context of the analysis or post-analysis in which the `ModelElementSet` element is contained. The list of attributes of a `ModelElementSet` element are:

Attribute	Base Type	Description
<code>class</code>	<code>string</code>	Class of the core. Can be <code>must</code> , <code>must complement</code> , <code>ivc</code> , <code>ivc complement</code> , <code>mcs</code> or <code>mcs complement</code> .
<code>size</code>	<code>integer</code>	Number of model elements in the core.
<code>property</code>	<code>string</code>	The property associated with the core. If all properties are considered, this attribute is missing.

A `ModelElementSet` element contains one `Runtime` element, which indicates the runtime for computing the core. It also contains a sequence of `Node` elements, each one enumerating the model

elements in that node that are part of the core. When relevant, it can also contain a Counterexample element (see the Property element for more info).

10 Contract Semantics

10.1 Assume-guarantee contracts

This section discusses the semantics of contracts, and in particular modes, in Kind 2. For details regarding the syntax, please see the [Contracts](#) section.

An assume-guarantee contract (A, G) for a node n is a set of assumptions A and a set of guarantees G . Assumptions describe how n **must** be used, while guarantees specify how n behaves.

More formally, n respects its contract (A, G) if all of its executions satisfy the temporal LTL formula

$$\Box A \Rightarrow \Box G$$

That is, if the assumptions always hold then the guarantees hold. Contracts are interesting when a node top calls a node sub , where sub has a contract (A, G) .

From the point of view of sub , a contract $(\{a_1, \dots, a_n\}, \{g_1, \dots, g_m\})$ represents the same verification challenge as if sub had been written

```
node sub (...) returns (...);
let
  ...
  assert a_1;
  ...
  assert a_n;
  --%PROPERTY g_1;
  ...
  --%PROPERTY g_m;
tel
```

The guarantees must be invariant of sub when the assumptions are forced.

For the caller however, the call $sub(\langle params \rangle)$ is legal **if and only if** the assumptions of sub are invariants of top at call-site. The verification challenge for top is therefore the same as

```
node top (...) returns (...);
let
  ... sub(<params>) ...
  --%PROPERTY a_1(<call_site>);
  ...
  --%PROPERTY a_n(<call_site>);
tel
```

10.2 Modes

Kind 2 augments traditional assume-guarantee contracts with the notion of mode. A mode (R,E) is a set R or requires and a set E of ensures. A Kind 2 contract is therefore a triplet (A,G,M) where M is a set of modes. If M is empty then the semantics of the contract is exactly that of an assume-guarantee contract.

10.2.1 Semantics

A mode represents a situation / reaction implication. A contract (A,G,M) can be re-written as an assume-guarantee contract (A,G') where

$$G' = G \cup \left\{ \bigwedge_i r_i \Rightarrow \bigwedge_i e_i \mid (\{r_i\}, \{e_i\}) \in M \right\}$$

For instance, a (linear) contract for non-linear multiplication could be

```
node abs (in: real) returns (res: real) ;
let res = if in < 0.0 then - in else in ; tel

node times (lhs, rhs: real) returns (res: real) ;
(*@contract

mode absorbing (
  require lhs = 0.0 or rhs = 0.0 ;
  ensure res = 0.0 ;
) ;
mode lhs_neutral (
  require not absorbing ;
  require abs(lhs) = 1.0 ;
  ensure abs(res) = abs(rhs) ;
) ;
mode rhs_neutral (
  require not absorbing ;
  require abs(rhs) = 1.0 ;
  ensure abs(res) = abs(lhs) ;
) ;
mode positive (
  require (
    rhs > 0.0 and lhs > 0.0
  ) or (
    rhs < 0.0 and lhs < 0.0
  ) ;
  ensure res > 0.0 ;
) ;
mode pos_neg (
```

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```

require (
  rhs > 0.0 and lhs < 0.0
) or (
  rhs < 0.0 and lhs > 0.0
) ;
ensure res < 0.0 ;
) ;
*)
let
  res = lhs * rhs ;
tel

```

Motivation: modes were introduced in the contract language of Kind 2 to account for the fact that most requirements found in specification documents are actually implications between a situation and a behavior. In a traditional assume-guarantee contract, such requirements have to be written as `situation => behavior` guarantees. We find this cumbersome, error-prone, but most importantly we think some information is lost in this encoding. Modes make writing specification more straightforward and user-friendly, and allow Kind 2 to keep the mode information around to

- improve feedback for counterexamples,
- generate mode-based test-cases, and
- adopt a defensive approach to guard against typos and specification oversights to a certain extent. This defensive approach is discussed in the next section.

10.2.2 Defensive check

Conceptually modes correspond to different situations triggering different behaviors for a node. Kind 2 is defensive in the sense that when a contract has at least one mode, it will check that the modes account for **all situations** the assumptions allow before trying to prove the node respects its contract.

More formally, consider a node `n` with contract

$$(A, G, \{(R_i, E_i)\})$$

The defensive check consists in checking that the disjunction of the requires of each mode

$$\text{one_mode_active} = \bigvee_i (\bigwedge_j r_{ij})$$

is an invariant for the system

$$A \wedge G \wedge (\bigwedge_i r_i \Rightarrow \bigwedge_i e_i)$$

If `one_mode_active` is indeed invariant, it means that as long as

- the assumptions are respected, and

- the node is correct w.r.t. its contract then at least one mode is active at all time.

Kind 2 follows this defensive approach. If a mode is missing, or a requirement is more restrictive than it should be then Kind 2 will detect the modes that are not exhaustive and provide a counterexample.

This defensive approach is not as constraining as it first appears. If one wants to leave some situation unspecified on purpose, it is enough to add to the current set of (non-exhaustive) modes a mode like

```
mode base_case (  
  require true ;  
) ;
```

which explicitly accounts for, and hence documents, the missing cases.

11 Post Analysis Treatments

Post-analysis treatments are flag-activated Kind 2 features that are not directly related to verification. The current post-analysis treatments available are

- certification,
- compilation to Rust,
- test generation,
- contract generation,
- invariant printing, and
- inductive validity core generation

All of them are deactivated by default. Post-analysis treatments run on the last analysis of a system. It is defined as the last analysis performed by Kind 2 on a given system. With the default settings, Kind 2 performs a single, monolithic analysis of the top node. In this case, the last analysis is this unique analysis.

This behavior is changed by the `compositional` flag. For example, say Kind 2 is asked to analyze node `top` calling two subnodes `sub_1` and `sub_2`, in compositional mode. Say also `sub_1` and `sub_2` have contracts, and that refinement is possible. In this situation, Kind 2 will analyze `top` by abstracting its two subnodes. Assume for now that this analysis concludes the system is safe. Kind 2 has nothing left to do on `top`, so this compositional analysis is the last analysis of `top`, Kind 2 will run the post-analysis treatments. Assume now that this purely compositional analysis discovers a counterexample. Since refinement is possible, Kind 2 will refine `sub_1` (and/or `sub_2`) and start a new analysis. Hence, the first, purely compositional analysis is not the last analysis of `top`. The analysis where `sub_1` and `sub_2` are refined is the last analysis of `top` regardless of its outcome (assuming no other refinement is possible).

Long story short, the last analysis of a system is either the first analysis allowing to prove the system safe, or the analysis where all refineable systems have been refined.

The `modular` flag forces Kind 2 to apply whatever analysis / treatment the rest of the flags specify to all the nodes of the system, bottom-up. Post-analysis treatments respect this behavior and will run on the last analysis of each node.

11.1 Prerequisites

Some treatments can fail (which results in a warning) because some conditions were not met by the system and/or the last analysis. The prerequisites for each treatment are:

Treatment	Conditions	Notes
certification	last analysis proved the system safe	will fail if node is partially defined
compilation to Rust		
test generation	system has a contract with more than one mode and the last analysis proved the system safe	
contract generation		experimental
invariant printing		
inductive validity core generation	last analysis proved the system safe	

12 Test Generation

Disclaimer: Test generation is, as of Kind 2 1.0, still a rather experimental feature. In particular, it works only for models whose nodes have inputs and outputs of simple type (int, real, bool, and enum), not structured type (record, tuple, or array). There is a lot of room for improvement and the Kind 2 team welcomes feedback / bug reports.

Most test generation techniques analyze the syntax of the model they run on to generate test cases satisfying some coverage criteria. Kind 2 does not follow this approach but instead generates tests based on the specification, more precisely the modes of the specification.

Kind 2's test generation was developed in a context where the actual implementation of the components is **outsourced**. That is, a model of the system is written in-house based on some specification. The model is then verified correct with respect to its specification, using Kind 2 of course, before the specification is given to external sub-contractors that will eventually produce some binaries but will **not** give access to their source code. At this point, there is a need to test these binaries in-house.

In this context, syntactic test generation is arguably not appropriate as it would be based on the syntax of the model, not that of the actual source code of the binaries. There is no reason to believe any connection between the two. Now, the only thing we know of the binaries is that they are supposed to verify the specification. For this reason, Kind 2's test generation ignores the syntax of the input model and instead builds on contracts (see [Contract Semantics](#)), and more precisely on the notion on mode.

12.1 Combinations of modes as abstractions

Modes specify behaviors specific to a situation in a contract, and can be seen as abstractions of the states allowed by the assumptions of the contract. Note that because of the mode exhaustiveness check, there is always at least one mode active in any reachable state.

One can explore, starting from the initial states, the mode that can be activated up to some depth. For example, consider the following stopwatch system:

```
contract stopwatchSpec ( tgl, rst : bool ) returns ( c : int ) ;
let
  var on: bool = tgl -> (pre on and not tgl) or (not pre on and tgl) ;
  assume not (rst and tgl) ;
  guarantee c >= 0 ;
  mode resetting ( require rst ; ensure c = 0 ; ) ;
  mode running (
    require not rst ; require on ; ensure c = (1 -> pre c + 1) ;
  ) ;
  mode stopped (
    require not rst ; require not on ; ensure c = (0 -> pre c) ;
```

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```
) ;
tel

node previous ( x : int ) returns ( y : int ) ;
let
  y = 0 -> pre x ;
tel

node stopwatch ( toggle, reset : bool ) returns ( count : int ) ;
(*@contract
  import stopwatchSpec ( toggle, reset ) returns ( count ) ;
*)
var running : bool ;
let
  running = (false -> pre running) <> toggle ;
  count = if reset then 0 else
    if running then previous(count) + 1 else previous(count) ;
tel
```

It seems that any of the three modes from the contract can be active at any point, since their activation only depends on the values of the inputs. We can ask Kind 2 to generate the graph of mode paths up to some depth (5 here):

```
kind2 --testgen true --testgen_len 5 stopwatch.lus
```

This will generate the following graph (and a lot of other files we will discuss below but omit for now):

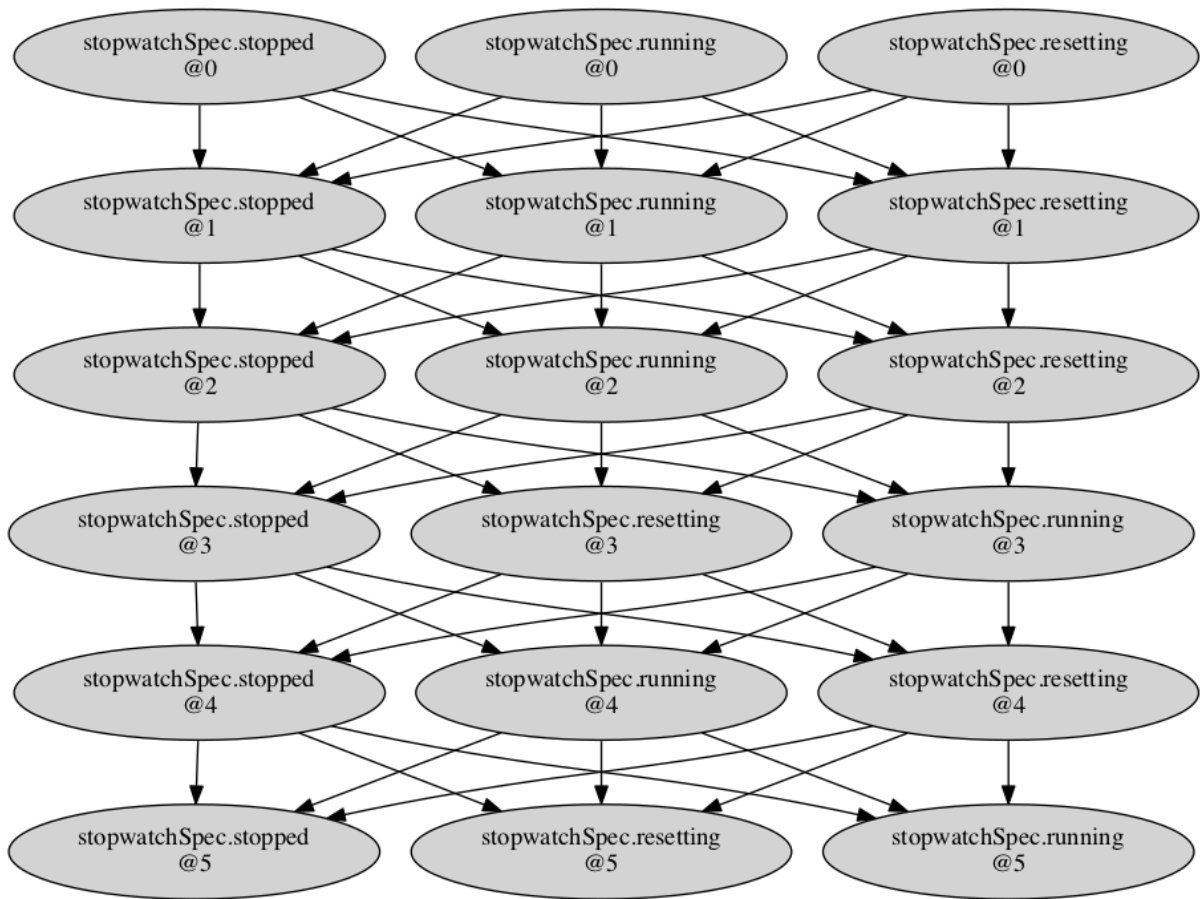


Fig. 1: Stopwatch DAG

The graph confirms our understanding of the specification, each mode can be activated at any time. Say now we made a mistake on the assumption:

```
assume not (rst or tgl) ;
```

It is now illegal to reset or start the stopwatch. The graph is generated very quickly as with this assumption the system cannot do anything:

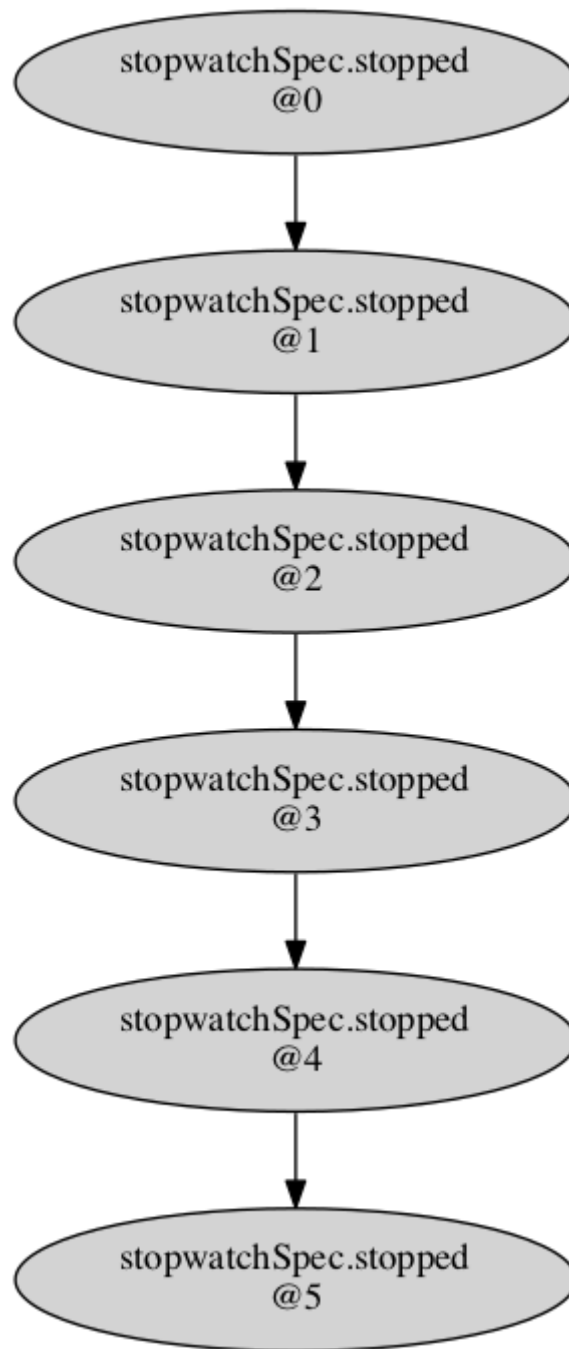


Fig. 2: Stopwatch mistake DAG

N.B. In this simple system, only one mode could be active at a time. This is not the case in general. See for example the mode graphs for the [mode logic](#) or the [full model](#) of the Transport Class Model (TCM) case study.

12.2 Generating test cases

Since Kind 2 can explore the traces of combinations of modes that can be activated from the initial states, generating test cases is simple. Each test case is simply a trace of inputs, or witness, triggering a different path of mode combinations in the DAG discussed above.

Each witness is logged in CSV file. A glue XML file lists all the test cases and provides additional information such as the trace of mode combinations they triggered in the model.

But aren't the witnesses still based on how the model is written?

Yes they are. There is no way to completely abstract the model/prototype away, nor is it desirable. Generating test cases solely on the specification is not realistic unless the specification is extremely strong and precise, which it very rarely is. (Also, if it was, it would arguably be easier to produce the object code as a refinement of the specification using the B-method for instance.)

12.3 Oracle generation

The point of generating these test cases is to eventually run them on an executable version of the model to check whether it crashes and respects the specification.

For convenience, Kind 2 automatically generates an executable oracle along with the test cases. It takes the form of a Rust project in the `oracle` subdirectory of the Kind 2 output directory. The best way to learn about how this oracle behaves is to generate and read its documentation by running `cargo doc` in said subdirectory and opening `target/doc/<system>/index.html`.

The idea is that this oracle will read comma-separated values on its standard input. These values correspond to the inputs fed to the System Under Test (SUT), followed by the values returned by the SUT. The oracle prints back the truth values of the guarantees / modes of the original contract as comma-separated values. (How the outputs are organized depends on your system and is currently not standardized. Refer to the oracle's documentation.)

Keeping in mind a test case is a sequence of input values each corresponding to a step or cycle for the SUT, the workflow is

- read inputs `ins` for current step from the test case file
- feed it to the SUT, obtaining some outputs `outs`
- write `ins` and `outs` as comma-separated values on the oracle's standard input
- read the truth values for the original contract on the oracle's standard output

Note: In general, the values for the contract depend on previous values of the SUT's inputs / outputs. In the workflow described above, the oracle keeps running between each step so that it can remember the information it needs from the previous steps to produce the next guarantee/mode truth values.

12.4 An example of a Test Execution Engine

A Test Execution Engine (TEE) compatible with Kind 2's test cases and oracles is available here:

<https://github.com/kind2-mc/teas>

Teas is written in Python, and is able to compare a binary with Kind 2's test cases using the oracle described above.

Disclaimer: Like Kind 2's test generation feature, Teas is in an experimental and unstable state.

13 Compilation to Rust

Disclaimer: While this feature has been tested on rather large systems, is still considered experimental. The Kind 2 team welcomes feedback / bug reports.

[Rust](#) is a very efficient language with a focus on safety. Kind 2 can compile Lustre to Rust, as long as the input system does not have **any unguarded pre's**, regardless of whether the initial undefined value is actually used. Arrays and records are currently **not** supported.

Compilation is activated by the `--compile true` flag.

The result is a Rust project in the `implem` subdirectory of the Kind 2 output directory. The project is extensively documented, you can read the documentation by running `cargo doc` in the project directory and opening `target/doc/<system>/index.html`.

13.1 Technical details

The project produces a binary that reads inputs as comma-separated values from its standard input and prints back outputs as comma-separated values on its standard output. Lustre's `reals` are compiled as 64-bits floats while `ints` become `usize`: 32-bits (64-bits) signed integers on 32-bits (64-bits) platforms.

Note:* Technically, this conversion is unsound because the semantics of `int` is mathematical (aka, infinite precision) integers, not machine integers, and that of `real` is mathematical real numbers, not floating point numbers.

13.2 Assertions, properties and contracts

Compilation in Kind 2 works under the assumption that the model has been proved correct. Therefore properties, guarantees, and modes are not compiled as they have already been proved at model-level.

To be precise, since Kind 2 works with mathematical integers and reals, it can be the case that the binary actually falsifies the specification for generating a floating point overflow, underflow, and NaN or for using integer arithmetic modulo `n`. We are considering offering to compile properties / guarantees / modes optionally through a flag.

Assertions and assumptions from the original models are compiled as internal checks and, when falsified, will cause the binary to stop after outputting an error message pointing to the assertion / assumption falsified in the original Lustre model.

14 Proof Certificates

One clear strength of model checkers, as opposed to proof assistants, say, is their ability to return precise error traces witnessing the violation of a given safety property. Such traces not only are invaluable for designers to correct bugs, they also constitute a checkable certificate. For instance Kind 2 display a counter-example trace that shows the evolution of values of all variables in the system up to a violation of the property. In most cases, it is possible to use a counter-example for a safety property to direct the execution of the system under analysis to a state that falsifies that property. In contrast, most model checkers are currently unable to return any form of corroborating evidence when they declare a safety property to be satisfied by the system. This is unsatisfactory in general since these are complex tools based on a variety of sophisticated algorithms and search heuristics, and so are not immune to errors.

To mitigate this problem, Kind 2 accompanies its safety claims with a certificate, an artifact embodying a proof of the claim. The certificate can then be validated by a trusted certificate/proof checker, in our case the [LFSC checker](#).

14.1 Certification chain

The certification process for Kind 2 is depicted in the graph below. Kind 2 generates two sorts of safety certificates, in the form of SMT-LIB 2 scripts: one certifying the faithfulness of the translation from the Lustre input model to the internal encoding, and another one certifying the invariance of the input properties for the internal encoding of the input system. These certificates are checked by cvc5, then turned into LFSC proof objects by collecting cvc5's own proofs and assembling them to form an overall proof that can be efficiently verified by the LFSC proof checker.

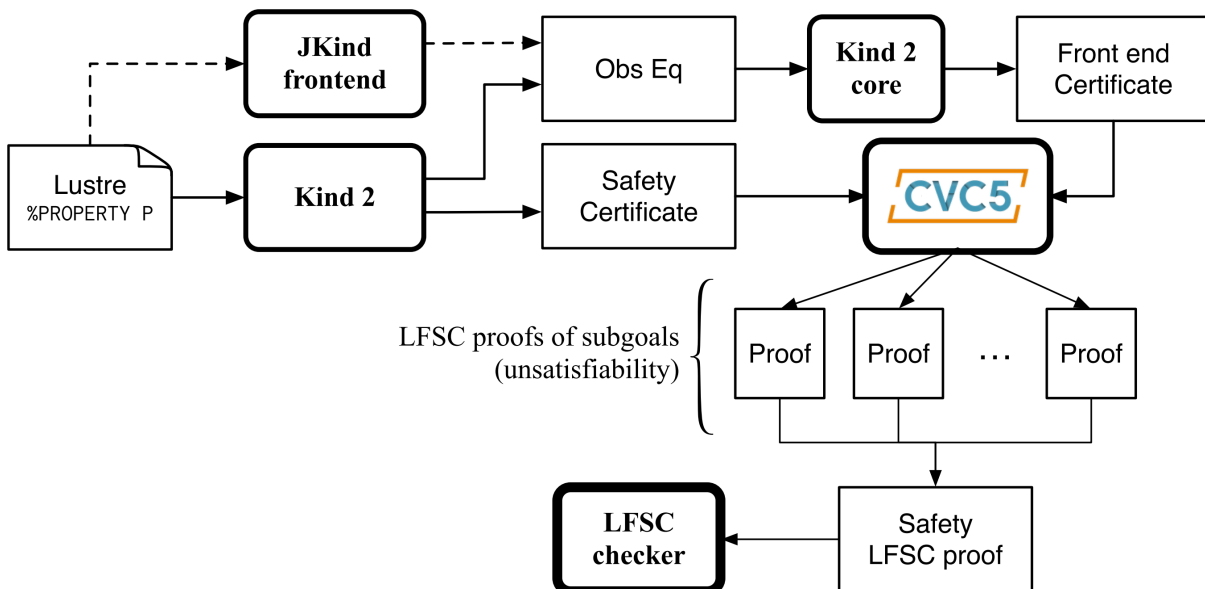


Fig. 1: Certification process

Trust is claimed at a higher level when both proof certificates are present. In practice, this means that Kind 2 didn't make any mistake in its model checking phase, and that the translation of the Lustre model to the internal representation is faithful.

14.2 Producing certificates and proofs with Kind 2

To illustrate this process, we rely on the toy model below (`add_two.lus`). The model encodes in Lustre a synchronous reactive component, `add_two`, that at each execution step other than the first, outputs the maximum between the previous value of its output variable `c` and the sum of the current values of input variables `a` and `b`. The value of `c` is initially `1.0`. The model is annotated with an invariance property stating that, at each step, the output `c` is positive whenever both inputs are.

```
node add_two (a, b : real) returns (c : real) ;
  var v : real;
      P : bool;
let
  v = a + b ;
  c = 1.0 -> if (pre c) > v then (pre c) else v ;
  P = (a > 0.0 and b > 0.0) => c > 0.0 ;
  --%PROPERTY P;
tel
```

Kind 2 offers the possibility to generate two types of certificates, SMT-LIB 2 certificates and actual proofs in the format of LFSC. It will do so only for systems whose properties (or contracts) are all proven valid.

14.2.1 Requirements

Frontend certificates and proofs production require the user to have JKind installed on their machine (together with a suitable version of Java).

SMT-LIB 2 certificates do not require anything additional except for an SMT solver to check the certificates.

LFSC proofs production requires `cvc5` (the binary can be specified with `--cvc5_bin`), its LFSC proof signatures, and the LFSC checker for the final proof checking phase.

LFSC checker

A bash script to download and build the LFSC checker is distributed with Kind 2:

```
lfsc/get-lfsc-checker.sh
```

The script also downloads the cvc5 LFSC signatures and generates an easy-to-use bash script (`lfsc-check.sh`) to check LFSC proofs generated by Kind 2:

```
lfsc
|-- get-lfsc-checker.sh
|-- bin
    |-- lfsc
    |-- lfsc-check.sh
|   ...
|-- signatures
    |-- arith_programs.plf
    |-- ...
```

14.2.2 SMT-LIB 2 certificates

These certificates are always produced but are only used as an intermediate step for LFSC proof production. The user still has the possibility to get them as the final output of Kind 2 in a convenient form. To do so, invoke Kind 2 (on the previous example `add_two.lus`) with the following:

```
kind2 --certif true add_two.lus
```

For successful runs, the output of Kind 2 will contain:

```
Post-analysis: certification

Certificate checker was written in add_two.lus.out/certif/certificate.smt2
Generating frontend eq-observer with jKind ...
Generating frontend certificate
...
Certificate checker was written in add_two.lus.out/certif/FEC.kind2.out/certif/FECC.
↔smt2
```

The certificates are located in the directory `add_two.lus.out/certif` which has the following structure:

```
add_two.lus.out/certif
|-- certificate_checker
|-- certificate_prelude.smt2
|-- certificate.smt2
|-- FEC.kind2
```

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```
|-- FEC.kind2.out/certif
  |-- FECC_checker
  |-- FECC_prelude.smt2
  |-- FECC.smt2
  |-- observer_sys.smt2
|-- jkind_sys_lfsc_trace.smt2
|-- jkind_sys.smt2
|-- kind2_sys.smt2
|-- observer_lfsc_trace.smt2
|-- observer.smt2
```

In particular, it contains two scripts of interest: `certificate_checker` and `FECC_checker`. They are meant to be run with the name of an SMT solver as argument and should produce each three `unsat` results. The first one checks that the certificate of invariance is valid with the provided SMT solver and the second script checks that the frontend certificate is valid.

```
> add_two.lus.out/certif/certificate_checker z3
Checking base case
unsat
Checking 1-inductive case
unsat
Checking property subsumption
unsat

> add_two.lus.out/certif/FEC.kind2.out/certif/FECC_checker z3
Checking base case
unsat
Checking 1-inductive case
unsat
Checking property subsumption
unsat
```

14.2.3 LFSC proofs

The other option offered by Kind 2, and the most trustworthy one, is to produce LFSC proofs. This can be done with the following invocation:

```
kind2 --proof true add_two.lus
```

Successful runs emit outputs that contain lines such as:

```
Post-analysis: certification

Generating frontend eq-observer with jKind ...
```

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```
Generating frontend proof
...
Final LFSC proof written to add_two.lus.out/add_two.lus.1.lfsc
```

The important one is the last message that indicate the file in which the proof was written. The directory produced by Kind 2 will have the following structure:

```
add_two.lus.out/
|-- add_two.lus.1.lfsc
|-- certificates.1
    |-- FEC.kind2
    |-- base.smt2
    |-- frontend_base.smt2
    |-- frontend_implication.smt2
    |-- frontend_induction.smt2
    |-- frontend_proof.lfsc
    |-- implication.smt2
    |-- induction.smt2
    |-- jkind_sys.smt2
    |-- jkind_sys_lfsc_trace.smt2
    |-- kind2_phi.smt2
    |-- kind2_phi_lfsc_trace.smt2
    |-- kind2_sys.smt2
    |-- kind2_sys_lfsc_trace.smt2
    |-- obs_phi.smt2
    |-- obs_phi_lfsc_trace.smt2
    |-- observer.smt2
    |-- observer_lfsc_trace.smt2
    |-- proof.lfsc
```

It contains as many proofs (at the root) as there are relevant analysis performed by Kind 2 (for modular and compositional reasoning). To make sure that the proof is an actual proof, one needs to call the LFSC checker on the generated output, together with the correct signatures:

```
lfsc/bin/lfsc <cvc5 signatures in order> <kind 2 signature> add_two.lus.out/add_two.
↪lus.1.lfsc
```

or use the convenient bash script generated by `lfsc/get-lfsc-checker.sh`:

```
lfsc/bin/lfsc-check.sh add_two.lus.out/add_two.lus.1.lfsc
```

The return code for either command execution is 0 when everything was checked correctly.

When the bash script is used and the whole proof is correct, the following line will be displayed:

```
Valid LFSC proof!
```

When the LFSC checker is called instead, three lines will be displayed when both the proof of invariance and the proof of correct translation by the frontend are valid:

```
success
success
success
```

In the case where only the invariance proof was produced and checked, the return code will still be 0 but only a single success will be in the output.

14.2.4 Proof options

Kind 2 supports several options to control the format and granularity of proofs:

- `--smaller_holes <bool>` (default `false`) – By default, LFSC proofs generated by Kind 2 contain holes encoded as `(trust ..)` steps. This option reduces the size of holes in the generated proofs, and thus, increases trust in Kind 2's result. The option is disabled by default as the more granular proofs take significantly more time to generate, are orders of magnitude larger, and take longer time to verify than proofs with bigger holes. Note: this option reduces the size of holes in the proofs and not their number, which is likely to increase when it is enabled.
- `--flatten_proof <bool>` (default `false`) – Break the proof down into a sequence of lemmas. The proof for each lemma is verified by the LFSC checker and erased immediately. This option helps reduce the memory footprint of the LFSC checker and improve its performance. It is recommended to enable this option with `--smaller_holes`. Note: enabling this option will increase the number of success messages displayed by the LFSC checker.

14.3 Contents of certificates

For a given problem (whose safety property is P), an internal certificate consists in only a pair (k, ϕ) where ϕ is a k -inductive invariant of the system which implies the original properties. SMT-LIB 2 certificates are in fact scripts whose check make sure that ϕ implies P and is k -inductive. The LFSC proof is a formal proof that P is invariant in the system, using sub-proofs of validity (unsatisfiability) returned by `cvc5`.

14.4 LFSC signature

A proof system is formally defined in LFSC through signatures, which contain a definition of the system's language together with axioms and proof rules. The proof system used by `cvc5` is defined over a number of signatures, which are included in its source code distribution. Those relevant to this work include signatures for propositional logic and resolution (`boolean_rules.plf`); first-order terms and formulas, with rules for CNF conversion and abstraction to propositional logic (`cnf_rules.plf`); equality over uninterpreted functions (`equality_rules.plf`); and real and integer linear arithmetic (`arith_rules.plf`).

`cvc5`'s proof system is extended with an additional signature (`kind.plf`) for k-inductive reasoning, invariance and safety. This signature also specifies the encoding for state variables, initial states, transition relations, and property predicates. State variables are encoded as functions from natural numbers to values. This way, the unrolling of the transition relation does not need the creation of several copies of the state variable tuple \mathbf{x} . For example, for the state vector $\mathbf{x} = (y, z)$ with y of type real and z of type integer, the LFSC encoding will make y and z respectively functions from naturals to reals and integers. So we will use the tuples $(y(0), z(0))$, $(y(1), z(1))$, ... instead of (y_0, z_0) , (y_1, z_1) , ... where $y_0, y_1, \dots, z_0, z_1, \dots$ are (distinct) variables. Correspondingly, our LFSC encoding of a transition relation formula $T[\mathbf{x}, \mathbf{x}']$ is parametrized by two natural variables, the index of the pre-state and of the post-state, instead of two tuples of state variables. Similarly, I, P and ϕ are parametrized by a single natural variable.

The signature defines several derivability judgments, including one for proofs of invariance, which has the following type:

$$\begin{aligned} \text{invariant} &: \Pi I : \mathbb{N} \rightarrow \text{formula}. \\ \Pi T &: \mathbb{N} \rightarrow \mathbb{N} \rightarrow \text{formula}. \\ \Pi I &: \mathbb{N} \rightarrow \text{formula.Type} \end{aligned}$$

It also contains various rules to build proofs of invariance by k-induction. This signature also specifies how to encapsulate proofs for the front-end certificates by providing a additional judgment, $\text{safe}(I, T, P, I', T', P')$, which can be derived only when $\text{invariant}(I, T, P)$ is derivable and the observational equivalence between (I, T, P) and (I', T', P') is provable (judgment `woe`). Self contained proofs of safety follow the sketch depicted below, where `Smt` stands for an unsatisfiability rule whose proof tree is obtained, with minor changes, from a proof produced by `cvc5`.

$$\begin{array}{c} \text{K-IND} \frac{k \in \mathbb{N} \quad \text{SMT} \frac{\vdots}{B_k \models \perp} \quad \text{SMT} \frac{\vdots}{S_k \models \perp}}{\text{invariant}(I, T, \phi)} \quad \text{SMT} \frac{\vdots}{\phi \models P} \\ \text{INVIMPL} \frac{\text{invariant}(I, T, \phi)}{\text{invariant}(I, T, P)} \quad \text{K-IND} \frac{\vdots}{\text{invariant}(I_o, T_o, \phi_o)} \quad \text{SMT} \frac{\vdots}{\phi_o \models P_o} \\ \text{OBS EQ} \frac{\text{invariant}(I_o, T_o, P_o)}{\text{woe}(I, T, P, I', T', P')} \\ \text{INV+OBS} \frac{\text{invariant}(I, T, P) \quad \text{woe}(I, T, P, I', T', P')}{\text{safe}(I, T, P)} \end{array}$$

Fig. 2: Proof sketch

15 Contract Generation

Disclaimer: This feature is very experimental. In particular, the modes (if any) of the contracts generated might not be exhaustive. In this case, Kind 2 will reject the contract during the mode exhaustiveness check.

Contract generation is intended, at least for now, as a helper for users to getting started with Kind 2's contract language. Contract generation is activated by the flag `--contract_gen`.

Internally, this feature is implemented by running invariant generation on the input system up to some depth, specified by flag `--contract_gen_depth`. Doing so will discover equivalence and implication invariants over the system. The ones that talk only about the input / outputs of the systems are used to create the contract dumped in a Lustre file in the output directory. Note that the restriction to just input and output variables causes many of the generated invariants to be discarded currently.

16 Invariant Printing

This treatment minimizes the invariants used in the proof of the valid properties, and shows them in the output without logging them on disk.

17 Interpreter

The interpreter is a special mode where Kind 2 reads input values from a file and prints the computed values for the output and local variables of a node at each step. If the Lustre file contains two or more top nodes, a single node must be selected with either the command-line option `--lustre_main <node_name>` or a single `--%MAIN` annotation in the Lustre file.

To use the interpreter, run:

```
kind2 --enable interpreter <lustre_file> --interpreter_input_file <input_file>
```

You can specify the number of steps to run with the option `--interpreter_steps <int>`. By default, the number of steps is determined by the input file.

17.1 Structure of the input file

The inputs must be specified in a JSON file.

The overall structure is as follows:

```
[
  {
    "var1": "42",
    "var2": true,
    "var3": "0.5"
  },
  {
    "var1": "24",
    "var2": false,
    "var3": "1.0/2.0"
  }
]
```

The top-level JSON array corresponds to the successive time steps. Each time step is described by a JSON object associating to each input variable its value for this time step.

NOTE: Kind2 also accepts the CSV format for backward compatibility reasons. However, it does not support records, arrays and tuples. Please give your input file the adequate extension (*.json or *.csv) in order to indicate to Kind2 which format you are using.

17.2 Integers and reals

As in the above example, integers and reals should be written as strings in order to avoid a potential loss of precision or an integer overflow while parsing the file. Nevertheless, small integers can be written as native JSON integers without problem.

17.3 Records

Record values can be expressed using a JSON object.

For instance, a variable `c` of type `{ re: real; im: real }` can be assigned as follows:

```
[
  {
    "c": { "re": "-1.0", "im": "0.25" }
  }
]
```

17.4 Arrays

Array values can be expressed using a JSON array.

For instance, a variable `a` of type `bool^3^2` can be assigned as follows:

```
[
  {
    "a": [[true, true, false], [false, true, true]]
  }
]
```

17.5 Tuples

The JSON format does not support tuples by default. However, Kind2 extends the JSON syntax so that tuples can be easily expressed.

For instance, a variable `t` of type `[int, bool, real]` can be assigned as follows:

```
[
  {
    "t": ("36", false, "5.0")
  }
]
```


An alternative syntax using a JSON object is allowed in case you want to produce a valid JSON file:

```
[
  {
    "t": { "0": "36", "1": false, "2": "5.0" }
  }
]
```

18 Inductive Validity Core

The inductive validity core generation is a post-analysis treatment that computes a minimal subset of the model elements (assumptions, guarantees, stateful equations, or node calls) that are sufficient to prove all valid properties.

To enable inductive validity core generation, run

```
kind2 <lustre_file> --ivc true
```

18.1 Options

- `--ivc_category {node_calls|contracts|equations|assertions|annotations}` (default: all categories) – Minimize only a specific category of elements, repeat option to minimize multiple categories
- `--ivc_only_main_node <bool>` (default false) – Only elements of the main node are considered in the computation
- `--ivc_all <bool>` (default false) – Compute all the Minimal Inductive Validity Cores
- `--ivc_approximate <bool>` (default true) – Compute an approximation (superset) of a MIVC. Ignored if `--ivc_all` or `--ivc_must_set` is true
- `--ivc_smallest_first <bool>` (default false) – Compute a smallest IVC first. If `--ivc_all` is false, the computed IVC will be a smallest one
- `--ivc_must_set <bool>` (default false) – Compute the MUST set in addition to the IVCs
- `--print_ivc <bool>` (default true) – Print the inductive validity core computed
- `--print_ivc_complement <bool>` (default false) – Print the complement of the inductive validity core computed (= the elements that were not necessary to prove the properties)
- `--minimize_program {no|valid_lustre|concise}` (default no) – Minimize the source Lustre program according to the inductive validity core(s) computed
- `--ivc_output_dir <string>` (default `<INPUT_FILENAME>`) – Output directory for the minimized programs
- `--ivc_uc_timeout <int>` (default 0) – Set a timeout for each unsat core check sent to the solver
- `--ivc_precomputed_mcs <int>` (default 0) – When computing all MIVCs, set a cardinality upper bound for the precomputed MCSs (helps prune space of candidates)

18.2 Example

Let's consider the following Lustre code:

```
contract fSpec(u,v: real) returns(r: real);
let
  guarantee r >= 0.0;
  guarantee true -> r >= pre(r);
  guarantee r >= u;
  guarantee r >= v;
tel;

node f(u, v : real) returns (r : real);
(*@contract import fSpec(u,v) returns (r) ; *)
var m1,m2: real;
let
  m1 = if v > u then v else u;
  m2 = if m1 > 0.0 then m1 else 0.0;
  r = m2 -> if pre(r) > m1 then pre(r) else m1;
tel;

node main(x, y : real) returns (P : bool);
var a,b : real;
let
  a = f(x,y);
  b = f(y,x);
  P = a >= x and a >= y and b >= x and b >= y;
  --%PROPERTY P;
tel;
```

If we are interesting in determining which guarantees of the contract `fSpec` of `f` are needed to prove `P`, we should run this command:

```
kind2 <lustre_file> --ivc true --ivc_category contracts --ivc_only_main_node false --
↔compositional true
```

- `--ivc_category contracts`: because we are only interested in minimizing the contract `fSpec`
- `--ivc_only_main_node false`: because `fSpec` is not the contract of the main node, so we need to consider all nodes
- `--compositional true`: as we want to minimize the contract of `f` and not its implementation, we need to enable compositional analysis

We obtain the following inductive validity core:

```
IVC (2 elements):
```

(continues on next page)

```

Node f
  Guarantee fSpec[l11c12].guarantee[l6c4][3] at position [l6c4]
  Guarantee fSpec[l11c12].guarantee[l7c4][4] at position [l7c4]

```

18.3 Minimizing over a subset of the assumptions/guarantees

If you are interested in computing an IVC among a subset of the assumptions or guarantees, you can use the category annotations. The assumptions and guarantees that should be considered must be preceded by the keyword `weakly`. All the other assumptions and guarantees will be considered as always present when computing the IVCs.

For instance, we can modify the previous example as follows:

```

contract fSpec(u,v: real) returns(r: real);
let
  weakly guarantee r >= 0.0;
  guarantee true -> r >= pre(r);
  weakly guarantee r >= u;
  guarantee r >= v;
tel;

```

```

kind2 <lustre_file> --ivc true --ivc_category annotations --ivc_only_main_node false -
↔-compositional true

```

We obtain the following inductive validity core:

```

IVC (1 elements):
Node f
  Guarantee fSpec[l11c12].weakly_guarantee[l6c4][3] at position [l6c4]

```

18.4 Computing all Inductive Validity Cores

If we want to compute ALL the minimal inductive validity cores, we can use the following flags:

```

kind2 <lustre_file> --ivc true --ivc_all true

```

- `--ivc_all true`: specify that we want to compute all the IVCs

19 Minimal Cut Set

The minimal cut set generation is a special mode where Kind 2 computes a minimal subset of the model elements (assumptions, guarantees, stateful equations, or node calls) whose no satisfaction leads to the violation of a property.

To enable minimal cut set generation, run

```
kind2 <lustre_file> --enable MCS
```

19.1 Options

- `--mcs_category {annotations|node_calls|contracts|equations|assertions}` (default: annotations) – Consider only a specific category of elements, repeat option to consider multiple categories
- `--mcs_only_main_node <bool>` (default false) – Only elements of the main node are considered in the computation
- `--mcs_all <bool>` (default false) – Specify whether all the Minimal Cut Sets must be computed or just one
- `--mcs_approximate <bool>` (default true) – Compute a MCS which is minimal with respect to all the counterexamples of the same length that the first counterexample found. This solution can be considered an approximation of a global one. Ignored if `--mcs_all` is true
- `--mcs_max_cardinality <int>` (default -1) – Only search for MCSs of cardinality lower or equal to this parameter. If -1, all MCSs will be considered
- `--mcs_per_property <bool>` (default true) – If true, MCSs will be computed for each property separately
- `--print_mcs <bool>` (default true) – Print the minimal cut set computed
- `--print_mcs_complement <bool>` (default false) – Print the complement of the minimal cut set computed (this is equivalent to computing a Maximal Unsafe Abstraction)
- `--print_mcs_legacy <bool>` (default false) – Print the minimal cut set using the legacy format
- `--print_mcs_counterexample <bool>` (default false) – Print a counterexample for each MCS found (ignored if `--print_mcs_legacy` is true)
- `--mcs_per_property <bool>` (default true) – If true, MCSs will be computed for each property separately

19.2 Example

Let's consider the following Lustre code:

```
contract spec(x,y: real) returns(z: real);
let
  weakly assume x = -y;
  weakly assume x >= 0.0;
tel;

node main(x, y : real) returns (z : real);
(*@contract import spec(x,y) returns (z) ; *)
var P : bool;
let
  z = x + y;
  P = z = 0.0;
  --%MAIN;
  --%PROPERTY P;
tel;
```

If you are interesting in determining a minimal set of the weak assumptions of the contract `fSpec` whose no satisfaction leads to the violation of `P`, you can run this command:

```
kind2 <lustre_file> --enable MCS --mcs_category annotations
```

Note that `--mcs_category annotations` is not required since it is the default value.

The following minimal cut set is printed:

```
MCS (1 elements) for property P:
Node main
  Assumption spec[l9c12].weakly_assume[l4c4][1] at position [l4c4]
```

In the example above, the `weakly` keyword is used to annotate the assumptions and guarantees to consider for the MCS computation (Kind2 will only try to remove these assumptions and guarantees, all the others will be kept).

Alternatively, if we want to compute a MCS over all the assumptions and guarantees, we can change the category to `contracts`:

```
kind2 <lustre_file> --enable MCS --mcs_category contracts
```

20 Contract Check

When an input model includes [imported nodes](#), it is important to check that the contracts associated with them can be realized, i.e., it is possible to construct a component such that for any input allowed by the contract assumptions, there is some output value that the component can produce that satisfies the contract guarantees.

To check the contracts of imported nodes, run

```
kind2 --enable CONTRACTCK <lustre_file>
```

If Kind 2 is able to prove some contract unrealizable and the `--print_deadlock` flag is true, Kind 2 will show a deadlocking trace such that all states except the last one satisfy the contract constraints. If the trace only has one state, the state shows input values such that no initial state values satisfy the contract constraints (including the state values chosen as sample). For traces with more than one state, the trace is such that no next state values satisfy the contract constraints from the second-to-last state giving the input values of the last state. Kind 2 will also show a set of conflicting constraints for the last state in the trace.

When the `--check_contract_is_sat` flag is true, Kind 2 will also check whether the unrealizable contract is at least satisfiable, i.e., it is possible to construct a component such that for at least one input sequence allowed by the contract assumptions, there is some output value that the component can produce that satisfies the contract guarantees.

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