Kind 2 User Documentation

Version 2.3.0

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1 Kind 2

Kind 2 is a multi-engine, parallel, SMT-based automatic model checker for safety properties of Lustre programs.

Kind 2 is a command-line tool. It takes as input a Lustre file annotated with properties to be proven invariant (see Kind 2 Input), and outputs which of the properties are true for all inputs, as well as an input sequence for those properties that are falsified. To ease processing by external tools, Kind 2 can output its results in JSON and XML formats (see JSON / XML Output).

By default Kind 2 runs a process for bounded model checking (BMC), two processes for k-induction (one for a fixed value of k=2, and other for increasing values of k), several processes for invariant generation, a process for IC3QE, and several processes for IC3IA in parallel on all properties simultaneously. It incrementally outputs counterexamples to properties as well as properties proved invariant.

The following command-line options control its operation (run `kind2 --help` for a full list). See Techniques for configuration examples and more details on each technique.

`--enable {BMC|IND|IND2|IC3QE|IC3IA|INVGEN|INVGENOS|...}` Select model checking engines

By default, all five model checking engines are run in parallel. Give any combination of `--enable BMC`, `--enable IND`, `--enable IND2`, `--enable IC3QE` and `--enable IC3IA` to select which engines to run. The option `--enable BMC` alone will not be able to prove properties valid, choosing `--enable IND` and `--enable IND2` only (or either of the two alone) will not produce any results. Any other combination is sound (properties claimed to be invariant are indeed invariant) and counterexample-complete (a counterexample will be produced for each property that is not invariant, given enough time and resources).

`--timeout <int>` (default `0` = none) – Run for the given number of seconds of wall clock time

`--smt_solver {Bitwuzla|cvc5|MathSAT|OpenSMT|SMTInterpol|Yices|Yices2|Z3}` (default `Z3`) – Select SMT solver

`--bitwuzla_bin <file>` – Executable for Bitwuzla

`--cvc5_bin <file>` – Executable for cvc5

`--mathsat_bin <file>` – Executable for MathSAT 5

`--opensmt_bin <file>` – Executable for OpenSMT

`--smtinterpol_jar <file>` – JAR of SMTInterpol

`--yices_bin <file>` – Executable for Yices 1 (native input)

`--yices2_bin <file>` – Executable for Yices 2 (SMT input)

`--z3_bin <file>` – Executable for Z3

`-v` Output informational messages

`-json` Output in JSON format

`-xml` Output in XML format

1.1 Try Kind 2 Online

Visit our web interface to try Kind 2 from your browser.

1.2 Download

If you use a Linux or a macOS computer, you can download an executable of the latest version of Kind 2 from here. First make sure though that you have the required software described next.

1.3 Required Software

To run Kind 2 the following software must be installed on your computer:

- Linux or macOS, and
- a supported SMT solver
  - Bitwuzla (for inputs with only machine integers),
  - cvc5,
  - MathSAT 5,
  - OpenSMT (v2.8.0),
  - SMTInterpol,
  - Yices 2,
  - Yices 1, or
  - Z3

Z3 is the presently recommended SMT solver and the default option. For best results, we recommend using a combination of several solvers. For systems with integer and real variables, we recommend using Z3 as the main solver (`--smt_solver Z3`) and MathSAT as the interpolating solver (`--smt_itp_solver MathSAT`). For systems with only machine integers, we recommend using Bitwuzla as the main solver (`--smt_solver Bitwuzla`), MathSAT as the interpolating solver (`--smt_itp_solver MathSAT`), and Z3 for performing quantifier elimination (`--smt_qe_solver Z3`).

1.4 VS Code Extension

You can also install our extension for Visual Studio Code which provides support for Kind 2. The extension contains Linux and macOS binaries for Kind 2 and Z3 ready to use. Windows is also supported through WSL2 (see here for more details).

1.5 Docker

Kind 2 is also available on Docker Hub.

1.5.1 Retrieving / updating the image

Install docker and then run

```
docker pull kind2/kind2:dev
```

Docker will retrieve the layers corresponding to the latest version of the Kind 2 repository, `develop` version. If you are interested in the latest release, run

```
docker pull kind2/kind2
```

instead.

If you want to update your Kind 2 image to latest one, simply re-run the `docker pull` command.

1.5.2 Running Kind 2 through docker

To run Kind 2 on a file on your system, it is recommended to mount the folder in which this file is as a volume. In practice, run

```
docker run -v <absolute_path_to_folder>:/lus kind2/kind2:dev <options> /lus/<your_
↪file>
```

where

- `<absolute_path_to_folder>` is the absolute path to the folder your file is in,
- `<your_file>` is the lustre file you want to run Kind 2 on, and
- `<options>` are some Kind 2 options of your choice.

N.B.

- the fact that the path to your folder must be absolute is a docker constraint;
- mount point `/lus` is arbitrary and does not matter as long as it is consistent with the last argument `/lus/<your_file>`. To avoid name clashes with folders already present in the container however, it is recommended to use `/lus`;

- replace `kind2:dev` by `kind2` if you want to run the latest release of Kind2 instead of the `develop` version;
- `docker run` does **not** update your local Kind 2 image to the latest one: the appropriate `docker pull` command does.

1.5.3 Packaging your local version of Kind 2

In the `docker` directory at the top level of the Kind 2 repository, there is a `Dockerfile` you can use to build your own Kind 2 image. To do so, just run

```
docker build -t kind2-local -f ./docker/Dockerfile .
```

at the root of the repository. `kind2-local` is given here as an example, feel free to call it whatever you want.

Note that building your own local Kind 2 image **does require access to the Internet**. This is because of the packages the build process needs to retrieve, as well as for downloading the z3 and cvc5 solvers.

1.6 Building and installing

If you prefer, you can build Kind 2 directly from sources, either through the OPAM package manager (recommended) or directly using dune.

1.6.1 Using OPAM

Start by installing OPAM 2.x following the instructions on the website, and make sure OPAM has been initialized by running `opam init`. If you want to build the development version of Kind 2 that includes the most recent changes, as opposed to the latest release, then run

```
opam pin add -n kind2 https://github.com/kind2-mc/kind2.git
```

(You can always undo this change later using this command `opam unpin kind2`).

Otherwise, skip the step above and either run

```
opam install --update-invariant kind2
```

if you have OPAM 2.1 or later installed on your system, or run

```
opam depext kind2
opam install --unlock-base kind2
```

if you have an older version of OPAM (you can run `opam --version` to check the version).

This guides the installation of the ZeroMQ C library and any other required external dependencies using the default package manager for your OS (may ask sudo permission). It also builds and installs a compatible version of the OCaml compiler and libraries, and the `kind2` binary. Now you can start using `kind2`.

Other options using OPAM

By default, `kind2` will be installed into the bin directory of your current OPAM switch. Run

```
opam install kind2 --destdir=<DIR>
```

to install the Kind 2 binary into `<DIR>/bin`. This will also create directories `<DIR>/doc` and `<DIR>/lib`.

In alternative, you can clone https://github.com/kind2-mc/kind2.git, move to its top-level directory, and run

```
make install
```

to have OPAM install `kind2` and its dependencies.

Note that z3 is available in OPAM so it is possible to install it too with OPAM by running:

```
opam install z3
```

Be aware, however, that this takes quite a bit of time (up to 25 minutes).

1.6.2 Direct Installation Using Dune

To build directly from sources you will also need the following software first:

- OCaml 4.14 or later,
- Dune 2.7 or later,
- dune-build-info,
- OCaml bindings for ZMQ,
- Yojson,
- num,
- Menhir parser generator

First install this software on your system using your preferred method. Then clone the Kind 2 git repository, move to the top-level directory of the repository, and run

```
dune build src @install
dune install --sections=bin --prefix <DIR>
```

to install the Kind 2 binary into `<DIR>/bin`.

You need a supported SMT solver in your PATH environment variable when running `kind2`.

1.7 Development

With OPAM 2.x you can create a local switch which will install all dependencies automatically.

```
opam switch create .
make
```

Alternatively, you can install all dependencies in your current switch by running:

```
opam install . --deps-only
make
```

For running the unit tests for front end, you can install ounit2 library using opam by running:

```
opam install ounit2
```

To run the ounit tests, you can use the following dune command:

```
dune test
```

To run regression tests, you need a Python interpreter and the pytest module. The simplest way to do this is to install uv. The test-running script will try to use `uv` to set up its own isolated python environment with `pytest`, so the rest of your system will not be impacted. If it fails to find `uv`, it will fallback to trying to use `pytest` in your system's Python interpreter.

```
make test
```

1.8 Documentation

Documentation is available online in HTML or PDF forms.

In order to generate the documentation locally, you need:

- A GNU version of `sed` (`gsed` on OSX)
- Python v3.5 or later
- Sphinx

For HTML documentation, you additionally need:

- sphinx-press-theme

For PDF documentation, you additionally need:

- latexmk

- [XeTeX](#)
- [lmodern](#)

If you're on Debian/Ubuntu, assuming you have Python 3 installed, you can run the following:

```
sudo apt-get install python3-sphinx latexmk texlive-xetex lmodern
pip3 install sphinx_press_theme
```

See `doc/usr/README.rst` for more information.

2   Techniques

This section presents the techniques available in Kind 2: how they work, and how they can be tweaked through various options:

- k-Induction
- Invariant Generation
- IC3

2.1 Compositional reasoning

When verifying a node `n`, compositional reasoning consists in abstracting the complexity of the subnodes of `n` by their contracts (see Contract Semantics). The idea is that the contract has typically a lot less state than the node it specifies, which in addition to its own state contains that of its subnodes recursively.

Compositional reasoning thus improves the scalability of Kind 2 by taking advantage of information provided by the user to abstract the complexity away. When in compositional mode (`--compositional true`), Kind 2 will abstract all calls (to subnodes that have a contract with at least one guarantee or one mode) in the top node and verify the resulting, abstract system.

A successful compositional proof of a node does not guarantee the correctness of the concrete (un-abstracted) node though, since the subnodes have not been verified. For this reason compositional reasoning is usually applied in conjunction with modular reasoning, discussed in the next section.

2.2 Modular reasoning

Modular reasoning is activated with the option `--modular true`. In this mode, Kind 2 will perform whatever type of analysis is specified by the other flags on **every node** of the hierarchy, bottom-up. The analysis is completed on every node even if some node is proved unsafe because of the falsification of one of its properties.

A timeout for each analysis can be specified using the `--timeout_analysis` flag. It can be used in conjunction with the global timeout given with the `--timeout` or `--timeout_wall` time.

Internally Kind 2 builds on previous analyses when starting a new one. For instance, by using the invariants previously discovered in subnodes of the node under analysis.

2.3 Refinement in compositional and modular analyses

An interesting configuration is

```
kind2 --modular true --compositional true ...
```

If `top` calls `sub` and we analyze `top`, it means we have previously analyzed `sub`. We are running in compositional mode so the call to `sub` is originally abstracted by its contract. Say the analysis fails with a counterexample. The counterexample might be spurious for the concrete version of `sub`: the failure would not happen if we used the concrete call to `sub` instead of the abstract one.

Say now that when we analyzed `sub`, we proved that it is correct. In this case Kind 2 will attempt to refine the call to `sub` in top. That is, undo the abstraction and use the implementation of `sub` in a new analysis.

Note that since `sub` is known to be correct, it is stronger than its contract. More precisely, it accepts fewer execution traces than its contract does. Hence anything proved with the abstraction of `sub` is still valid after refinement, and Kind 2 will use these results right away.

2.4 Modifiers to control node/function abstraction

To prevent Kind 2 from abstracting a specific node or function that has both a body and a contract during compositional analysis, use the `transparent` modifier before the `node` or `function` keywords:

```
transparent function F(...) returns (...)
```

To prevent Kind 2 from refining a specific node or function that has both a body and a contract during compositional and modular analyses, use the `opaque` modifier before the `node` or `function` keywords:

```
opaque node N(...) returns (...)
```

3 k-Induction

k-Induction is a well-known technique for the verification of transition systems. A k-induction engine is composed of two parts: base and step. Base performs bounded model checking on the properties, i.e. checks the **base case**. Step checks whether it is possible to reach a violation of one of the properties from a trace of states satisfying them: the **inductive step**.

In Kind 2 base and step run in parallel, and can be enabled separately. Running step alone with

```
kind2 --enable IND <file>
```

will not yield anything interesting, as step cannot falsify properties nor prove anything without base. To run the actual k-induction engine, you must enable base (`BMC`) and step (`IND`):

```
kind2 --enable BMC --enable IND <file>
```

3.1 Options

k-Induction can be tweaked with the following options.

`--bmc_max <int>` (default `0`) – sets an upper bound on the number of unrolling base and step will perform. `0` is for unlimited.

`--ind_compress <bool>` (default `false`) – activates path compression in step, **i.e.** counterexamples with a loop will be dismissed. You can activate several path compression strategies:

- `--ind_compress_equal <bool>` (default `true`) – compresses states if they are equal modulo inputs
- `--ind_compress_same_succ <bool>` (default `false`) – compresses states if they have the same successors (experimental)
- `--ind_compress_same_pred <bool>` (default `false`) – compresses states if they have the same predecessors (experimental)

`--ind_lazy_invariants <bool>` (default `false`) – deactivates eager use of invariants in step. Instead, when a step counterexample is found each invariant is evaluated on the model until one blocks it. The invariant is then asserted to block the counterexample, and step starts a new check-sat.

4   Invariant Generation

The invariant generation technique currently implemented in Kind 2 is an improved version of [the one implemented in PKind](). It works by instantiating templates on a set of terms provided by a syntactic analysis of the system.

The main improvement is that in Kind 2, invariant generation is modular. That is to say it can attempt to discover invariants for subnodes of the top node. The idea is that looking at small components and discovering invariants for them provides results faster than analyzing the system monolithically. To disable the modular behavior of invariant generation, use the option `--invgen_top_only true`.

There are two invariant generation techniques: one state (OS) and two state (TS). The former will only look for invariants between the state variables in the current state, while the latter tries to relate the current state with the previous state. The two are separated because as the system grows in size, two state invariant generation can become very expensive.

The one state and two state variants can be activated with `--enable INVGENOS` and `--enable INVGEN` respectively.

Note that, in theory, two state invariant generation is strictly more powerful than the one state version, albeit slower, since two state can also discover one state invariants. When both variants are running, Kind 2 optimizes two state invariant generation by forcing it to look only for two state invariants.

The bottom line is that running i) only two state invariant generation or ii) one state and two states will discover the same invariants. In the case of i) the same techniques seeks both one state and two state invariants at the same time, which is slower than ii) where one state and two state invariants are sought by different processes running in parallel.

4.1   Options

Invariant generation can be tweaked using the following options. Note that this will affect both the one state and two state process if both are running.

`--invgen_prune_trivial <bool>` (default `true`) – when invariants are discovered, do not communicate one-state invariants implied by previous one-state invariants, and two-state invariants implied by previous two-state invariants or the transition relation.

`--invgen_max_succ <int>` (default 1) – the number of unrolling to perform on subsystems before moving on to the next one in the hierarchy.

`--invgen_lift_candidates <bool>` (default `false`) – if true, then candidate terms generated for subsystems will be lifted to their callers. **Warning** this might choke invariant generation with a huge number of candidates for large enough systems.

`--invgen_mine_trans <bool>` (default `false`) – if true, the transition relation will be mined for candidate terms. Can make the set of candidate terms untractable.

`--invgen_renice <int>` (only positive values) – the bigger the parameter, the lower the priority of invariant generation will be for the operating system.

4.2 Lock Step K-induction

Another improvement on the PKind invariant generation is the way the search for a k-induction proof of the candidate invariants is performed. In PKind, a bounded model checking engine is run up to a certain depth `d` and discovers falsifiable candidate invariants. The graph used to produce the potential invariants is refined based on this information. Once the bound on the depth is reached, an inductive step instance looks for actual invariants by unrolling up to `d`.

In Kind 2, base and step are performed in lock step. Once the candidate invariant graph has been updated by base for some depth, step runs at the same depth and broadcasts the invariants it discovers to the whole framework. It is thus possible to generate invariants earlier and thus speed up the whole analysis.

5 IC3

Kind 2 supports two SMT-based extensions of the SAT-based verification technique IC3. The challenge when lifting IC3 to infinite state systems is the computation of pre-images of the system's transition relation. The first extension, IC3QE, uses quantifier elimination to compute the pre-image. If the input problem is in linear integer arithmetic, Kind 2 uses a built-in method that performs a fast approximate quantifier elimination. Otherwise, the quantifier elimination is delegated to an SMT solver, which is at this time possible with Z3 and cvc5.

The second extension, IC3IA, implements a version of IC3 that relies on implicit (predicate) abstraction by Cimatti et al. The main idea of the method is to work on an abstraction of the state space induced by a set of predicates so that the computation of pre-images of the system's transition relation does not require the use of quantifier elimination. As with most abstraction methods, this introduces the problem of having to handle spurious abstract counterexamples for the property to be proven, that is, traces that falsify the property in the abstracted system but are not actual executions of the original system. The method addresses this problem by using an abstraction refinement technique based on logical interpolants. Kind 2 currently supports three proof-based interpolating SMT solvers for the generation of interpolants: MathSAT, SMTInterpol, and OpenSMT. In addition, Kind 2 also implements a built-in method for producing interpolants based on quantifier elimination that can be used with Z3 and cvc5. When the IC3IA engine is enabled, each property is handled separately by a different process; two when the built-in method for producing interpolants is used, one generating backward interpolants and another one generating forward interpolants.

To enable nothing but the IC3 engines (IC3QE and IC3IA), run

```
kind2 --enable IC3 <file>
```

If you only want to enable of the engines, e.g. IC3QE, run

```
kind2 --enable IC3QE <file>
```

5.1 IC3-IA Options

`--smt_itp_solver {MathSAT | SMTInterpol | Z3qe | cvc5qe | OpenSMT}` – set the SMT solver used for interpolation.

`--ic3ia_max <int>` – set the maximum number of IC3IA parallel processes. Each process checks an individual property.

5.2 IC3-QE Options

--qe_method {precise|impl|cooper} (default cooper) – select the quantifier elimination strategy: cooper for the built-in approximate method, precise or impl to delegate to the SMT solver. The precise strategy computes the exact pre-image, which is an expensive operation. The impl strategy under-approximates the result by computing a conjunctive implicant first. If the problem is not in linear integer arithmetic, cooper falls back to impl.

--smt_qe_solver {Z3 | cvc5} (default detect) – set the SMT solver used for quantifier elimination

To see other advanced options run --help_of ic3qe.

6 Kind 2 Input

Kind 2 reads input models written in an extension of the dataflow Lustre language (see this primer for a quick introduction to the Lustre language). Kind 2 supports most of the Lustre V4 syntax and some elements of Lustre V6. See the file examples/syntax-test.lus for examples of all supported language constructs.

6.1 Properties and top-level node

To specify an invariant property to verify in a Lustre node, add the following annotation in the body (i.e. between keywords `let` and `tel`) of the node:

```
--%PROPERTY ["<name>"] <bool_expr> ;
```

or, use a `check` statement:

```
check ["<name>"] <bool_expr> ;
```

where `<name>` is an identifier for the property and `<bool_expr>` is a Boolean Lustre expression.

In addition to invariant properties, Kind 2 also accepts dedicated syntax for checking the existence of a witness. You can specify reachability properties of the form:

```
--%PROPERTY reachable ["<name>"] <bool_expr> [from <int>] [within <int>];
```

or, using a `check` statement:

```
check reachable ["<name>"] <bool_expr> [from <int>] [within <int>];
```

where the clauses between square brackets are optional. The optional clauses allow you to specify, exclusively or at the same time, a lower and upper bound on the number of execution steps in the witness trace. Concretely, `check reachable P from m` asks whether a state satisfying P is reachable in `m` steps or more while `check reachable P within n` asks whether a state satisfying P is reachable in `n` steps or less. Moreover, Kind 2 also supports the following syntax for the specification of properties where the lower and upper bounds are the same:

```
check reachable ["<name>"] <bool_expr> at <int>;
```

Without modular reasoning active, Kind 2 only analyzes the properties of what it calls the top nodes. By default, any node that is not depended on by another node (i.e. called by that node) is a top node. Alternatively, nodes can be marked as main nodes by doing the following:

```
--%MAIN ;
```

to the body of that node.

You can also specify the main node in the command line arguments, with

```
kind2 --lus_main <node_name> ...
```

Main nodes specified by the command line option override main nodes annotated in the source code. If any main nodes exist then only main nodes are analyzed (top nodes are not).

6.1.1 Examples

The following example declares two nodes `greycounter` and `intcounter`, as well as an observer node `top` that calls these nodes and verifies that their outputs are the same. The node `top` is annotated with `--%MAIN` ; which makes it a main node. The line `--%PROPERTY OK;` means we want to verify that the Boolean stream `OK` is always true.

```
node greycounter (reset: bool) returns (out: bool);
var a, b: bool;
let
  a = false -> (not reset and not pre b);
  b = false -> (not reset and pre a);
  out = a and b;

tel

node intcounter (reset: bool; const max: int) returns (out: bool);
var t: int;
let
  t = 0 -> if reset or pre t = max then 0 else pre t + 1;
  out = t = 2;

tel

node top (reset: bool) returns (OK: bool);
var b, d: bool;
let
  b = greycounter(reset);
  d = intcounter(reset, 3);
  OK = b = d;

  --%MAIN ;

  --%PROPERTY OK;

tel
```

Kind 2 produces the following on standard output when run with the default options (`kind2`

`<file_name.lus>`):

```
kind2 v1.5.1


================================================================
Analyzing top
  with First top: 'top'
            subsystems
                | concrete: intcounter, greycounter


<Success> Property OK is valid by inductive step after 0.065s.


----------------------------------------------------------------
Summary of properties:
----------------------------------------------------------------
OK: valid (k=5)
================================================================
```

We can see here that the property `OK` has been proven valid for the system (by k-induction).

The second example demonstrates reachability properties using a single `counter` node:

```
node counter () returns (out: int);
let
   out = 0 -> pre out + 1;

   check reachable out = 10;
   check reachable out = 100 from 99;
   check reachable out = 50 at 50;
   check reachable out = 15 from 10 within 20;

   check reachable out = 10 within 5;
tel
```

Kind 2 produces output reporting that the first four expressions are reachable, while the last is not. If you want to print a witness in the standard output for each proven reachability property, pass `--print_witness true` to Kind 2. To dump the witness to a file instead, pass `--dump_witness true` to Kind 2.

6.1.2 Conditional Properties

Invariant properties of a node are often case-based, with each case describing what the component should do depending on a specific situation. These properties are usually encoded in conditional properties of the form `situation => behavior`, and are often better represented in terms of the mode logic of a node (see subsection Modes in Contract Semantics). However, these properties do not always imply modal behavior, or they are not defined in terms of the interface of a node. For those cases, Kind 2 allows the user to specify a conditional invariant property of the form `B => A` as follows:

```
check A provided B;
```

This dedicated syntax makes writing properties more straightforward and user-friendly, but also allows Kind 2 to trigger additional checks. A challenge for the user with these kinds of properties arises if the guard `B` may always be false, for example due to a modeling error. The user may believe that the property is interesting and true, whereas the property is vacuously true.

When the dedicated syntax above is used, Kind 2 simultaneously checks that `B => A` is invariant and `B` is reachable. If `B => A` is in fact invariant, the reachability check lets you know whether the implication is trivially true or not. Notice that when running Kind 2 in modular mode, the reachability check is performed locally to a node without taking call contexts into account; only the specified assumptions are considered. You can disable this check by passing `--check_nonvacuity false` to Kind 2, or by suppressing all reachability checks (`--check_reach false`).

6.2 Contracts

A contract `(A,G,M)`for a node is a set of assumptions `A`, a set of guarantees `G`, and a set of modes `M`. The semantics of contracts is given in the Contract Semantics section, here we focus on the input format for contracts. Contracts are specified either locally, using the inline syntax, or externally in a contract node. Both the local and external syntax have a body composed of items, each of which define

- a ghost variable / constant,
- an assumption,
- a guarantee,
- a mode, or
- an import of a contract node.

They are presented in detail below, after the discussion on local and external syntaxes.

6.2.1 Inline syntax

A local contract is a block between the signature of the node

```
node <id> (...) returns (...) ;
```

and its body. That is, between the ; of the node signature and the `let` opening its body.

A local contract block is denoted by the keywords con and noc:

```
con
  [item]+
noc
```

The original contract syntax (which is deprecated but still available) is a special block comment of the form

```
(*@contract
  [item]+
*)
```

or

```
/*@contract
  [item]+
*/
```

6.2.2 External syntax

A contract node is very similar to a traditional lustre node. The two differences are that

- it starts with `contract` instead of `node`, and
- its body can only mention contract items.

A contract node thus has form

```
contract <id> (<in_params>) returns (<out_params>) ;
let
  [item]+
tel
```

To use a contract node one needs to import it through an inline contract. See the next section for more details.

6.2.3 Contract items and restrictions

Ghost variables and constants

A ghost variable (constant) is a stream that is local to the contract. That is, it is not accessible from the body of the node specified. Ghost variables (constants) are defined with the `var` (`const`) keyword. Kind 2 performs type -inference for constants so in most cases type annotations are not necessary.

The general syntax is

```
const <id> [: <type>] = <expr> ;
var   <id>  : <type>  = <expr> ;
```

For instance:

```
const max = 42 ;
var ghost_stream: real = if input > max then max else input ;
```

Assumptions

An assumption over a node `n` is a constraint one must respect in order to use `n` legally. It cannot depend on outputs of `n` in the current state, but referring to outputs under a `pre` is fine.

The idea is that it does not make sense to ask the caller to respect some constraints over the outputs of `n`, as the caller has no control over them other than the inputs it feeds `n` with. The assumption may however depend on previous values of the outputs produced by `n`.

Assumptions are given with the `assume` keyword, followed by any legal Boolean expression:

```
assume <expr> ;
```

Guarantees

Unlike assumptions, guarantees do not have any restrictions on the streams they can depend on. They typically mention the outputs in the current state since they express the behavior of the node they specified under the assumptions of this node.

Guarantees are given with the `guarantee` keyword, followed by any legal Boolean expression:

```
guarantee <expr> ;
```

Modes

A mode (`R,E`) is a set of requires `R` and a set of ensures `E`. Modes are named to ease traceability and improve feedback. The general syntax is

```
mode <id> (
  [require <expr> ;]*
  [ensure  <expr> ;]*
) ;
```

For instance:

```
mode engaging (
  require true -> not pre engage_input ;
  require engage_input ;
  -- No ensure, same as `ensure true ;`.
) ;
mode engaged (
  require engage_input ;
  require false -> pre engage_input ;
  ensure  output <= upper_bound ;
  ensure  lower_bound <= output ;
) ;
```

Imports

A contract import merges the current contract with the one imported. That is, if the current contract is (`A,G,M`) and we import (`A',G',M'`), the resulting contract is (`A U A'`, `G U G'`, `M U M'`) where `U` is set union. However, each contract import introduces its own namespace to avoid name collisions.

When importing a contract, it is necessary to specify how the instantiation of the contract is performed. This defines a mapping from the input (output) formal parameters to the actual ones of the import.

When importing contract `c` in the contract of node `n`, the actual input parameters of the import of `c` cannot depend on outputs of `n` in the current state. The reason is that the distinction between inputs and outputs lets Kind 2 check that the assumptions requirements make sense, i.e. do not depend on outputs of `n` in the current state.

The general syntax is

```
import <id> ( <expr>,* <expr> ) returns ( <id>,* <id> ) ;
```

For instance:

```
contract spec (engage, disengage: bool) returns (engaged: bool) ;
let ... tel

node my_node (
  -- Flags are "signals" here, but `bool`s in the contract.
  engage, disengage: real
) returns (
  engaged: real
) ;
con
  var bool_eng: bool = engage <> 0.0 ;
  var bool_dis: bool = disengage <> 0.0 ;
  var bool_enged: bool = engaged <> 0.0 ;

  var never_triggered: bool = (
    not bool_eng -> not bool_eng and pre never_triggered
  ) ;

  assume not (bool_eng and bool_dis) ;
  guarantee true -> (
    (not engage and not pre bool_eng) => not engaged
  ) ;

  mode init (
    require never_triggered ;
    ensure not bool_enged ;
  ) ;

  import spec (bool_eng, bool_dis) returns (bool_enged) ;
noc
let ... tel
```

Mode references

Once a mode has been defined it is possible to refer to it with

```
::<scope>::<mode_id>
```

where `<mode_id>` is the name of the mode, and `<scope>` is the path to the mode in terms of contract imports.

In the example from the previous section for instance, say contract `spec` has a mode `m`. The inline contract of `my_node` can refer to it by

```
::spec::m
```

To refer to the `init` mode:

```
::init
```

A mode reference is syntactic sugar for the `requires` of the mode in question. So if mode `m` is

```
mode m (
  require <r_1> ;
  require <r_2> ;
  ...
  require <r_n> ; -- Last require.
  ...
) ;
```

then `::<path>::m` is exactly the same as

```
(<r_1> and <r_1> and ... and <r_n>)
```

N.B.: a mode reference

- is a Lustre expression of type `bool` just like any other Boolean expression. It can appear under a `pre`, be used in a node call or a contract import, etc.
- is only legal **outside** the mode item itself. That is, no self-references are allowed. Forward references are allowed.

An interesting use-case for mode references is that of checking properties over the specification itself. One may want to do so to make sure the specification behaves as intended. For instance

```
mode m1 (...) ;
mode m2 (...) ;
mode m3 (...) ;

guarantee true -> ( -- `m3` cannot succeed to `m1`.
  (pre ::m1) => not ::m3
) ;
guarantee true -> ( -- `m1`, `m2` and `m3` are exclusive.
  not (::m1 and ::m2 and ::m3)
) ;
```

6.2.4 Merge, When, Activate and Restart

Note: the first few examples of this section illustrating (unsafe) uses of `when` and `activate` are **not legal** in Kind 2. They aim at introducing the semantics of lustre clocks. As discussed below, they are only legal when used inside a `merge`, hence making them safe clock-wise.

Also, `activate` and `restart` are actually not a legal Lustre v6 operator. They are however legal in Scade 6.

A `merge` is an operator combining several streams defined on **complementary** clocks. There is two ways to define a stream on a clock. First, by wrapping its definition inside a `when`.

```
node example (i: int) returns (out: int) ;
var i_pos: bool ; x: int ;
let
  ...
  i_pos = i >= 0 ;
  x = i when i_pos ;
  ...
tel
```

Here, x is only defined when `in_pos`, its clock, is `true`. That is, a trace of execution of `example` sliced to x could be

step	i	i_pos	x
0	3	true	3
1	-2	false	//
2	-1	false	//
3	7	true	7
4	-42	true	//

where // indicates that x undefined.

The second way to define a stream on a clock is to wrap a node call with the `activate` keyword. The syntax for this is

```
(activate <node_name> every <clock>)(<input_1>, <input_2>, ...)
```

For example, consider the following node:

```
node sum_ge_10 (i: int) returns (out: bool) ;
var sum: int ;
let
  sum = i + (0 -> pre sum) ;
```

```
   out = sum >= 10 ;
tel
```

Say now we call this node as follows:

```
node example (i: int) returns (...) ;
var tmp, i_pos: bool ;
let
  ...
  i_pos = i >= 0 ;
  tmp = (activate sum_ge_10 every i_pos)(i) ;
  ...
tel
```

That is, we want `sum_ge_10(i)` to tick iff `i` is positive. Here is an example trace of `example` sliced to `tmp`; notice how the internal state of `sum_ge_10` (i.e. `pre sum_ge_10.sum`) is maintained so that it does refer to the value of `sum_ge_10.sum` at the last clock tick of the `activate`:

step	i	i_pos	tmp	sum_ge_10.i	pre sum_ge_10.sum	sum_ge_10.sum
0	3	true	false	3	nil	3
1	2	true	false	2	3	5
2	-1	false	nil	nil	5	nil
3	2	true	false	2	5	7
4	-7	false	nil	nil	7	nil
5	35	true	true	35	7	42
6	-2	false	nil	nil	42	nil

Now, as mentioned above the `merge` operator combines two streams defined on **complimentary** clocks. The syntax of `merge` is:

```
merge( <clock> ; <e_1> ; <e_2> )
```

where `e_1` and `e_2` are streams defined on `<clock>` and `not <clock>` respectively, or on `not <clock>` and `<clock>` respectively.

Building on the previous example, say add two new streams `pre_tmp` and `safe_tmp`:

```
node example (i: int) returns (...) ;
var tmp, i_pos, pre_tmp, safe_tmp: bool ;
let
  ...
  i_pos = i >= 0 ;
  tmp = (activate sum_ge_10 every i_pos)(i) ;
  pre_tmp = false -> pre safe_tmp  ;
```

```
  safe_tmp = merge( i_pos ; tmp ; pre_tmp when not i_pos ) ;
  ...
tel
```

That is, `safe_tmp` is the value of `tmp` whenever it is defined, otherwise it is the previous value of `safe_tmp` if any, and `false` otherwise. The execution trace given above becomes

step	i	i_pos	tmp	pre_tmp	safe_tmp
0	3	true	false	false	false
1	2	true	false	false	false
2	-1	false	nil	false	false
3	2	true	false	false	false
4	-7	false	nil	false	false
5	35	true	true	false	true
6	-2	false	nil	true	true

Just like with uninitialized `pre`s, if not careful one can easily end up manipulating undefined streams. Kind 2 forces good practice by allowing `when` and `activate ... every` expressions only inside a `merge`. All the examples of this section above this point are thus invalid from Kind 2's point of view.

Rewriting them as valid Kind 2 input is not difficult however. Here is a legal version of the last example:

```
node example (i: int) returns (...) ;
var i_pos, pre_tmp, safe_tmp: bool ;
let
  ...
  i_pos = i >= 0 ;
  pre_tmp = false -> pre safe_tmp  ;
  safe_tmp = merge(
    i_pos ;
    (activate sum_ge_10 every i_pos)(i) ;
    pre_tmp when not i_pos
  ) ;
  ...
tel
```

Kind 2 supports resetting the internal state of a node to its initial state by using the construct restart/every. Writing

```
(restart n every c)(x1, ..., xn)
```

makes a call to the node `n` with arguments `x1`, …, `xn` and every time the Boolean stream `c` is

true, the internal state of the node is reset to its initial value.

In the example below, the node `top` makes a call to `counter` (which is an integer counter modulo a constant `max`) which is reset every time the input stream `reset` is true.

```
node counter (const max: int) returns (t: int);
let
  t = 0 -> if pre t = max then 0 else pre t + 1;
tel


node top (reset: bool) returns (c: int);
let
  c = (restart counter every reset)(3);
tel
```

A trace of execution for the node top could be:

step	reset	c
0	false	0
1	false	1
2	false	2
3	false	3
4	true	0
5	false	1
6	false	2
7	true	0
8	true	0
9	false	1

> **Note:** This construction can be encoded in traditional Lustre by having a Boolean input for the reset stream for each node. However providing a built-in way to do it facilitates the modeling of complex control systems.

Restart and activate can also be combined in the following way:

```
(activate (restart n every r) every c)(a1, ..., an)
(activate n every c restart every r)(a1, ..., an)
```

These two calls are the same (the second one is just syntactic sugar). The (instance of the) node `n` is restarted whenever `r` is true and the resulting call is activated when the clock `c` is true. Notice that the restart clock `r` is also sampled by `c` in this call.

6.3 Partially defined nodes

Kind 2 allows nodes to define their outputs only partially. For instance, the node

```
node count (trigger: bool) returns (count: int ; error: bool) ;
con
  var once: bool = trigger or (false -> pre once) ;
  guarantee count >= 0 ;
  mode still_zero (
    require not once ;
    ensure count = 0 ;
  ) ;
  mode gt (
    require not ::still_zero ;
    ensure count > 0 ;
  ) ;
noc
let
  count = (if trigger then 1 else 0) + (0 -> pre count) ;
tel
```

can be analyzed: first for mode exhaustiveness, and the body is checked against its contract, although it is only partially defined. Here, both will succeed.

6.4 The `imported` keyword

Nodes (and functions, see below) can be declared `imported`. This means that the node does not have a body (`let ... tel`). In a Lustre compiler, this is usually used to encode a C function or more generally a call to an external library.

```
node imported no_body (inputs: ...) returns (outputs: ...) ;
```

In Kind 2, this means that the node is always abstract in the contract sense. It can never be refined, and is always abstracted by its contract. If none is given, then the implicit (rather weak) contract

```
con
  assume true ;
  guarantee true ;
noc
```

is used.

In a modular analysis, `imported` nodes will not be analyzed, although if their contract has modes they will be checked for exhaustiveness, consistently with the usual Kind 2 contract

workflow. Every output of an imported node is assumed to depend on every input. This may lead Kind 2 to detect circular dependencies that do not exist in an _actual_ system, resulting in the rejection of an input model. To make Kind 2 accept such model, the imported node must be refined by decomposing it into smaller subnodes and specifying the actual dependencies among inputs and outputs.

6.4.1 Partially defined nodes **VS** `imported`

Kind 2 allows partially defined nodes, that is nodes in which some streams do not have a definition. At first glance, it might seem like a node with no definitions at all (with an empty body) is the same as an `imported` node.

It is not the case. A partially defined node still has a (potentially empty) body which can be analyzed. The fact that it is not completely defined does not change this fact. If a partially defined node is at the top level, or is in the cone of influence of the top node in a modular analysis, then it's body **will** be analyzed.

An `imported` node on the other hand explicitly does not have a body. Its non-existent body will thus never be analyzed.

6.5 Functions

Kind 2 supports the `function` keyword which is used just like the `node` one but has slightly different semantics. Like the name suggests, the output(s) of a `function` must be a non-temporal combination of its inputs. That is, a function cannot depend on the `->`, `pre`, `merge`, `when`, `condact`, or `activate` operators. A function is also not allowed to call a node, only other functions. In Lustre terms, functions are stateless.

In Kind 2, these restrictions also apply to the contract attached to a function, if any. Moreover, Kind 2 enforces that partially defined functions, imported functions, and functions abstracted by their contracts behave as mathematical functions. That is, given the same inputs, the functions always produce the same outputs.

6.5.1 Benefits and limitations

Functions are interesting in the model-checking context of Kind 2 mainly as a mean to make an abstraction more precise. A realistic use-case is when one wants to abstract non-linear expressions. While the simple expression `x*y` seems harmless, at SMT-level it means bringing in the theory of non-linear arithmetic.

Non-linear arithmetic has a huge impact not only on the performances of the underlying SMT solvers, but also on the SMT-level features Kind 2 can use (not to mention undecidability). Typically, non-lineary arithmetic tends to prevent Kind 2 from performing satisfiability checks with assumptions, a feature it heavily relies on.

The bottom line is that as soon as some non-linear expression appear, Kind 2 will most likely fail to analyze most non-trivial systems because the underlying solver will simply give up.

Hence, it is usually extremely rewarding to abstract non-linear expressions away in a separate function equipped with a contract. The contract would be a linear abstraction of the non-linear expression that is precise enough to prove the system using correct. That way, a compositional analysis would i) verify the abstraction is correct and ii) analyze the rest of the system using this abstraction, thus making the analysis a linear one.

Using a function instead of a node simply results in a better abstraction. Kind 2 will encode, at SMT-level, that the outputs of this component depend on the current version of its inputs only, not on its previous values.

The downside of using functions in your model is that the IC3QE engine and the IC3IA engine with the Z3qe or cvc5qe options must shut down, since their current implementation cannot reason about the resulting system.

6.6 If statements and frame conditions

Within node definitions, Kind 2 has support for two features that allow the programmer to use a more imperative style– (1) `if` statements and (2) frame conditions.

6.6.1 If statements

Kind 2 has always supported conditional expressions of the form `x = if condition then expr1 else expr2`, where the `if/then/else` expression either evaluates to `expression1` or `expression2`, depending on the value of `condition`. However, in some circumstances, it may be more natural to use `if` statements that serve as control flow (rather than evaluate to a value). For example, Kind 2 now supports statements of the form:

```
if condition1 then
   y1 = expr1;
   y2 = expr2;
elsif condition2 then
   y1 = expr3;
   y2 = expr4;
else
   y1 = expr5;
   y2 = expr6;
fi
```

In the above block, if `condition1` is true, then `y1` and `y2` will be set to `expr1` and `expr2`, respectively. Otherwise, `y1` and `y2` will be set to either `expr3` and `expr4` or `expr5` and `expr6`, depending on the value of `condition2`. The `if` statement is closed with the `fi` token. As with

other mainstream programming languages, Kind 2 allows for arbitrary nesting of `if` statements, as well as writing `if` statements that do not have any `else` or `elsif` blocks.

Note: If statements are syntactic sugar for conditional expressions. The `if` statement above is equivalent to:

```
y1 = if condition1 then expr1 else (if condition2 then expr3 else expr5);
y2 = if condition1 then expr2 else (if condition2 then expr4 else expr6);
```

6.6.2 Frame conditions

Kind 2 also has support for code blocks with frame conditions. At the beginning of the block (denoted by the `frame` keyword), the user specifies a list of variables that they wish to define within the frame block. All variables defined within the frame block must be present in this list. Then, initial values are optionally specified for these variables. Variables are defined within the frame block body (denoted by the `let` and `tel` keywords). It is possible to leave variables (partially or fully) undefined. A variable is considered fully undefined if it is declared in the list of frame block variables, but there is no definition given in the frame block body. A variable is considered partially defined if it is defined within an `if` block, but a definition is not supplied in all cases (e.g., `if c then y = x; fi` defines y within the `then` case but not the `else` case).

If a variable is fully undefined, then it is set to its initialization value (if one exists) in the first timestep, and it stutters (is set equal to its value on the previous timestep) on other timesteps. If a variable is partially undefined, then the same assignment is performed, but only for branches of the `if` block where the variable is left undefined.

The following example involves three variables `y1`, `y2`, and `y3`. Since `y1` is left fully undefined within the frame block body, it will always be equal to 0 (its initialization value). `y2` will have value `0, 1, 2, 3, ...` since it is not fully or partially undefined (notice that the initialization value is not used in this case). Finally, `y3` will have value `//, 0, 1, 2, 3, ...` since it is also not fully or partially undefined, regardless of the presence of an unguarded `pre`.

```
node example() returns (y1, y2, y3: int);
let
   frame ( y1, y2, y3 )
   (* Initializations *)
   y1 = 0; y2 = 100; y3 = 5;

   (* Body *)
   let
      y2 = counter();
      y3 = pre counter();
   tel
tel
```

```
node counter() returns (y: int);
let
    y = 0 -> pre y + 1;
tel
```

Frame conditions are especially useful when combined with the `if` statements described in the previous subsection, as variables can be left undefined in some branches of the `if` statement.

```
node example() returns (y1, y2: int);
let
    frame ( y1, y2 )
    (* Initializations *)
    y1 = 10;
    y2 = 100;

    (* Body *)
    let
        if (counter() < 10)
        then
            y1 = counter();
        else
            y2 = counter() * 2;
        fi
    tel
tel



node counter() returns (y: int);
let
    y = 0 -> pre y + 1;
tel
```

In the above example, `y1` is left undefined in the `else` branch of the `if` statement, and `y2` is left undefined in the `then` branch. Since the condition `counter() < 10` holds in the initial timestep, `y1` will be initialized to `0` according to its definition in the `then` branch. Then, `y1` will continue to be equal to `counter()` on the second through tenth timesteps, and then stutter (staying at 9) for the remaining timesteps.

On the other hand, `y2` starts at its supplied initialization value at the top of the frame block (100) since it is left undefined in the `then` branch of the `if` block. It stutters there for the first 10 timesteps, and then is set to `counter() * 2` for the remaining timesteps.

Note that variables do not have to have initializations. When no initialization is given, a variable's initial value is equal to the initial value of the expression defined in the frame block body. If the corresponding expression is undefined in the first timestep, or if there is no equation

defining the variable in the first timestep, then the variable is undefined in the first timestep. For example, the following code is supported because even though `y1`, `y2`, and `y3` do not have an initializations, they are present in the list of variables `frame ( y1, y2, y3 )`. The initial value of `y1` is 0 (the initial value assigned by `counter()`); the initial value of `y2` is undefined (due to the unguarded `pre`); and the initial value of `y3` is also undefined (due to the lack of an equation defining `y3` initially).

```
frame ( y1, y2, y3 )
let
   y1 = counter();
   y2 = pre counter();
tel


node counter() returns (y: int);
let
   y = 0 -> pre y + 1;
tel
```

Also, it is still possible to assign to multiple variables at once (equations of the form `y1, y2 = (expr1, expr2);`) in either the initializations or the frame block body.

The frame block semantics may introduce unguarded `pre` expressions. For example, the definition of `y` in the following code block is equivalent to `y = pre y`. So, Kind 2 will produce two warning messages. The first will state that `y` is uninitialized in the frame block, and the second will state that there is an unguarded `pre` (due to this lack of initialization).

```
frame ( y )
let
tel
```

Similarly, in the following code block, the definitions of `y1` and `y2` are equivalent to `y1 = if cond then 0 else pre y1` and `y2 = if cond then pre y2 else 1`, respectively. This situation (and any other situation where the frame block semantics result in the generation of an unguarded `pre`) will also generate the two warnings as discussed in the previous paragraph.

```
frame (y1, y2)
let
   if cond
   then
      y1 = 0;
   else
      y2 = 1;
   fi
tel
```

6.6.3 Restrictions

A frame block cannot be nested within an if statement or another frame block, as demonstrated in the following examples:

```
if condition
then
   frame ( y1, y2 )
   y1 = init1; y2 = init2;
   let
       y1 = 10;
   tel
fi
```

```
frame ( y1, y2 )
y1 = init1; y2 = init2;
let
   y1 = expr1;
   frame ( y2 )
   y2 = init3;
   let
       y2 = expr2;
   tel
tel
```

Assertions, `MAIN` annotations, and `PROPERTY` annotations also cannot be placed within if statements or frame blocks.

Since an initialization only defines a variable at the first timestep, it need not be stateful. Therefore, a frame block initialization cannot contain any `pre` or `->` operators. This restriction also ensures that initializations are never undefined.

6.7 Polymorphic nodes

In some situations, the user may want to express multiple variations of a node, where the only differences between them lie in the input and output types. For example, consider different interface type variations of the `SafePre` node, which returns the previous value of its single input, but initialized with the first value of the input stream.

```
node SafePreInt(x: int) returns (y: int);
let
  y = x -> pre x;
tel

node SafePreBool(x: bool) returns (y: bool);
```

```
let
  y = x -> pre x;
tel


node Top(x1: int; x2: bool) returns (y1: int; y2: bool);
let
  y1 = SafePreInt(y1);
  y2 = SafePreBool(y2);
tel
```

Kind 2 allows the user to express such variations more concisely through polymorphic nodes, where the user includes a set of polymorphic type parameters in the node declaration and the specific type arguments at the call site. Polymorphic type parameters are specified using angle brackets as `<ty1; ...; tyn>` whereas call-site polymorphic arguments are specified using the `@` instantiation operator.

```
node SafePre<T>(x: T) returns (y: T);
let
  y = x -> pre x;
tel


node Top(x1: int; x2: bool) returns (y1: int; y2: bool);
let
  y1 = SafePre@<int>(y1);
  y2 = SafePre@<bool>(y2);
tel
```

Note that `SafePre` can be called with any type, not just primitive types (e.g. `SafePre@<[int, bool]>(.)` and `SafePre@<[int, U]>(.)`, where `U` is itself a type parameter in the caller's declaration). Type arguments must be passed at the call site; inference of type arguments is not yet supported.

Another example is a polymorphic node `PairSwap`, which takes a polymorphic pair tuple as input and returns the corresponding swapped pair tuple as output.

```
node PairSwap<T; U>(x: [T, U]) returns (y: [U, T]);
let
y = {x[1], x[0]};
tel
```

For a polymorphic node to be well-typed, it must be meaningful for any type instantiation (in other words, the type parameters are semantically universally quantified). This type of polymorphism is called parametric polymorphism, and is also sometimes referred to as generics in general-purpose programming languages.

To illustrate these semantics, even though the `+` operator is overloaded between `int -> int`

`-> int` and `real -> real -> real`, the following polymorphic node will give a type error, as it cannot be instantiated with any type.

```
-- Generates a type error
node BadPolymorphicAdd<T>(x1, x2: T) returns (y: T);
let
  y = x1 + x2;
tel
```

Note that polymorphic nodes can have `check(.)` statements just as non-polymorphic nodes. When checking properties of polymorphic nodes at the top level, the type parameters are interpreted as abstract types.

6.8 Polymorphic contracts

In addition to polymorphic nodes, Kind 2 supports polymorphic contracts. The first way of defining a polymorphic contract is by adding a type parameter to a contract definition. For example, the `Stutter` contract states that the output `y` must either be equal to the input `x` or the previous value of `x`.

```
contract Stutter<T> (x: T) returns (y: T) ;
let
   guarantee
     (y = x) or
     (true -> (y = pre x));
tel
```

Then, the polymorphic contract can be included in a node using an import statement, where the type arguments are provided at the import statement (analogously to a polymorphic node declaration and node call).

```
contract Stutter<T> (x: T) returns (y: T) ;
let
   guarantee
     (y = x) or
     (true -> (y = pre x));
tel


node N (x: int) returns (y: int);
con
   import Stutter@<int>(x) returns (y);
noc
let
   y = pre x;
tel
```

```
node P<U>(x: U) returns (y: U);
con
    import Stutter@<U>(x) returns (y);
noc
let
   y = pre x;
tel
```

Above, node `N` instantiates the contract `Stutter` with type `int`. Also, node `P` demonstrates using a polymorphic contract declaration with a polymorphic node.

Another way of specifying a polymorphic contract is by including it directly in the node declaration of a polymorphic node as a local contract.

```
node M<T>(x: int) returns (y: int);
con
    guarantee
       (y = x) or
       (true -> (y = pre x));
noc
let
   y = pre x;
tel
```

6.9 Nondeterministic choice operator

There are situations in the design of reactive systems where nondeterministic behaviors must be modeled. Kind 2 offers a convenient polymorphic operator of the form `any { x: T | P(x) }` which denotes an arbitrary stream of values of type `T` satisfying the predicate `P`. We also support `choose { x: T | P(x) }`, where the only difference between `any` and `choose` is that `any` is nondeterministic, while `choose` is functional (deterministic and non-temporal). In the expression above `x` is a locally bound variable of Lustre type `T`, and `P(x)` is a Lustre boolean expression that typically, but not necessarily, contains `x`. The expression `P(x)` may also contain any input, output, or local variable that are in the scope of the `any` (or `choose`) expression. The following example shows a component using the `any` (or `choose`) operator to define a local stream `l` of arbitrary odd values.

```
node N(y: int) returns (z:int);
con
  assume "y is odd" y mod 2 = 1;
  guarantee "z is even" z mod 2 = 0;
```

```
noc
  var l: int;
let
  l = any { x: int | x mod 2 = 1 };
  -- with `choose`, `l` is constant
  -- l = choose { x: int | x mod 2 = 1 };
  z = y + l;
tel
```

In reality, the polymorphic operator `any` (or `choose`) can be instantiated with any Lustre type `T` using the instantiation operator `@` as follows: `any@<T>`. For instance, the expression `any@<int>` is also accepted and denotes an arbitrary stream of values of type `int`. In fact, the form `any { x: T | P(x) }` is syntactic sugar for the more verbose form `any @ < subtype { x: T | P(x) } >`, where `T` has been instantitated with the refinement type `subtype { x: T | P(x) }`.

A challenge for the user with the use of the `any` (or `choose`) operator arises if the specified condition is inconsistent, or more generally, unrealizable. In that case, the system model may be satisfied by no execution trace. As a consequence, any property, even an inconsistent one, would be trivially satisfied by the (inconsistent) system model. For instance, the condition of the `any` (or analogously, `choose`) operator in the node of the following example is inconsistent, and thus, there is no realization of the system model. As a result, Kind 2 proves the property P1 valid.

```
node N(y: int) returns (z: int);
  var l: int;
let
  l = any { x : int | x < 0 and x > 0 };
  -- Use `choose` if you want `l` to be constant
  -- l = choose { x : int | x < 0 and x > 0 };
  z = y + l;
  check "P1" z > 0 and z < 0;
tel
```

This problem is mitigated by the possibility for the user to check that the predicate `P(x)` in the `any` (or `choose`) expression is realizable. This is possible because, for each `any` (resp., `choose`) expression occurring in a model, Kind 2 introduces an internal imported node (resp., imported function) whose contract restricts the values of the returned output using the given predicate as a guarantee. The user can take advantage of this fact to detect issues with the conditions of `any` (or `choose`) expressions by enabling Kind 2's functionality that checks the realizability of contracts of imported nodes and functions. When this functionality is enabled, Kind 2 is able to detect the problem illustrated in the example above.

It is worth mentioning that Kind 2 does not consider the surrounding context when checking the realizability of the introduced imported node or function. Because of this limitation, some

checks may fail even if, in a broader context where all constraints included in the model are considered, the imported node or function would actually be considered realizable. Only the constraints imposed by the variable types are taken into account.

For instance, the realizability check for the `any` expression in the following example would fail if `b` were declared simply as an integer stream, rather than using the refinement type `subtype { x: int | a <= x }`.

```
node N(a: int) returns (z: int);
var b: subtype { x: int | a <= x };
let
  b = a + 10;
  z = any { x: int | a <= x and x <= b };
  check z>=a+10 => z=b;
tel
```

7 Arrays

Experimental feature

7.1 Lustre arrays

Kind 2 supports the traditional Lustre V5 syntax for arrays.

7.1.1 Declarations

Array variables can be declared as global, local or as input/output of nodes. Arrays in Lustre are always indexed by integers (type `int` in Lustre), and the type of an array variable is written with the syntax `t ^ <size>` where `t` is a Lustre type and `<size>` is an integer literal or a constant symbol.

The following

```
A : int ^ 3;
```

declares an array variable `A` of type array of size 3 whose elements are integers. The size of the array can also be given by a defined constant.

```
const n = 3;
...
A : int ^ n;
```

This declaration is equivalent to the previous one for `A`.

An interesting feature of these arrays is the possibility for users to write generic nodes and functions that are parametric in the size of the array. For instance one can write the following node returns the last element of an array.

```
node last (const n: int; A: int ^ n) returns (x: int);
let
  x = A[n-1];
tel
```

It takes as input the size of the array and the array itself. Note that the type of the input `A` depends on the value of the first constant input `n`. In Lustre, calls to such nodes should of course end up by having concrete values for `n`, this is however not the case in Kind 2 (see Extension to unbounded arrays).

Arrays can be multidimensional, so a user can declare e.g. matrices with the following

```
const n = 4;
const m = 5;
...

M1 : bool ^ n ^ m;
M2 : int ^ 3 ^ 3;
```

Here `M1` is a matrix of size 4x5 whose elements are Boolean, and `M2` is a square matrix of size 3x3 whose elements are integers.

> **Remark**
>
> `M1` can also be viewed as an array of arrays of Booleans.

Kind 2 also allows one to nest datatypes, so it is possible to write arrays of records, records of arrays, arrays of tuples, and so on.

```
type rational = { n: int; d: int };

rats: rational^array_size;
mm: [int, bool]^array_size;
```

In this example, `rats` is declared as an array of record elements and `mm` is an array of pairs.

7.1.2 Definitions

In the body of nodes or at the top-level, arrays can be defined with literals of the form

```
A = [2, 5, 7];
```

This defines an array `A` of size 3 whose elements are 2, 5 and 7. Another way to construct Lustre arrays is to have each elements be the same value. This can be done with expressions of the form `<value> ^ <size>`. For example the two following definitions are equivalent.

```
A = 2 ^ 3;
A = [2, 2, 2];
```

Arrays are indexed starting at 0 and the elements can be accessed using the selection operator `[ ]`. For instance the result of the evaluation of the expression `A[0]` for the previously defined array `A` is 2.

The selection operators can also be applied to multidimensional arrays. Given a matrix `M` defined by

```
M = [[1, 2, 3],
     [4, 5, 6],
     [7, 8, 9]];
```

then the expression `M[1][2]` is valid and evaluates to 6. The result of a single selection on an n-dimensional array is an (n-1)-dimensional array. The result of `M[2]` is the array `[7, 8, 9]`.

7.1.3 Unsupported features of Lustre V5

Kind 2 currently **does not support** the following features of Lustre V5:

- Array concatenation like `[0, 1] | [2, 3, 4]`
- Array slices like `A[0..3]`, `A[0..3 step 2]`, `M[0..1][1..2]` or `M[0..1, 1..2]`
- The operators are not homomorphically extended. For instance `or` has type `bool -> bool -> bool`, given two arrays of Booleans `A` and `B`, the expression `A or B` will be rejected at typing by Kind 2
- Node calls don't have an homomorphic extension either

7.2 Extension to unbounded arrays

Kind 2 provides an extension of Lustre to express equational constraints between unbounded arrays. This syntax extension allows users to inductively define arrays, give whole array definitions and allows to encode most of the other unsupported array features. This extension was originally suggested by Esterel.

> **Remark**
>
> Here, by unbounded we mean whose size is an unbounded constant.

In addition, we also enriched the specification language of Kind 2 to support (universal and existential) quantifiers, allowing one to effectively model parameterized system.

7.2.1 Whole array definitions

Equations in the body of nodes can now take the following forms

- `A = <term>` ; This equation defines the values of the array `A` to be the same as the values of the array expression `<term>`.
- `A[i] = <term(i)>` ; This equation defines the values of all elements in the array `A`. The index `i` has to be a symbol, it is bound locally to the equation and shadows all other mentions of `i`. Index variables that appear on the left hand side of equations are **implicitly universally quantified**. The right hand side of the equation, `<term(i)>` can depend on this index. The meaning of the equation is that, for any integer `i` between 0 and the size of `A`, the value at position `i` is defined as the term `<term(i)>`.

Semantically, a whole array equation is equivalent to a quantified equation. Let `A` be an array of size an integer constant `n`, then following equation is legal.

```
A[i] = if i = 0 then 2 else B[i - 1] ;
```

It is equivalent to the formula $\forall i \in [0; n]. (i = 0 \Rightarrow A[i] = 2) \wedge (i \neq 0 \Rightarrow A[i] = B[i\text{-}1])$.

Multidimensional arrays can also be redefined the same way. For instance the equation

```
M[i][j] = if i = j then 1 else 0 ;
```

defines `M` as the identity matrix

```
[[ 1 , 0 , 0 ,..., 0 ],
 [ 0 , 1 , 0 ,..., 0 ],
 [ 0 , 0 , 1 ,..., 0 ],
 .................. ,
 [ 1 , 0 , 0 ,..., 1 ]]
```

It is possible to write an equation of the form

```
M[i][i] = i;
```

but in this case the second index `i` shadows the first one, hence the definition is equivalent to the following one where the indexes have been renamed.

```
M[j][i] = i;
```

7.2.2 Inductive definitions

One interesting feature of these equations is that we allow definitions of arrays inductively. For instance it is possible to write an equation

```
A[i] = if i = 0 then 0 else A[i-1] ;
```

This is however not very exciting because this is the same as saying that `A` will contain only zeros, but notice we allow the use of `A` in the right hand side.

Dependency analysis

Inductive definitions are allowed under the restriction that they should be well founded. For instance, the equation

```
A[i] = A[i];
```

is not and will be rejected by Kind 2 the same way the equation `x = x;` is rejected. Of course this restriction does not apply for array variables under a `pre`, so the equation `A[i] = pre A[i];` is allowed.

In practice, Kind 2 will try to prove statically that the definitions are well-founded to ensure the absence of dependency cycles. We only attempt to prove that definitions for an array `A` at a given index `i` depends on on values of `A` at indexes strictly smaller than `i`.

For instance the following set of definitions is rejected because e.g. `A[k]` depends on `A[k]`.

```
A[k] = B[k+1] + y;
B[k] = C[k-1] - 2;
C[k] = A[k] + k;
```

On the other hand this one will be accepted.

```
A[k] = B[k+1] + y;
B[k] = C[k-1] - 2;
C[k] = ( A[k-1] + B[k] ) * k ;
```

Because the order is fixed and that the checks are simple, it is possible that Kind 2 rejects programs that are well defined (with respect to our semantic for whole array updates). It will not, however, accept programs that are ill-defined.

For instance each of the following equations will be rejected.

```
A[i] = if i = 0 then 0 else if i = 1 then A[0] else A[i-1];
```

```
A[i] = if i = n then 0 else A[i+1];
```

```
A[i] = if i = 0 then 0 else A[0];
```

Examples

This section gives some examples of usage for inductive definitions and whole array updates as a way to encode unsupported features and as way to encode complicated functions succinctly.

Sum of the elements in an array

The following node returns the sum of all elements in an array.

```
node sum (const n: int; A: int ^ n) returns (s: int);
var cumul: int ^ n;
let
  cumul[i] = if i = 0 then A[0] else A[i] + cumul[i-1];
  s = cumul[n-1];
tel
```

We declare a local array `cumul` to store the cumulative sum (i.e. `cumul[i]` contains the sum of elements in `A` up to index `i`) and the returned value of the node is the element stored in the last position of `cumul`.

Note that this node is parametric in the size of the array.

Array slices

Array slices can be trivially implemented with the features presented above.

```
node slice (const n: int; A: int ^ n; const low: int; const up: int)
returns (B : int ^ (up-low));
let
  B[i] = A[low + i];
tel
```

Homomorphic extensions

Encoding an homomorphic `or` on Boolean arrays is even simpler.

```
node or_array (const n: int; A, B : bool^n) returns (C: bool^n);
let
  C[i] = A[i] or B[i];
tel
```

Defining a generic homomorphic extension of node calls is not possible because nodes are not first order objects in Lustre.

Parameterized systems

It is possible to describe and check properties of parameterized systems. Contrary to the Lustre compilers, Kind 2 does not require the constants used as array sizes to be instantiated with actual values. In this case the properties are checked for any array sizes.

```
node slide (const n:int; s: int) returns(A: int^n);
let
  A[i] = if i = 0 then s else (-1 -> pre A[i-1]);

  --%PROPERTY n > 1 => (true -> A[1] = pre s);
tel
```

This node stores in an array `A` a sliding window over an integer stream `s`. It saves the values taken by `s` up to `n` steps in the past, where `n` is the size of the array.

Here the property says, that if the array `A` has at least two cells then its second value is the previous value of `s`.

7.2.3 Quantifiers in specifications

To better support parameterized systems or systems with large arrays, we expose quantifiers for use in the language of the specifications. Quantifiers can thus appear in **properties**, **contracts** and **assertions**.

Universal quantification is written with:

```
forall ( <x : type>;+ ) P(<x>+)
```

where `x` are the quantified variables and `type` is their type. `P` is a formula or a predicate in which the variable `x` can appear.

For example, the following

```
forall (i, j: int) 0 <= i and i < n and 0 <= j and j < n => M[i][j] = M[j][i]
```

is a formula that specifies that the matrix `M` is symmetric.

> **Remark**
>
> Existential quantification takes the same form except we use `exists` instead of `forall`.

Quantifiers can be arbitrarily nested and alternated at the propositional level.

Example

The same parameterized system of a sliding window, slightly modified to express the property that `A` contains in each of its cells, an uninitialized value (i.e. value `-1`), or one of the previous values of the stream `s`.

```
node slide (const n:int; s: int) returns(ok: bool^n);
var A: int^n;
let
  A[i] = if i = 0 then s else (-1 -> pre A[i-1]);
  ok[i] = A[i] = -1 or A[i] = s or (false -> pre ok[i]);


  --%PROPERTY forall (i: int) 0 <= i and i < n => ok[i];
tel
```

7.2.4 Limitations

One major limitation that is present in the arrays of Kind 2 is that one cannot have node calls in inductive array definitions whose parameters contain unbounded array indices.

For instance, it is currently not possible to write the following in Kind 2 where `A` and `B` are arrays, `n` is a symbolic constant, and `some_node` takes values as inputs.

```
node some_node (x: int) returns (y: int);
...

A, B: int^n;
...

A[i] = some_node(B[i]);
```

Another limitation is that quantified variables cannot appear in the parameters of a node call. These limitations do not apply if the call is to an inlinable function, which is currently defined as a function that meets all the following criteria:

- It has a single output, and the output is defined by an equation.
- Either there is no proof obligation on its output (via a contract or a refinement type), or the function is annotated as transparent.
- It does not include `assert` statements or array definitions.

7.2.5 Command line options

We provide different encodings of inductive array definitions in our internal representation of the transition system. The command line interface exposes different options to control which encoding is used. This is particularly relevant for SMT solvers that have built-in features, whether it is support for the theory of arrays, or special options or annotations for quantifier instantiation.

These options are summed up in the following table and described in more detail in the rest of this section.

Option	Description
–smt_arrays	Use the builtin theory of arrays in solvers
–inline_arrays	Instantiate quantifiers over array bounds in case they are statically known
–arrays_rec	Define recursive functions for arrays (for cvc5)

The default encoding will use quantified formulas for inductive definitions and whole array updates.

For example if we have

```
A : int^6;
...
A[k] = x;
```

we will generate internally the constraint

> k: int. $0 <= k < 6 =>$ (select A k) = x

These form of constraint are handled in an efficient way by cvc5 (thanks to finite model finding).

`--smt_arrays`

By default arrays are converted using ah-hoc selection functions to avoid stressing the theory of arrays in the SMT solvers. This option tells Kind 2 to use the builtin theory of arrays of the solvers instead. If you want to try it, it's probably a good idea to use it in combination of `--smtlogic detect` for better performances.

`--inline_arrays`

By default, Kind 2 will generate problems with quantifiers for arrays which should be useful for problems with large arrays. This option tells Kind 2 to instantiate these quantifiers when it can reasonably do so. Only cvc5 has a good support for this kind of quantification so you may want to use this option with the other solvers.

The previous example

```
A : int^6;
...
A[k] = x;
```

will now be encoded by the constraint

> (select A 0) = x (select A 1) = x (select A 2) = x (select A 3) = x (select A 4) = x (select A 5) = x

`--arrays_rec`

This uses a special kind of encoding to tell cvc5 to treat quantified definitions of some uninterpreted functions as recursive definitions.

8 Machine Integers

Kind2 supports both signed and unsigned versions of C-style machine integers of width 8, 16, 32, and 64.

8.1 Declarations

Machine integer variables can be declared as global, local, or as input/ouput of nodes. Signed machine integers are declared as type `intN` and unsigned machine integers are declared as type `uintN` where N is the width (8, 16, 32, or 64).

The following

```
x : uint8;
y : int16;
```

declares a variable `x` of type unsigned machine integer of width 8, and variable `y` of type signed machine integer of width 16.

8.2 Values

Machine integers values can be constructed using implicit conversion functions applied to integer literals. The implicit conversion functions are of the form `uintN` for unsigned machine integers and `intN` for signed machine integers.

The following

```
x = uint8 27;
y = int16 -5012;
```

defines `x` to have value 27, and `y` to have value -5012, given that `x` is a variable of type `uint8` and `y` is a variable of type `int16`.

8.3 Semantics

Machine integers of width `x` represent binary numbers of size `x`. Signed machine integers are represented using 2's complement.

The bounds of machine integers are specified here for convenience:

```
uint8  : 0 to 255
uint16 : 0 to 65535
```

```
uint32 : 0 to 4294967295
uint64 : 0 to 18446744073709551615
int8   : -128 to 127
int16  : -32768 to 32767
int32  : -2147483648 to 2147483647
int64  : -9223372036854775808 to 9223372036854775807
```

When the conversion functions are used for literals that are out of this range, they are converted to a machine integer that is in range using the modulo operation, as in C. For instance, in the following

```
x = uint8 256;
y = int16 32768;
```

x evaluates to 0 and y to -3268, given that x is a variable of type uint8 and y is a variable of type int16.

Conversions are allowed between machine integers of different widths, as long as both types are either signed or unsigned. Values remain unchanged when converted from a smaller to a larger width; values are adjusted modulo the range of the destination type when converted from larger to smaller width. The following code illustrates this.

```
a : int8;
b : int16;
c : uint16;
d : uint8;
a = int8 120;
b = int16 a; -- b == int16 120
c = uint16 300;
d = uint8 c; -- c == uint8 44
```

8.4 Operations

Kind2 allows the following operations over the machine integer types.

8.4.1 Arithmetic Operations

Addition (+), subtraction (-), multiplication (*), division (div), modulo (mod), and unary negation (-) are allowed on either signed or unsigned machine integers, and return a machine integer with the same sign and same width as the input(s).

```
a, a1, a2 : uint8;
b : uint16;
```

```
c : uint32;
d : uint64;
e, f : int8;
a1 = (uint8 5);
a2 = (uint8 22);
a = a1 + a2;
b = (uint16 20) * (uint16 200);
c = (uint32 500) div (uint32 5);
d = (uint64 25) mod (uint64 10);
e = (int8 -5) + (- (int8 10));
f = (int8 10) - (int8 -5);
```

8.4.2 Logical Operations

Conjunction (`&&`), disjunction (`||`), and negation (`!`) are performed in a bitwise fashion over the binary equivalent of their machine integer inputs. Conjunction and disjunction are binary, while negation is unary. All 3 operations return a machine integer that has the same sign and same width as its input(s).

```
a, b, b1, b2, c : uint8;
a = (uint8 0) && (uint8 45); --a = (uint8 0)
b1 = (uint8 255);
b2 = (uint8 45);
b = b1 && b2; --b = (uint8 45)
c = !(uint8 0); --c = (uint8 255)
```

8.4.3 Shift Operations

Left shift (`lsh`) and right shift (`rsh`) operations are binary operations: the first input is either signed or unsigned, the second input is unsigned, and the sign of the output matches that of the first input; both inputs and the output have the same width.

Right shifting when the first operand is signed, results in an arithmetic right shift, where the bit shifted in matches the sign bit.

A left shift is equivalent to multiplication by 2, and a right shift is equivalent to division by 2, as long as the result can fit into the machine integer of the same width. In other words, the left shift operator shifts towards the most-significant bit and the right shift operator shifts towards the least-significant bit.

```
a, b, c : bool;
a = (uint8 0) lsh (uint8 10) = (uint8 0); --true
b = (uint8 255) rsh (uint8 12) = (uint8 255); --true
c = (int8 -1) lsh (uint8 1) = (int8 -2); --true
```

51

8.4.4 Comparison Operations

The following comparison operations are all binary: `>`, `<`, `>=`, `<=`, `=`. They input machine integers of the same size and sign, and output a boolean value.

```
a : bool;
a = (int8 -12) < (int8 12); --true
```

8.5 Limitations

Currently, only SMT solvers cvc5 and Z3 support logics that allows the usage of integers and machine integers together. To use any of the other supported SMT solvers, the Lustre input must contain only machine integers.

Moreover, the IC3QE engine requires either cvc5 or Z3, and the IC3IA engine requires MathSAT, cvc5, or Z3, to run on models with machine integers. If these requirements are not satisfied, Kind 2 runs with the corresponding IC3 model checking engine disabled.

9 Refinement Types

Kind 2 supports refinement types. A refinement type is comprised of two components: (i) a **base type**, and (ii) a predicate that restricts the members of the base type.

9.1 Declarations

Refinement types have syntax of the form `subtype { var: base_type | P(var) }`.

For example, `type Nat = subtype { x: int | x >= 0 }` declares a refinement type `Nat` over the base type `int`, where the values of `Nat` are all the nonnegative integers. When assigning a refinement type to a node input, output, or local variable, Kind 2 also supports an alternative, more concise syntax of the form `var: base_type | P(var)`.

For example,

```
node N(x: int | x >= 0) returns (y: int | y >= 0);
```

denotes the interface of a node `N` which takes a stream of natural numbers `x` as input and returns a stream of natural numbers `y` as output. The above example can be equivalently expressed using the full syntax:

```
node N(x: subtype { n: int | n >= 0 }) returns (y: subtype { n: int | y >= 0});
```

The base type being refined can be any type, not just a primitive type. For example,

```
type Nat = subtype { x: int | x >= 0 };
type LessThan100 = { x: Nat | x < 100 };
```

declares a refinement type `LessThan100` whose base type `Nat` is itself a refinement type. Note that we can still recursively chase base types until we reach a primitive type. In this case, `LessThan100`'s recursively chased primitive base type is `int`.

Additionally, refinement types can be components of more complicated types:

```
const n: int;
type Nat = subtype { x: int | x >= 0 };
type NatArray = Nat^n;
```

Above, we declare a type `NatArray`, an array of natural numbers.

Since Lustre is a declarative language, there is no conceptual ordering between variable declarations (input, output, and local variables). A consequence of this is that refinement type predicates can contain variables that are defined before or after the current variable in the input file. For example, the following is legal.

```
node N() returns (x: | x <= y; y | y = x + 10);
```

Above, the predicate in `x`'s type references `y`, which is allowed even though `y` comes after `x` in the list of node outputs.

9.2 Semantics

Refinement types on input variables represent assumptions, while refinement types on locals and node outputs represent proof obligations.

Consider the following example:

```
type Even = subtype { n: int | n mod 2 = 0 };
type Odd = subtype { n: int | n mod 2 = 1 };

node M(x1: Even; x2: Odd) returns (y: Odd);
let
   y = x1 + x2;
   --%MAIN;
tel
```

Kind2 will attempt to prove that node `M`'s output `y` respects type `Odd` while assuming that input `x1` has type `Even` and input `x2` has type `Odd`. More intuitively, Kind 2 will prove that adding an even and an odd integer results in an odd integer. Conceptually, the refinement types can be viewed as an augmentation of `M`'s contract as follows:

```
node M(x1: int; x2: int) returns (y: int);
con
   assume x1 mod 2 = 0;
   assume x2 mod 2 = 1;
   guarantee y mod 2 = 1;
noc
let
   y = x1 + x2;
   --%MAIN;
tel
```

If an output variable with a refinement type is left undefined, Kind 2 will specify that the value ranges over a recursively chased base type.

```
node M() returns (y: Nat | y < 100);
let
tel
```

In the above example, `M`'s return value `y` will range over all integers, not just natural numbers

less than 100. This is because `y` is an output variable, and therefore its refinement type is viewed as a proof obligation. In this case, Kind 2 will report that `y` violates its refinement type.

9.3 Operations

From the point of view of primitive operations (e.g. `+`, `-`, `pre`) and node calls, variables with refinement types can syntactically be used anywhere that variables with the corresponding base type can be used, and vice versa. For example, if `x` has type `Nat`, `y` has type `Nat`, and `z` has type `int`, then `x+y`, `z+x`, and `y+z` (among other combinations) are all legal. Further, if node `M` has a single parameter of type `Nat`, then the node call `M(z)` is legal, and if node `N` has a single parameter of type `int`, then the node call `M(x)` is legal.

While all of the above are syntactically valid, Kind 2 may still fail type-related proof obligations. For example, in the node call `M(z)` (where `z` has type `int` and `M` takes a single parameter of type `Nat`), `M`'s typing assumption on its input will be violated if `z` can be negative.

9.4 Realizability

Because refinement types are essentially contract augmentations, it is possible to specify refinement types that are unrealizable. In other words, it is possible to specify refinement type contraints that are unimplementable (impossible to satisfy with any implementation).

As an example, the following node interface is unrealizable:

```
node M(x: int) returns (y: int | 0 <= y and y <= x);
```

Output variable `y`'s refinement type states that `y` must be between `0` and `x`. However, if input `x` is negative, then no value for `y` will satisfy its type.

One way to make the above interface realizable is to add a refinement type for `x`:

```
node M(x: int | x >= 0) returns (y: int | 0 <= y and y <= x);
```

To check the realizability of refinement types, one can call `kind2 <filename> --enable CONTRACTCK`. Kind 2 performs three types of realizability checks:

1. Node and imported node contracts, including type information
2. Node environments, i.e., checking that the set of assumptions on a node's input is realizable
3. Individual refinement types, i.e., that a global refinement type declaration is realizable

You can specify a particular node or function to analyze using `--lus_main <node_name>`, and a specific refinement type using `--lus_main_type <type_name>`.

9.5 Structured types

Refinement types can be arbitrarily nested within structured types (e.g., tuple component types, array and set element types, and map key and value types). For example, consider node N below.

```
type Nat = subtype { x: int | x >= 0 };
const N: Nat;

node N () returns (my_tuple: [Nat, int]; my_set: set<Nat>;
                   my_array: Nat^N; my_map: map<Nat, Nat>)
...
```

Due to the refinement types, node N carries the following proof obligations: my_tuple[0] $>=$ 0 (for the tuple's first component type), forall (e: int) e in my_set $=>$ e $>=$ 0 (for the set's element type), forall (i: int) 0 $<=$ i and i $<$ N $=>$ my_array[i] $>=$ 0 (for the array's element type), forall (k: int) k in my_map $=>$ k $>=$ 0 (for the map's key type), and forall (k: int) k in my_map $=>$ my_map[k] $>=$ 0 (for the map's value type). If one has refinement types in node inputs, node locals, or global constants, assumptions or proof obligations (depending on the case) are generated analogously.

10 Enumeration types

```
type my_enum = enum { A, B, C };
node n (x : my_enum, ...) ...
```

Enumerated datatypes are encoded as subranges so that solvers handle arithmetic constraints only. This also allows to use the already present quantifier instantiation techniques in Kind 2.

10.1 N-way merge

As in Lustre V6, merges can also be performed on a clock of a user defined enumerated datatype.

```
merge c
 (A -> x when A(c))
 (B -> w + 1 when B(c));
```

Arguments of merge have to be sampled with the correct clock. Clock expressions for merge can be just a clock identifier or its negation or `A(c)` which is a stream that is true whenever `c = A`.

Merging on a Boolean clock can be done with two equivalent syntaxes:

```
merge(c; a when c; b when not c);

merge c
  (true -> a when c)
  (false -> b when not c);
```

11   History Types

In order to improve the expressivity of Kind 2's specification language, the tool provides a built-in type constructor that allows users to refer to an unbounded number of previous values of a stream. Specifically, the unary type constructor `history(x)`, that takes a stream `x` of arbitrary type `T` as its single argument, represents the set of all streams `z` of values of type `T` such that at any time `t >= 0`, there exists a `k` in the interval `[0, t]` such that `z(t) = x(k)`.

For instance, given a node with an input stream `x` and an output stream `y`, both with the same type, the property the current value of stream y equals the current value or a previous value of a stream x plus one can't be expressed in Lustre. However, using the type constructor `history`, one can easily express the property as `exists (z: history(x)) y=z+1`.

Notice that `history(x)` denotes a refinement type, suggesting its applicability wherever a type is expected in the model. However, at present, the implementation restricts the use of the type constructor `history` to the type of a quantified variable. We plan to lift this restriction in future versions of Kind 2.

12   Abstract Types

Kind 2 supports Lustre's **abstract types**, which are user-declared types without definitions. Abstract types are declared with the syntax `type <name>`. Below is a simple Lustre file that declares an identity node that takes an input of (abstract) type `T` and returns an output of type `T` equal to the input.

```
type T;
function id_T (x: T) returns (y: T);
let
    y = x;
tel
```

In Kind 2, all abstract types have infinite domains. As a result, assumptions that constrain an abstract type to a finite domain are inconsistent (such an example is shown in the following code block).

```
type T;
function id_T (x: T) returns (y: T);
con
    assume forall (x: T) (forall (y: T) x = y);
noc
let
    y = x;
tel
```

Thus, users should exercise caution with assumptions involving quantification over variables with abstract types.

13 Polymorphic User Types

Kind 2 supports **polymorphic user types**, which are user-defined types that contain type parameters. An example is a polymorphic user-defined `Pair` type, declared as `type Pair<T; U> = [T, U];`.

A polymorphic user-defined type `T` is instantiated with `T<...>` syntax (analogous to polymorphic nodes and node calls) as in the following examples.

```
type Pair<T; U> = [T, U];


node SwapIntBool(x: Pair<int; bool>) returns (y: Pair <bool; int>)
let
    y = {x.%1, x.%0};
tel


node SwapGeneric<T; U>(x: Pair<T; U>) returns (y: Pair <U; T>)
let
    y = {x.%1, x.%0};
tel
```

In other words, `Pair` (or any other user-defined polymorphic type) can be viewed as as a **type constructor** which takes types as inputs and returns a type.

14   Tuple types

Tuples are constructed with the syntax `'(x1, ..., xn)` and destructed with the syntax `t[idx]`, where `idx` is some concrete natural number that is in range (with `0`-based indexing).

```
type my_tuple = [int, bool, real];
node n (x : my_tuple) returns (y : my_tuple)
let
  y = '(0, false, x[2]);
tel
```

15 Sets

Set types have the syntax `set<T>`, where `T` is any type that does not contain sets, maps, or arrays. For example `set<int>` denotes (streams of) sets of integers, and `set<[bool, int]>` denotes (streams of) sets of Boolean and integer pairs.

Set literals can be constructed with curly braces with comma-separated elements, e.g. `{ 1 }`, `{ 1, 2, 3 }`, and `{ x, 4 }` (assuming `x` has type `int`). Type annotations are required for empty sets (e.g. `{}@<int>`) and optional for non-empty set literals (e.g. `{ 1 }@<int>`).

The built-in set operators are **set union** (denoted by `+`), **set intersection** (denoted by `*`), and **set membership** (denoted by `in`). All are infix and take the expected semantics; see below for an example.

```
node N (s1, s2: set<int>) returns (out: set<int>)
let
  out = s1 * { 1, 2, 3 } + {}@<int>;

  check forall (i: int) not (i in s1 + s2) = (not (i in s1) and not (i in s2));
  check forall (i: int) i in out => (i = 1 or i = 2 or i = 3);
tel
```

16 Maps

Map types have the syntax `map<K, V>` (or `map<K; V>`), where `V` is any type, and `K` is any type that does not contain sets, maps, or arrays. For example `map<int, int>` denotes (streams of) maps of integers to integers, and `map<set<[bool, int]>, real>` denotes (streams of) maps of Boolean and integer pairs to reals.

Map literals can be built with the constructor `map[k1 := v1; ...; kn := v2]` which creates a map with keys `k1` through `kn`, each mapping to its corresponding value. For example, `map[0 := 0; 1 := 1]`, `map[{ '(false, 0) } := 0.0]`, and `map[x := y]` are all valid map literals. Type annotations are required for empty maps (e.g. `map[]@<int, int>`) and optional for non-empty map literals (e.g. `map[1 := 1]@<int, int>`).

The built-in map operators are **map insertion/update** (denoted by `m[k1 := v1; ...; kn := vn]` for map expression `m`), **map index access** (denoted by `m[k]`), and **map (key) membership** (denoted by `in`). Indexing a map with `m[k]` returns the associated value for `k` in map `m`. If `m` does not have a binding for `k`, then the output of the operation is unconstrained. However, the operation is still functional in the sense that indexing a map will always yield the same value for a fixed key and timestep (i.e., for all maps `m` and keys `k` of the proper type, `m[k] = m[k]` is valid, even if key `k` is not in the map `m`). Otherwise, the operators all take the expected semantics. See below for an example.

```
node N (inp: map<int, int>) returns (out, out2: map<int, int>)
let
  out = inp[0 := 0; 1 := 1; 2 := 2];
  out2 = map[0 := 0; 1 := 1];

  check 0 in out;
  check out[0] = 0;
  check forall (i: int) not (i in { 0, 1, 2 }) => out[i] = inp[i];
  check forall (i: int) not (i = 0 or i = 1) => not (i in out2);
tel
```

17 JSON / XML Output

Kind 2 can output its results in two structured formats: JSON and XML. They facilite the processing of Kind 2's results by external tools. The next sections describe each of these output formats in detail.

17.1 JSON format

The JSON output is activated by running Kind 2 with the `-json` option. Its syntax is fully specified by the JSON schema available in the schemas/kind2-output.json file.

The root element of a JSON output document is either a Log Object if Kind 2 terminates early with an error, or an array of Results Objects if Kind 2 succeeds generating some result. Every Results Object (including Log Object) is identified and distinguished from other Results objects by a property of type string called `objectType`.

In a successful execution, a Kind2 Options Object specifies the options used by the tool, and any Log message is added to the array as it is written. When Kind 2 is run as an interpreter, the array includes one Execution Object that contains a description of the computed values for the output and state variables. Otherwise, Kind 2 works as a model checker and performs a series of analyses. The beginning of a main analysis is indicated by an AnalysisStart Object, and its end by an AnalysisStop Object. Within these delimiters, a Property Object describes the result for a particular property of the input model under the parameters of the analysis. When the verbose mode is enabled, statistics and progress info of the analysis is also recorded along through Stat and Progress objects.

Similarly to main analyses, when a post-analysis is enabled, the beginning of the post-analysis is indicated by an PostAnalysisStart Object, and its end by an PostAnalysisEnd Object.

17.1.1 Log Object

A `Log` object records an informative message from the tool. The value of its `objectType` property is `log`. The list of properties of a `Log` object are:

Key	Type	Description
level	string	A level that gives a rough guide of the importance of the message. Can be `fatal`, `error`, `warn`, `note`, `info`, `debug`, or `trace`.
source	string	The name of the Kind 2 module which wrote the log.
file	string	Associated input file, if any.
line	integer	Associated line in the input file, if any.
column	integer	Associated column in the input file, if any.
value	string	The log message.

17.1.2 Results Objects

A `Result object` can be one of the following objects: a Log Object, a Kind2 Options Object, an AnalysisStart Object, an AnalysisStop Object, a Property Object, a Stat Object, a Progress Object, a PostAnalysisStart Object, or a PostAnalysisEnd Object.

17.1.3 Kind2 Options Object

A `Kind2 options` object describes the options used by the tool in the current execution. The value of its `objectType` property is `kind2Options`. The list of properties of a `Kind2 options` object are:

Key	Type	Description
`enabled`	`array`	List of Kind 2 module names that are enabled.
`timeout`	`number`	The wallclock timeout used for all the analyses.
`bmcMax`	`integer`	Maximal number of iterations for BMC and K-induction.
`compositional`	`boolean`	Whether compositional analysis is enabled or not.
`modular`	`boolean`	Whether modular analysis is enabled or not.

17.1.4 AnalysisStart Object

An `AnalysisStart` object indicates the beginning of a main analysis. The value of its `objectType` property is `analysisStart`. The list of properties of an `AnalysisStart` object are:

Key	Type	Description
`top`	`string`	Name of the current top-level component.
`concrete`	`array`	Names of the subcomponents whose implementation is used in the analysis.
`abstract`	`array`	Names of the subcomponents whose contract is used in the analysis.
`assumptions`	`array`	Array of pairs (name of subcomponent, number of considered invariants).

17.1.5 AnalysisStop Object

An `AnalysisStop` object indicates the end of a main analysis. The value of its `objectType` property is `analysisStop`. No properties are associated.

17.1.6 Property Object

A `Property` object describes the result for a particular property of the input model. The result should be considered in the context of the analysis in which the property object is contained. The value of its `objectType` property is `property`. The list of properties of an `AnalysisStart` object are:

Key	Type	Description
`name`	`string`	Property identifier or description.
`scope`	`string`	Name of the component where the property was analyzed.
`line`	`integer`	Associated line in the input file, if any.
`column`	`integer`	Associated column in the input file, if any.
`source`	`string`	Origin of the property. Can be `Assumption` if it comes from an assumption check, `Guarantee` if it comes from the check of a guarantee, `Ensure` if it comes from a check of a require-ensure clause in a contract mode, `OneModeActive` if it comes from an exhaustiveness check of the state space covered by the modes of a contract, and `PropAnnot` if it comes from the check of a property annotation.
`runtime`	`object`	The runtime of the analysis (in seconds), and whether the timeout expired
`k`	`integer`	The value of `k` in a k-inductive proof, if any.
`trueFor`	`integer`	The largest value of `k` for which the property was proved to be true, if any.
`answer`	`object`	The `source` of the answer, and the result `value` of the check. The result can be `valid`, `falsifiable`, or `unknown`.
`counterExample`	`object`	Counterexample to the property satisfaction (only available when `answer` is `falsifiable`). It describes a sequence of values for each stream that leads the system to the violation of the property. It also gives the list of contract modes that are active at each step, if any.

17.1.7 Stat Object

An `Stat` object provides statistics info about the current analysis. The value of its `objectType` property is `stat`. The list of properties of a `Stat` object are:

Key	Type	Description
source	string	Name of the Kind 2 module which reported the info.
sections	array	List of `statSection` objects, each of them with a section `name` and a list of `statItem` objects. Each `statItem` has a `name`, a `type`, and a `value`. See schemas/kind2-output.json for further details.

17.1.8 Progress Object

An `Progress` object reports the current value of `k` for k-inductive-based analyses. The value of its `objectType` property is `progress`. The list of properties of a `Progress` object are:

Key	Type	Description
source	string	Name of the k-inductive-based analysis.
k	integer	Value for `k`.

17.1.9 PostAnalysisStart Object

An `PostAnalysisStart` object indicates the beginning of a post-analysis. The value of its `objectType` property is `postAnalysisStart`. The list of properties of an `PostAnalysisStart` object are:

Key	Type	Description
name	string	Name of the post-analysis

The post-analyses currently available are Test Generation (`testgen`), Proof Certificates (`certification`), Contract Generation (`contractgen`), Invariant Printing (`invprint`), and Inductive Validity Core (`ivc`).

17.1.10 PostAnalysisEnd Object

An `PostAnalysisEnd` object indicates the end of a post-analysis. The value of its `objectType` property is `postAnalysisEnd`. No properties are associated.

17.1.11 Execution Object

An `Execution` object describes the sequences of values for the output and state variables of an input model computed from its simulation (see the interpreter mode). The value of its `objectType` property is `execution`. It only has one object property called `trace` which follows the same format than property `counterExample` in Property Object.

17.1.12 ModelElementSet Object

A `ModelElementSet` object describes a set of model elements (a model element can be an equation, a node call, an assumption, a guarantee, etc). It is used to describe a core that we can get from an Inductive Validity Core (`ivc`) or Minimal Cut Set (`mcs`) analysis. The result should be considered in the context of the analysis or post-analysis in which the ModelElementSet object is contained. The value of its `objectType` property is `modelElementSet`.

Key	Type	Description
`class`	`string`	Class of the core. Can be `must`, `must complement`, `ivc`, `ivc complement`, `mcs` or `mcs complement`.
`size`	`integer`	Number of model elements in the core.
`property`	`string`	The property associated with the core. If all properties are considered, this field is missing.
`runtime`	`object`	The runtime for computing the core (in seconds).
`nodes`	`array`	For each node, contains an object that enumerates the model elements of the node that are part of the core.
`counterExample`	`object`	Counterexample to the property satisfaction (only when relevant, that is, when class is `mcs` or `mcs complement`). See the `property` object for more info.

17.2 XML format

The XML output is activated by running Kind 2 with the `-xml` option. Its syntax is fully specified by the XML schema available in the schemas/kind2-output.xsd file.

The root element of a XML output document is either a Log Element if Kind 2 terminates early with an error, or a Results Element if Kind 2 succeeds generating some result.

17.2.1 Log Element

A `Log` element is a simple element that records an informative message from the tool. The list of attributes of a `Log` element are:

Attribute	Base Type	Description
class	xs:string	A level that gives a rough guide of the importance of the message. Can be `fatal`, `error`, `warn`, `note`, `info`, `debug`, or `trace`.
source	xs:string	The name of the Kind 2 module which wrote the log.
line	xs:integer	Associated line in the input file, if any.
column	xs:integer	Associated column in the input file, if any.

17.2.2 Results Element

A `Results` element is a sequence of zero or more of the following elements: a Log Element, an AnalysisStart Element, an AnalysisStop Element, a Property Element, a Stat Element, a Progress Element, a PostAnalysisStart Element, a PostAnalysisEnd Element, or an Execution Element.

The list of attributes of a `Results` element are:

Attribute	Base Type	Description
enabled	xs:string	List of comma-separated Kind 2 enabled module names.
timeout	xs:decimal	The wallclock timeout used for all the analyses.
bmc_max	xs:integer	Maximal number of iterations for BMC and K-induction.
compositional	xs:boolean	Whether compositional analysis is enabled or not.
modular	xs:boolean	Whether modular analysis is enabled or not.

17.2.3 AnalysisStart Element

An `AnalysisStart` element is an empty element that indicates the beginning of a main analysis. The list of attributes of an `AnalysisStart` element are:

Attribute	Base Type	Description
`top`	`xs:string`	Name of the current top-level component.
`concrete`	`xs:string`	Names of the subcomponents whose implementation is used in the analysis (comma-separated list).
`abstract`	`xs:string`	Names of the subcomponents whose contract is used in the analysis (comma-separated list).
`assumptions`	`xs:string`	Comma-separated list of pairs (subcomponent name, number of considered invariants).

17.2.4 AnalysisStop Element

An `AnalysisStop` element is an empty element that indicates the end of a main analysis. No attributes.

17.2.5 Property Element

A `Property` element describes the result for a particular property of the input model. The result should be considered in the context of the analysis in which the property element is contained. The list of attributes of a `Property` element are:

Attribute	Base Type	Description
`name`	`xs:string`	Property identifier or description.
`scope`	`xs:string`	Name of the component where the property was analyzed.
`file`	`xs:string`	Associated input file, if any.
`line`	`xs:integer`	Associated line in the input file, if any.
`column`	`xs:integer`	Associated column in the input file, if any.
`source`	`xs:string`	Origin of the property. Can be `Assumption` if it comes from an assumption check, `Guarantee` if it comes from the check of a guarantee, `Ensure` if it comes from a check of an ensure clause in a contract mode, `OneModeActive` if it comes from an exhaustiveness check of the state space covered by the modes of a contract, and `PropAnnot` if it comes from the check of a property annotation.

A `Property` element contains one `Answer` element, which includes the result for the property check (`valid`, `falsifiable`, or `unknown`), and identifies the Kind 2 module responsible for the answer. If the result is `valid`, or `falsifiable`, it also contains a `Runtime` element, which

reports the runtime of the analysis (in seconds), and whether the timeout expired or not. If the result is `valid`, a K element gives the value of k for which the property was proved valid. If the result is `falsifiable`, a `Counterexample` element describes a sequence of values for each stream that leads the system to the violation of the property. It also gives the list of contract modes that are active at each step, if any. If the result is `unknown`, the `Property` element may contain a `TrueFor` element specifying the largest value of k for which the property was proved to be true.

17.2.6 Stat Element

An `Stat` element provides statistics info about the current analysis. It has only one attribute of type `xs:string`, `source`, which is the name of the Kind 2 module which reported the piece of information. Its content consists in one or more `Section` elements. Each section has one `name` element, and one or more `item` elements. Each `item` element has one `name` element, and either a `value` element or a `valuelist` element. A `valuelist` has one or more `value` elements, and each `value` element has a `type` attribute (currently `int` or `float`), and its content is the actual value.

17.2.7 Progress Element

A `Progress` element is a simple element that reports the current value of k for a k-inductive-based analysis. It has only one attribute of type `xs:string`, `source`, which is the name of the k-inductive-based analysis.

17.2.8 PostAnalysisStart Element

An `PostAnalysisStart` element is an empty element that indicates the beginning of a post-analysis. It has only one attribute of type `xs:string`, the `name` of the post-analysis. The post-analyses currently available are Test Generation (`testgen`), Proof Certificates (`certification`), Contract Generation (`contractgen`), Invariant Printing (`invprint`), and Inductive Validity Core (`ivc`).

17.2.9 PostAnalysisEnd Element

An `PostAnalysisEnd` element is an empty element that indicates the end of a post-analysis. No attributes.

17.2.10 Execution Element

An `Execution` element describes the sequences of values for the output and state variables of an input model computed from the simulation of its execustion (see the interpreter mode).

17.2.11 ModelElementSet Element

A `ModelElementSet` element describes a set of model elements (a model element can be an equation, a node call, an assumption, a guarantee, etc). It is used to describe a core that we can get from an Inductive Validity Core (`ivc`) or Minimal Cut Set (`mcs`) analysis. The result should be considered in the context of the analysis or post-analysis in which the ModelElementSet element is contained. The list of attributes of a `ModelElementSet` element are:

Attribute	Base Type	Description
class	string	Class of the core. Can be `must`, `must complement`, `ivc`, `ivc complement`, `mcs` or `mcs complement`.
size	integer	Number of model elements in the core.
property	string	The property associated with the core. If all properties are considered, this attribute is missing.

A `ModelElementSet` element contains one `Runtime` element, which indicates the runtime for computing the core. It also contains a sequence of `Node` elements, each one enumerating the model elements in that node that are part of the core. When relevant, it can also contain a `Counterexample` element (see the `Property` element for more info).

18   Exit codes

Since version 1.9.0, Kind 2 returns the standard exit code `0` for success, and a non-zero exit code to indicate an error, or an unsuccessful analysis result. To force Kind 2 to use only non-zero exit codes for errors, pass the option `--exit_code_mode only_errors`. The precise meaning of the exit codes are described in section Code Convention. For information on the old convention, see section Former Convention.

18.1 Code Convention

With the default settings, Kind 2 performs a single, monolithic analysis of the main node. If Kind 2 proves all invariant properties valid and all reachability properties reachable, then it returns (exit code) `0`. If no properties are disproven, but some properties could not be proven (e.g. due to a timeout), Kind 2 returns `30`. When Kind 2 disproves one or more properties, it returns `40`.

In modular mode, the properties of all nodes are checked bottom-up. Moreover, when compositional analysis is enabled too, the same node may be analyzed several times with different levels of abstraction (see section Refinement in compositional and modular analyses for details). In this case, Kind 2 returns `40` if one or more properties were disproven in any analysis. It returns `30` if no properties were disproven, but some nodes were not analyzed (e.g. due to a timeout) or some properties could not be proven. It returns `0` if all properties were proven for all nodes in every analysis.

When contracts of imported nodes are checked for realizability, Kind 2 also reports an exit status following a similar convention. If all the contracts are proven realizable, it returns `0`. If some contract is proven unrealizable, it returns `40`. When no contract is proven unrealizable, but some contract could not be proven realizable, it returns `30`.

If Kind 2 detects a general error, it returns `1`. When the error is related to an incorrect command-line argument, it returns `2`. If Kind 2 detects a parse error, it returns `3`. If Kind 2 cannot find an SMT solver on the PATH, it returns `4`. When an unknown or unsupported version of an SMT solver is detected, it returns `5`.

18.2 Former Convention

Version 1.8.0 and earlier were not following the POSIX convention of returning `0` for success. When all properties were proven, Kind 2 returned `20`. If some property was disproven, it returned `10`. If no properties were disproven, but some result was unknown, it returned `0`. Moreover, Kind 2 returned `2` for any error.

19 Contract Semantics

19.1 Assume-guarantee contracts

This section discusses the semantics of contracts, and in particular modes, in Kind 2. For details regarding the syntax, please see the Contracts section.

An assume-guarantee contract `(A,G)` for a node `n` is a set of assumptions `A` and a set of guarantees `G`. Assumptions describe how `n` **must** be used, while guarantees specify how `n` behaves.

More formally, `n` respects its contract `(A,G)` if all of its executions satisfy the temporal LTL formula

$$\Box A \Rightarrow \Box G$$

That is, if the assumptions always hold then the guarantees hold. Contracts are interesting when a node `top` calls a node `sub`, where `sub` has a contract `(A,G)`.

From the point of view of `sub`, a contract `({a_1, ..., a_n}, {g_1, ..., g_m})` represents the same verification challenge as if `sub` had been written

```
node sub (...) returns (...) ;
let
  ...
  assert a_1 ;
  ...
  assert a_n ;
  --%PROPERTY g_1 ;
  ...
  --%PROPERTY g_m ;
tel
```

The guarantees must be invariant of `sub` when the assumptions are forced.

For the caller however, the call `sub(<params>)` is legal **if and only if** the assumptions of `sub` are invariants of `top` at call-site. The verification challenge for `top` is therefore the same as

```
node top (...) returns (...) ;
let
  ... sub(<params>) ...
  --%PROPERTY a_1(<call_site>) ;
  ...
  --%PROPERTY a_n(<call_site>) ;
tel
```

19.2 Modes

Kind 2 augments traditional assume-guarantee contracts with the notion of mode. A mode `(R,E)` is a set `R` or requires and a set `E` of ensures. A Kind 2 contract is therefore a triplet `(A,G,M)` where `M` is a set of modes. If `M` is empty then the semantics of the contract is exactly that of an assume-guarantee contract.

19.2.1 Semantics

A mode represents a situation / reaction implication. A contract `(A,G,M)` can be re-written as an assume-guarantee contract `(A,G')` where

$$G' = G \ \cup \ \{ \ \bigwedge_i r_i \Rightarrow \bigwedge_i e_i \mid (\{r_i\}, \{e_i\}) \in M\}$$

For instance, a (linear) contract for non-linear multiplication could be

```
node abs (in: real) returns (res: real) ;
let res = if in < 0.0 then - in else in ; tel

node times (lhs, rhs: real) returns (res: real) ;
con
  mode absorbing (
    require lhs = 0.0 or rhs = 0.0 ;
    ensure res = 0.0 ;
  ) ;
  mode lhs_neutral (
    require not absorbing ;
    require abs(lhs) = 1.0 ;
    ensure abs(res) = abs(rhs) ;
  ) ;
  mode rhs_neutral (
    require not absorbing ;
    require abs(rhs) = 1.0 ;
    ensure abs(res) = abs(lhs) ;
  ) ;
  mode positive (
    require (
      rhs > 0.0 and lhs > 0.0
    ) or (
      rhs < 0.0 and lhs < 0.0
    ) ;
    ensure res > 0.0 ;
  ) ;
  mode pos_neg (
    require (
```

```
      rhs > 0.0 and lhs < 0.0
    ) or (
      rhs < 0.0 and lhs > 0.0
    ) ;
    ensure res < 0.0 ;
  ) ;
noc
let
  res = lhs * rhs ;
tel
```

Motivation: modes were introduced in the contract language of Kind 2 to account for the fact that most requirements found in specification documents are actually implications between a situation and a behavior. In a traditional assume-guarantee contract, such requirements have to be written as `situation => behavior` guarantees. We find this cumbersome, error-prone, but most importantly we think some information is lost in this encoding. Modes make writing specification more straightforward and user-friendly, and allow Kind 2 to keep the mode information around to

- improve feedback for counterexamples,
- generate mode-based test-cases, and
- adopt a defensive approach to guard against typos and specification oversights to a certain extent. This defensive approach is discussed in the next section.

19.2.2 Defensive checks

Conceptually modes correspond to different situations triggering different behaviors for a node. Kind 2 is defensive in the sense that when a contract has at least one mode, it will check that the modes account for **all situations** the assumptions allow before trying to prove the node respects its contract.

More formally, consider a node `n` with contract

$$(A, G, \{(R_i, E_i)\})$$

The defensive check consists in checking that the disjunction of the requires of each mode

$$\mathsf{one\_mode\_active} = \bigvee_i (\bigwedge_j r_{ij})$$

is an invariant for the system

$$A \wedge G \wedge (\bigwedge r_i \Rightarrow \bigwedge e_i)$$

If `one_mode_active` is indeed invariant, it means that as long as

- the assumptions are respected, and
- the node is correct w.r.t. its contract then at least one mode is active at all time.

Kind 2 follows this defensive approach. If a mode is missing, or a requirement is more restrictive than it should be then Kind 2 will detect the modes that are not exhaustive and provide a counterexample.

This defensive approach is not as constraining as it first appears. If one wants to leave some situation unspecified on purpose, it is enough to add to the current set of (non-exhaustive) modes a mode like

```
mode base_case (
  require true ;
) ;
```

which explicitly accounts for, and hence documents, the missing cases.

In addition, Kind 2 checks that all modes are reachable in the system. In other words, Kind 2 also checks that for each mode there exists a reachable state satisfying the conjunction of its requires. This lets you know whether the mode implication is vacuously true or not.

When the node associated to the contract has a body (it is not imported), the check will be performed twice. First, considering only the information of the contract. Then, considering the equations of the body too.

Notice that when running Kind 2 in modular mode, the reachability check is performed locally to a node without taking call contexts into account; only the specified assumptions are considered.

You can disable this check by passing `--check_nonvacuity false` to Kind 2, or by suppressing all reachability checks (`--check_reach false`).

20 Post Analysis Treatments

Post-analysis treatments are flag-activated Kind 2 features that are not directly related to verification. The current post-analysis treatments available are

- certification,
- test generation,
- contract generation,
- assumption generation,
- invariant printing, and
- inductive validity core generation

All of them are deactivated by default. Post-analysis treatments run on the last analysis of a system. It is defined as the last analysis performed by Kind 2 on a given system. With the default settings, Kind 2 performs a single, monolithic analysis of the top node. In this case, the last analysis is this unique analysis.

This behavior is changed by the `compositional` flag. For example, say Kind 2 is asked to analyze node `top` calling two subnodes `sub_1` and `sub_2`, in compositional mode. Say also `sub_1` and `sub_2` have contracts, and that refinement is possible. In this situation, Kind 2 will analyze `top` by abstracting its two subnodes. Assume for now that this analysis concludes the system is safe. Kind 2 has nothing left to do on `top`, so this compositional analysis is the last analysis of `top`, Kind 2 will run the post-analysis treatments. Assume now that this purely compositional analysis discovers a counterexample. Since refinement is possible, Kind 2 will refine `sub_1` (and/or `sub_2`) and start a new analysis. Hence, the first, purely compositional analysis is not the last analysis of `top`. The analysis where `sub_1` and `sub_2` are refined is the last analysis of `top` regardless of its outcome (assuming no other refinement is possible).

Long story short, the last analysis of a system is either the first analysis allowing to prove the system safe, or the analysis where all refineable systems have been refined.

The `modular` flag forces Kind 2 to apply whatever analysis / treatment the rest of the flags specify to all the nodes of the system, bottom-up. Post-analysis treatments respect this behavior and will run on the last analysis of each node.

20.1 Prerequisites

Some treatments can fail (which results in a warning) because some conditions were not met by the system and/or the last analysis. The prerequisites for each treatment are:

Treatment	Conditions	Notes
certification	last analysis proved the system safe	will fail if node is partially defined
test generation	system has a contract with more than one mode and the last analysis proved the system safe	
contract generation		experimental
assumption generation	last analysis falsified some property	generates non-temporal constraints
invariant printing		
inductive validity core generation	last analysis proved the system safe	

21 Test Generation

Most test generation techniques analyze the syntax of the model they run on to generate test cases satisfying some coverage criteria. Kind 2 does not follow this approach but instead generates tests based on the specification, more precisely the modes of the specification.

Kind 2's test generation was developed in a context where the actual implementation of the components is **outsourced**. That is, a model of the system is written in-house based on some specification. The model is then verified correct with respect to its specification, using Kind 2 of course, before the specification is given to external sub-contractors that will eventually produce some binaries but will **not** give access to their source code. At this point, there is a need to test these binaries in-house.

In this context, syntactic test generation is arguably not appropriate as it would be based on the syntax of the model, not that of the actual source code of the binaries. There is no reason to believe any connection between the two. Now, the only thing we know of the binaries is that they are supposed to verify the specification. For this reason, Kind 2's test generation ignores the syntax of the input model and instead builds on contracts (see Contract Semantics), and more precisely on the notion on mode.

21.1 Combinations of modes as abstractions

Modes specify behaviors specific to a situation in a contract, and can be seen as abstractions of the states allowed by the assumptions of the contract. Note that because of the mode exhaustiveness check, there is always at least one mode active in any reachable state.

One can explore, starting from the initial states, the mode that can be activated up to some depth. For example, consider the following `stopwatch` system:

```
contract stopwatchSpec ( tgl, rst : bool ) returns ( c : int ) ;
let
  var on: bool = tgl -> (pre on and not tgl) or (not pre on and tgl) ;
  assume not (rst and tgl) ;
  guarantee c >= 0 ;
  mode resetting ( require rst ; ensure c = 0 ; ) ;
  mode running (
    require not rst ; require on ; ensure c = (1 -> pre c + 1) ;
  ) ;
  mode stopped (
    require not rst ; require not on ; ensure c = (0 -> pre c) ;
  ) ;
tel

node previous ( x : int ) returns ( y : int ) ;
```

```
let
  y = 0 -> pre x ;
tel

node stopwatch ( toggle, reset : bool ) returns ( count : int ) ;
con
  import stopwatchSpec ( toggle, reset ) returns ( count ) ;
noc
var running : bool ;
let
  running = (false -> pre running) <> toggle ;
  count = if reset then 0 else
    if running then previous(count) + 1 else previous(count) ;
tel
```

It seems that any of the three modes from the contract can be active at any point, since their activation only depends on the values of the inputs. We can ask Kind 2 to generate the graph of mode paths up to some depth (5 here):

```
kind2 --testgen true --testgen_len 5 stopwatch.lus
```

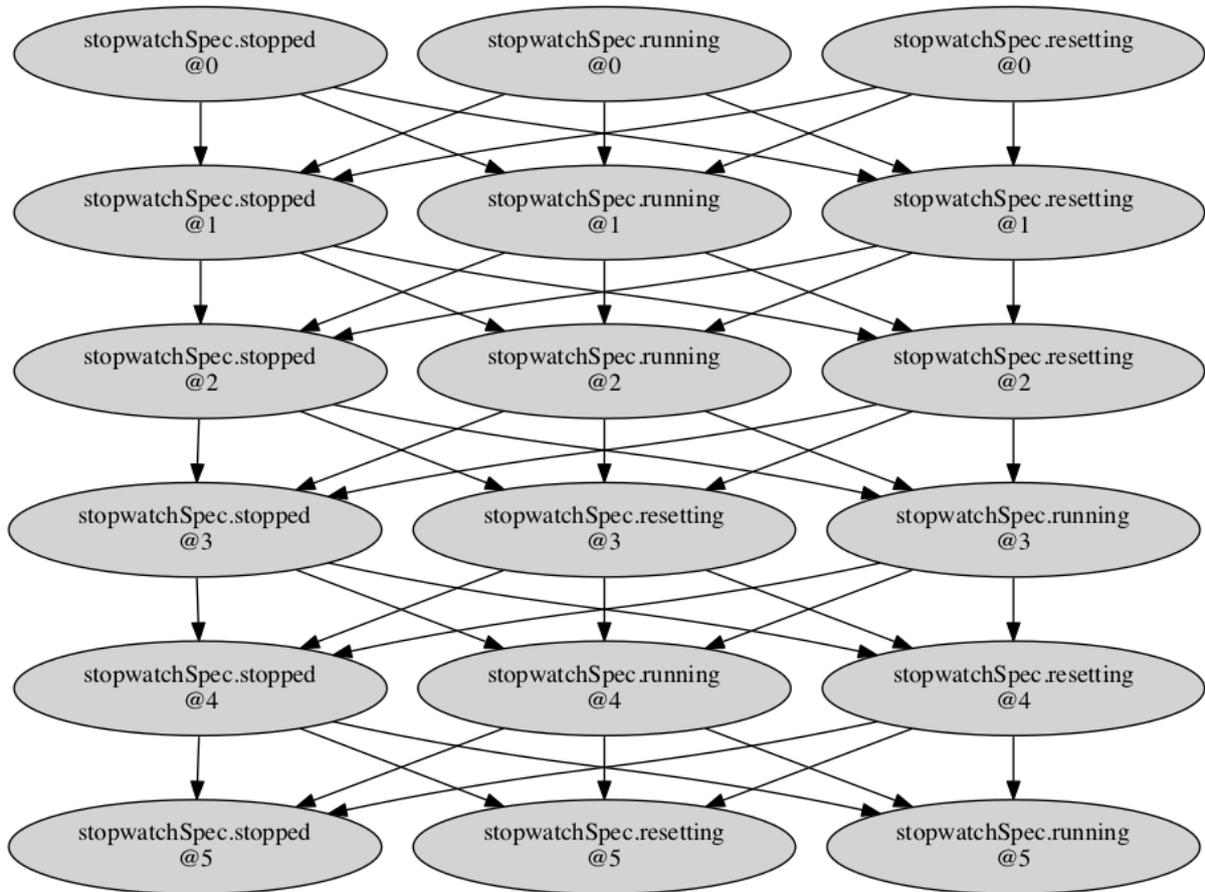This will generate the following graph (and a lot of other files we will discuss below but omit for now):

Fig. 1: Stopwatch DAG

The graph confirms our understanding of the specification, each mode can be activated at any time. Say now we made a mistake on the assumption:

```
assume not (rst or tgl) ;
```

It is now illegal to reset or start the stopwatch. The graph is generated very quickly as with this assumption the system cannot do anything:
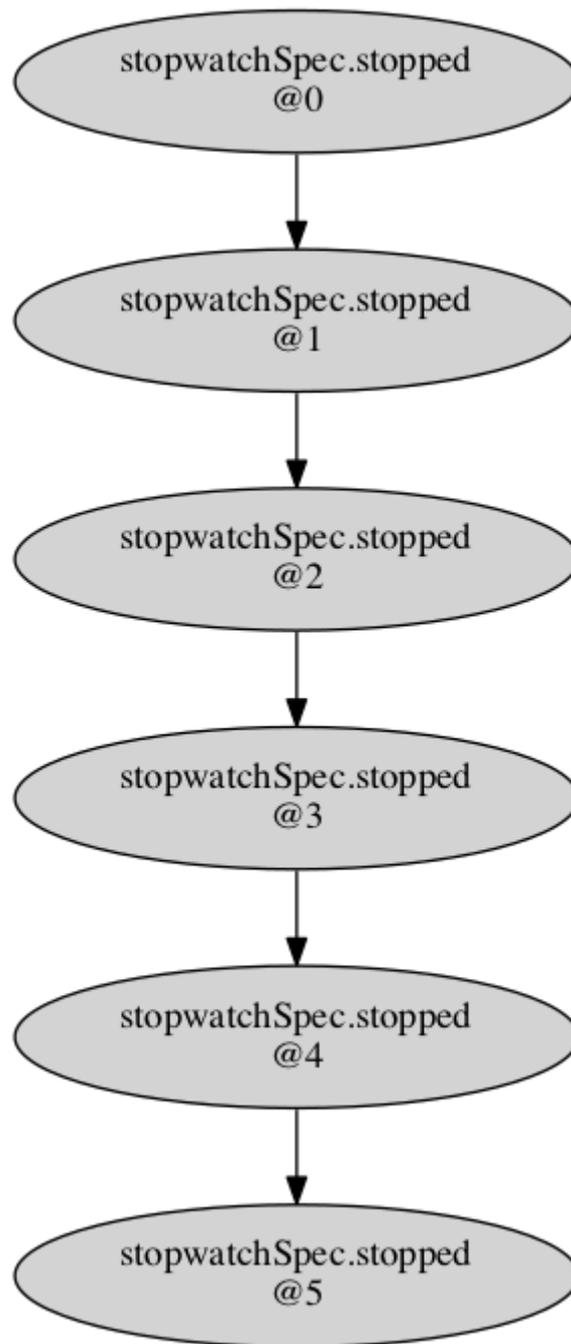
Fig. 2: Stopwatch mistake DAG

N.B. In this simple system, only one mode could be active at a time. This is not the case in general. See for example the mode graphs for the mode logic or the full model of the Transport Class Model (TCM) case study.

21.2 Generating test cases

Since Kind 2 can explore the traces of combinations of modes that can be activated from the initial states, generating test cases is simple. Each test case is simply a trace of inputs, or witness, triggering a different path of mode combinations in the DAG discussed above.

Each witness is logged in JSON file. It is in the same format as the interpreter input format. (See the Interpreter)

A glue XML file lists all the test cases and provides additional information such as the trace of mode combinations they triggered in the model.

> But aren't the witnesses still based on how the model is written?

Yes they are. There is no way to completely abstract the model/prototype away, nor is it desirable. Generating test cases solely on the specification is not realistic unless the specification is extremely strong and precise, which it very rarely is. (Also, if it was, it would arguably be easier to produce the object code as a refinement of the specification using the B-method for instance.)

21.3 Analyzing the executable

The purpose of generating these test cases is to eventually run them on an executable version of the model to check whether it crashes and whether it respects the specification.

For convenience, Kind 2 offers a feature, a contract monitor, which checks whether the output produced by the executable for a given test case respects the contract.

The contract monitor reads the input values of the test case that are fed to the System Under Test (SUT), along with the output values returned by the SUT, and reports the truth values of the guarantees and modes of the original contract. The input format for the contract monitor is the same as the interpreter input format, except that the input includes not only the values of the input variables but also the values of the output variables.

22 Proof Certificates

One clear strength of model checkers, as opposed to proof assistants, say, is their ability to return precise error traces witnessing the violation of a given safety property. Such traces not only are invaluable for designers to correct bugs, they also constitute a checkable certificate. For instance Kind 2 display a counterexample trace that shows the evolution of values of all variables in the system up to a violation of the property. In most cases, it is possible to use a counterexample for a safety property to direct the execution of the system under analysis to a state that falsifies that property. In contrast, most model checkers are currently unable to return any form of corroborating evidence when they declare a safety property to be satisfied by the system. This is unsatisfactory in general since these are complex tools based on a variety of sophisticated algorithms and search heuristics, and so are not immune to errors.

To mitigate this problem, Kind 2 accompanies its safety claims with a certificate, an artifact embodying a proof of the claim. The certificate can then be validated by a trusted certificate/proof checker, in our case the LFSC checker.

22.1 Certification chain

The certification process for Kind 2 is depicted in the graph below. Kind 2 generates two sorts of safety certificates, in the form of SMT-LIB 2 scripts: one certifying the faithfulness of the translation from the Lustre input model to the internal encoding, and another one certifying the invariance of the input properties for the internal encoding of the input system. These certificates are checked by cvc5, then turned into LFSC proof objects by collecting cvc5's own proofs and assembling them to form an overall proof that can be efficiently verified by the LFSC proof checker.
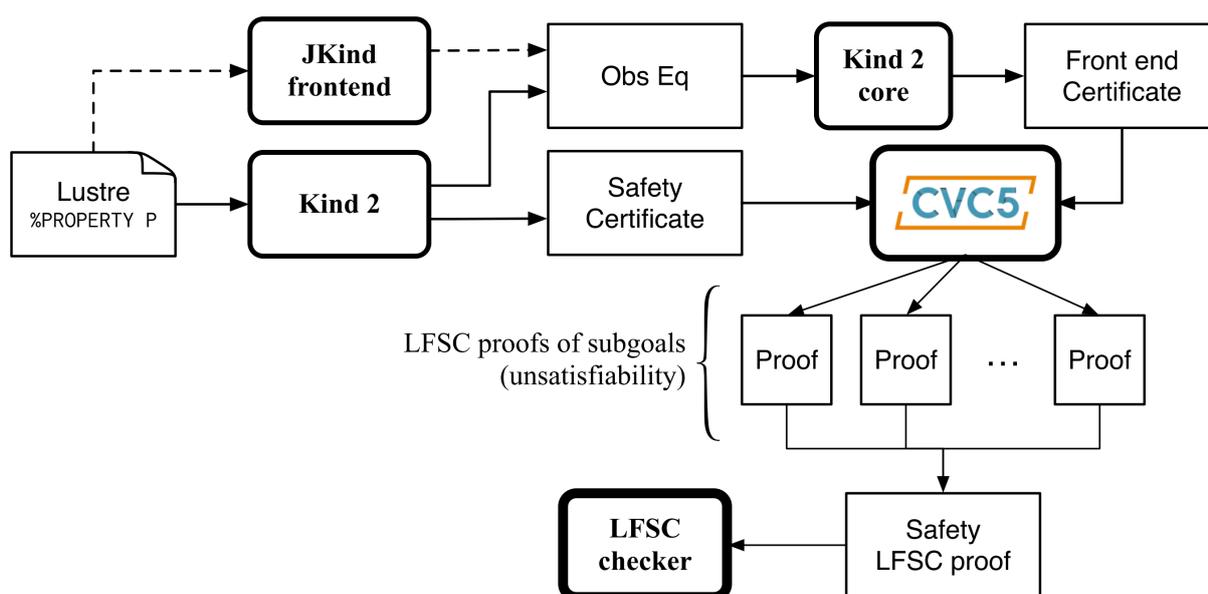

Fig. 1: Certification process

Trust is claimed at a higher level when both proof certificates are present. In practice, this means that Kind 2 didn't make any mistake in its model checking phase, and that the translation of the Lustre model to the internal representation is faithful.

22.2 Producing certificates and proofs with Kind 2

To illustrate this process, we rely on the toy model below (`add_two.lus`). The model encodes in Lustre a synchronous reactive component, `add_two`, that at each execution step other than the first, outputs the maximum between the previous value of its output variable `c` and the sum of the current values of input variables `a` and `b`. The value of `c` is initially `1.0`. The model is annotated with an invariance property stating that, at each step, the output `c` is positive whenever both inputs are.

```
node add_two (a, b : real) returns (c : real) ;
  var v : real;
      P : bool;
let
  v = a + b ;
  c = 1.0 -> if (pre c) > v then (pre c) else v ;
  P = (a > 0.0 and b > 0.0) => c > 0.0 ;
  --%PROPERTY P;
tel
```

Kind 2 offers the possibility to generate two types of certificates, SMT-LIB 2 certificates and actual proofs in the format of LFSC. It will do so only for systems whose properties (or contracts) are all proven valid.

22.2.1 Requirements

Frontend certificates and proofs production require the user to have JKind installed on their machine (together with a suitable version of Java).

SMT-LIB 2 certificates do not require anything additional except for an SMT solver to check the certificates.

LFSC proofs production requires cvc5 (the binary can be specified with `--cvc5_bin`), its LFSC proof signatures, and the LFSC checker for the final proof checking phase.

LFSC checker

A bash script to download and build the LFSC checker is distributed with Kind 2:

```
lfsc/get-lfsc-checker.sh
```

The script also downloads the cvc5 LFSC signatures and generates an easy-to-use bash script (`lfsc-check.sh`) to check LFSC proofs generated by Kind 2:

```
lfsc
|-- get-lfsc-checker.sh
|-- bin
    |-- lfscc
    |-- lfsc-check.sh
|   ...
|-- signatures
    |-- arith_programs.plf
    |-- ...
```

22.2.2 SMT-LIB 2 certificates

These certificates are always produced but are only used as an intermediate step for LFSC proof production. The user still has the possibility to get them as the final output of Kind 2 in a convenient form. To do so, invoke Kind 2 (on the previous example `add_two.lus`) with the following:

```
kind2 --certif true add_two.lus
```

For successful runs, the output of Kind 2 will contain:

```
Post-analysis: certification

Certificate checker was written in add_two.lus.out/certif/certificate.smt2
Generating frontend eq-observer with jKind ...
Generating frontend certificate
...
Certificate checker was written in add_two.lus.out/certif/FEC.kind2.out/certif/FECC.
↪smt2
```

The certificates are located in the directory `add_two.lus.out/certif` which has the following structure:

```
add_two.lus.out/certif
|-- certificate_checker
|-- certificate_prelude.smt2
```

```
|-- certificate.smt2
|-- FEC.kind2
|-- FEC.kind2.out/certif
    |-- FECC_checker
    |-- FECC_prelude.smt2
    |-- FECC.smt2
    |-- observer_sys.smt2
|-- jkind_sys_lfsc_trace.smt2
|-- jkind_sys.smt2
|-- kind2_sys.smt2
|-- observer_lfsc_trace.smt2
|-- observer.smt2
```

In particular, it contains two scripts of interest: `certificate_checker` and `FECC_checker`. They are meant to be run with the name of an SMT solver as argument and should produce each three `unsat` results. The first one checks that the certificate of invariance is valid with the provided SMT solver and the second script checks that the frontend certificate is valid.

```
> add_two.lus.out/certif/certificate_checker z3
Checking base case
unsat
Checking 1-inductive case
unsat
Checking property subsumption
unsat

> add_two.lus.out/certif/FEC.kind2.out/certif/FECC_checker z3
Checking base case
unsat
Checking 1-inductive case
unsat
Checking property subsumption
unsat
```

22.2.3 LFSC proofs

The other option offered by Kind 2, and the most trustworthy one, is to produce LFSC proofs. This can be done with the following invocation:

```
kind2 --proof true add_two.lus
```

Successful runs emit outputs that contain lines such as:

```
Post-analysis: certification

Generating frontend eq-observer with jKind ...
Generating frontend proof
...
Final LFSC proof written to add_two.lus.out/add_two.lus.1.lfsc
```

The important one is the last message that indicate the file in which the proof was written. The directory produced by Kind 2 will have the following structure:

```
add_two.lus.out/
|-- add_two.lus.1.lfsc
|-- certificates.1
    |-- FEC.kind2
    |-- base.smt2
    |-- frontend_base.smt2
    |-- frontend_implication.smt2
    |-- frontend_induction.smt2
    |-- frontend_proof.lfsc
    |-- implication.smt2
    |-- induction.smt2
    |-- jkind_sys.smt2
    |-- jkind_sys_lfsc_trace.smt2
    |-- kind2_phi.smt2
    |-- kind2_phi_lfsc_trace.smt2
    |-- kind2_sys.smt2
    |-- kind2_sys_lfsc_trace.smt2
    |-- obs_phi.smt2
    |-- obs_phi_lfsc_trace.smt2
    |-- observer.smt2
    |-- observer_lfsc_trace.smt2
    |-- proof.lfsc
```

It contains as many proofs (at the root) as there are relevant analysis performed by Kind 2 (for modular and compositional reasoning). To make sure that the proof is an actual proof, one needs to call the LFSC checker on the generated output, together with the correct signatures:

```
lfsc/bin/lfscc <cvc5 signatures in order> <kind 2 signature> add_two.lus.out/add_two.
↪lus.1.lfsc
```

or use the convenient bash script generated by **lfsc/get-lfsc-checker.sh**:

```
lfsc/bin/lfsc-check.sh add_two.lus.out/add_two.lus.1.lfsc
```

The return code for either command execution is `0` when everything was checked correctly.

When the bash script is used and the whole proof is correct, the following line will be displayed:

```
Valid LFSC proof!
```

When the LFSC checker is called instead, three lines will be displayed when both the proof of invariance and the proof of correct translation by the frontend are valid:

```
success
success
success
```

In the case where only the invariance proof was produced and checked, the return code will still be 0 but only a single `success` will be in the output.

22.2.4 Proof options

Kind 2 supports several options to control the format and granularity of proofs:

- `--smaller_holes <bool>` (default `false`) – By default, LFSC proofs generated by Kind 2 contain holes encoded as (`trust ..`) steps. This option reduces the size of holes in the generated proofs, and thus, increases trust in Kind 2's result. The option is disabled by default as the more granular proofs take significantly more time to generate, are orders of magnitude larger, and take longer time to verify than proofs with bigger holes. Note: this option reduces the size of holes in the proofs and not their number, which is likely to increase when it is enabled.
- `--flatten_proof <bool>` (default `false`) – Break the proof down into a sequence of lemmas. The proof for each lemma is verified by the LFSC checker and erased immediately. This option helps reduce the memory footprint of the LFSC checker and improve its performance. It is recommended to enable this option with `--smaller_holes`. Note: enabling this option will increase the number of `success` messages displayed by the LFSC checker.

22.3 Contents of certificates

For a given problem (whose safety property is P), an internal certificate consists in only a pair (k, ϕ) where ϕ is a k-inductive invariant of the system which implies the original properties. SMT-LIB 2 certificates are in fact scripts whose check make sure that ϕ implies P and is k-inductive. The LFSC proof is a formal proof that P is invariant in the system, using sub-proofs of validity (unsatisfiability) returned by cvc5.

22.4 LFSC signature

A proof system is formally defined in LFSC through signatures, which contain a definition of the system's language together with axioms and proof rules. The proof system used by cvc5 is defined over a number of signatures, which are included in its source code distribution. Those relevant to this work include signatures for propositional logic and resolution (`boolean_rules.plf`); first-order terms and formulas, with rules for CNF conversion and abstraction to propositional logic (`cnf_rules.plf`); equality over uninterpreted functions (`equality_rules.plf`); and real and integer linear arithmetic (`arith_rules.plf`).

cvc5's proof system is extended with an additional signature (`kind.plf`) for k-inductive reasoning, invariance and safety. This signature also specifies the encoding for state variables, initial states, transition relations, and property predicates. State variables are encoded as functions from natural numbers to values. This way, the unrolling of the transition relation does not need the creation of several copies of the state variable tuple **x**. For example, for the state vector **x** = (y , z) with y of type real and z of type integer, the LFSC encoding will make y and z respectively functions from naturals to reals and integers. So we will use the tuples (y(0) , z(0)), (y(1) , z(1)), … instead of (y0 , z0), (y1 , z1), … where y0 , y 1 , …, z0 , z1, … are (distinct) variables. Correspondingly, our LFSC encoding of a transition relation formula T[**x**, **x'**] is parametrized by two natural variables, the index of the pre-state and of the post-state, instead of two tuples of state variables. Similarly, I, P and ϕ are parametrized by a single natural variable.

The signature defines several derivability judgments, including one for proofs of invariance, which has the following type:

$$\text{invariant} : \Pi \text{ I} : \mathbb{N} \to \text{formula}.$$
$$\Pi \text{ T} : \mathbb{N} \to \mathbb{N} \to \text{formula}.$$
$$\Pi \text{ I} : \mathbb{N} \to \text{formula.Type}$$

It also contains various rules to build proofs of invariance by k-induction. This signature also specifies how to encapsulate proofs for the front-end certificates by providing a additional judgment, safe(I,T,P,I',T',P'), which can be derived only when invariant(I,T,P) is derivable and the observational equivalence between (I,T,P) and (I',T',P') is provable (judgment woe). Self contained proofs of safety follow the sketch depicted below, where Smt stands for an unsatisfiability rule whose proof tree is obtained, with minor changes, from a proof produced by cvc5.

Fig. 2: Proof sketch

23 Contract Generation

Disclaimer: This feature is very experimental. In particular, the modes (if any) of the contracts generated might not be exhaustive. In this case, Kind 2 will reject the contract during the mode exhaustiveness check.

Contract generation is intended, at least for now, as a helper for users to getting started with Kind 2's contract language. Contract generation is activated by the flag `--contract_gen`.

Internally, this feature is implemented by running invariant generation on the input system up to some depth, specified by flag `--contract_gen_depth`. Doing so will discover equivalence and implication invariants over the system. The ones that talk only about the input / outputs of the systems are used to create the contract dumped in a Lustre file in the output directory. Note that the restriction to just input and output variables causes many of the generated invariants to be discarded currently.

24 Invariant Printing

This treatment minimizes the invariants used in the proof of the valid properties, and shows them in the output without logging them on disk.

25 Interpreter

The interpreter is a special mode where Kind 2 reads input values from a file and prints the computed values for the output and local variables of a node at each step. If the Lustre file contains two or more top nodes, a single node must be selected with either the command-line option `--lus_main <node_name>` or a single `--%MAIN` annotation in the Lustre file.

To use the interpreter, run:

```
kind2 --enable interpreter <lustre_file> --interpreter_input_file <input_file>
```

You can specify the number of steps to run with the option `--interpreter_steps <int>`. By default, the number of steps is determined by the input file.

25.1 Structure of the input file

The inputs must be specified in a JSON file.

The overall structure is as follows:

```json
[
  {
    "var1": "42",
    "var2": true,
    "var3": "0.5"
  },
  {
    "var1": "24",
    "var2": false,
    "var3": "1.0/2.0"
  }
]
```

The top-level JSON array corresponds to the successive time steps. Each time step is described by a JSON object associating to each input variable its value for this time step.

NOTE: Kind2 also accepts the CSV format for backward compatibility reasons. However, it does not support records, arrays and tuples. Please give your input file the adequate extension (*.json or *.csv) in order to indicate to Kind2 which format you are using.

25.2 Integers and reals

As in the above example, integers and reals should be written as strings in order to avoid a potential loss of precision or an integer overflow while parsing the file. Nevertheless, small integers can be written as native JSON integers without problem.

25.3 Records

Record values can be expressed using a JSON object.

For instance, a variable `c` of type `{ re: real; im: real }` can be assigned as follows:

```
[
  {
    "c": { "re": "-1.0", "im": "0.25" }
  }
]
```

25.4 Arrays

Array values can be expressed using a JSON array.

For instance, a variable `a` of type `bool^3^2` can be assigned as follows:

```
[
  {
    "a": [[true, true, false], [false, true, true]]
  }
]
```

25.5 Tuples

The JSON format does not support tuples by default, so the emelents of the tuple must be named by their index in a JSON object.

For instance, a variable `t` of type `[int, bool, real]` can be assigned as follows:

```
[
  {
    "t": { "0":"36", "1": false, "2":"5.0" }
  }
]
```

26   Contract Monitor

The contract monitor is a special mode where Kind 2 reads input and output values from a
file and prints a full contract trace of the execution of the top-level node and the subnodes
that appear in the contract. The trace includes truth values for assumptions, guarantees, mode
requires, and mode ensures.

To use the contract monitor, run:

```
kind2 --enable contract_monitor <lustre_file> --monitor_trace_file <input_file>
```

You can specify the number of steps to run with the option `--monitor_steps <int>`. By
default, the number of steps is determined by the input file.

For example, consider the following `stopwatch` system:

```
contract stopwatchSpec ( tgl, rst : bool ) returns ( c : int ) ;
let
  var on: bool = tgl -> (pre on and not tgl) or (not pre on and tgl) ;
  assume not (rst and tgl) ;
  guarantee c >= 0 ;
  mode resetting ( require rst ; ensure c = 0 ; ) ;
  mode running (
    require not rst ; require on ; ensure c = (1 -> pre c + 1) ;
  ) ;
  mode stopped (
    require not rst ; require not on ; ensure c = (0 -> pre c) ;
  ) ;
tel


node previous ( x : int ) returns ( y : int ) ;
let
  y = 0 -> pre x ;
tel


node stopwatch ( toggle, reset : bool ) returns ( count : int ) ;
con
  import stopwatchSpec ( toggle, reset ) returns ( count ) ;
noc
var running : bool ;
let
  running = (false -> pre running) <> toggle ;
  count = if reset then 0 else
    if running then previous(count) + 1 else previous(count) ;
tel
```

Using a JSON file contianing a full execution trace:

```
[
  {
  "toggle": true,
  "reset": false,
  "count": 1
  },
  {
    "toggle": true,
    "reset": false,
    "count": 1
  },
  {
    "toggle": false,
    "reset": false,
    "count": 1
  },
  {
    "toggle": false,
    "reset": false,
    "count": 1
  },
  {
    "toggle": true,
    "reset": false,
    "count": 2
  },
  {
    "toggle": false,
    "reset": false,
    "count": 3
  }
]
```

```
kind2 --enable contract_monitor stopwatch.lus
--monitor_trace_file stopwatch_trace.json --monitor_steps 6
```

This produces the following output:

```
Execution:
Node stopwatch ()
  == Assumptions ==
  assume[l4c3]        tt    tt    tt    tt    tt    tt
  == Guarantees ==
  guarantee[l5c3]     tt    tt    tt    tt    tt    tt
  == Modes ==
  stopped.requires    ff    tt    tt    tt    ff    ff
```

```
stopped.ensures       ff   tt   tt   tt   ff   ff
running.requires      tt   ff   ff   ff   tt   tt
running.ensures       tt   ff   ff   ff   tt   tt
resetting.requires    ff   ff   ff   ff   ff   ff
resetting.ensures     ff   ff   ff   ff   ff   ff
== Inputs ==
toggle                tt   tt   ff   ff   tt   ff
reset                 ff   ff   ff   ff   ff   ff
== Outputs ==
count                  1    1    1    1    2    3
== Ghosts ==
on                    tt   ff   ff   ff   tt   tt
```

27 Inductive Validity Core

The inductive validity core generation is a post-analysis treatement that computes a minimal subset of the model elements (assumptions, guarantees, stateful equations, or node calls) that are sufficient to prove all valid properties.

To enable inductive validity core generation, run

```
kind2 <lustre_file> --ivc true
```

27.1 Options

- `--ivc_category {node_calls|contracts|equations|assertions|annotations}` (default: all categories) – Minimize only a specific category of elements, repeat option to minimize multiple categories
- `--ivc_only_main_node <bool>` (default `false`) – Only elements of the main node are considered in the computation
- `--ivc_all <bool>` (default `false`) – Compute all the Minimal Inductive Validity Cores
- `--ivc_approximate <bool>` (default `true`) – Compute an approximation (superset) of a MIVC. Ignored if `--ivc_all` or `--ivc_must_set` is `true`
- `--ivc_smallest_first <bool>` (default `false`) – Compute a smallest IVC first. If `--ivc_all` is `false`, the computed IVC will be a smallest one
- `--ivc_must_set <bool>` (default `false`) – Compute the MUST set in addition to the IVCs
- `--print_ivc <bool>` (default `true`) – Print the inductive validity core computed
- `--print_ivc_complement <bool>` (default `false`) – Print the complement of the inductive validity core computed (= the elements that were not necessary to prove the properties)
- `--minimize_program {no|valid_lustre|concise}` (default `no`) – Minimize the source Lustre program according to the inductive validity core(s) computed
- `--ivc_output_dir <string>` (default `<INPUT_FILENAME>`) – Output directory for the minimized programs
- `--ivc_uc_timeout <int>` (default 0) – Set a timeout for each unsat core check sent to the solver
- `--ivc_precomputed_mcs <int>` (default 0) – When computing all MIVCs, set a cardinality upper bound for the precomputed MCSs (helps prune space of candidates)

27.2 Example

Let's consider the following Lustre code:

```
contract fSpec(u,v: real) returns(r: real);
let
    guarantee r >= 0.0;
    guarantee true -> r >= pre(r);
    guarantee r >= u;
    guarantee r >= v;
tel;


node f(u, v : real) returns (r : real);
con
    import fSpec(u,v) returns (r) ;
noc
var m1,m2: real;
let
    m1 = if v > u then v else u;
    m2 = if m1 > 0.0 then m1 else 0.0;
    r = m2 -> if pre(r) > m1 then pre(r) else m1;
tel;


node main(x, y : real) returns (P : bool);
var a,b : real;
let
    a = f(x,y);
    b = f(y,x);
    P = a >= x and a >= y and b >= x and b >= y;
    --%PROPERTY P;
tel;
```

If we are interesting in determining which guarantees of the contract `fSpec` of `f` are needed to prove `P`, we should run this command:

```
kind2 <lustre_file> --ivc true --ivc_category contracts --ivc_only_main_node false --
↪compositional true
```

- `--ivc_category contracts`: because we are only interested in minimizing the contract `fSpec`
- `--ivc_only_main_node false`: because `fSpec` is not the contract of the main node, so we need to consider all nodes
- `--compositional true`: as we want to minimize the contract of `f` and not its implementation, we need to enable compositional analysis

We obtain the following inductive validity core:

```
IVC (2 elements):
  Node f
    Guarantee fSpec[l11c12].guarantee[l6c4][3] at position [l6c4]
    Guarantee fSpec[l11c12].guarantee[l7c4][4] at position [l7c4]
```

27.3 Minimizing over a subset of the assumptions/guarantees

If you are interested in computing an IVC among a subset of the assumptions or guarantees, you can use the category `annotations`. The assumptions and guarantees that should be considered must be preceded by the keyword `weakly`. All the other assumptions and guarantees will be considered as always present when computing the IVCs.

For instance, we can modify the previous example as follows:

```
contract fSpec(u,v: real) returns(r: real);
let
    weakly guarantee r >= 0.0;
    guarantee true -> r >= pre(r);
    weakly guarantee r >= u;
    guarantee r >= v;
tel;
```

```
kind2 <lustre_file> --ivc true --ivc_category annotations --ivc_only_main_node false -
↪-compositional true
```

We obtain the following inductive validity core:

```
IVC (1 elements):
  Node f
    Guarantee fSpec[l11c12].weakly_guarantee[l6c4][3] at position [l6c4]
```

27.4 Computing all Inductive Validity Cores

If we want to compute ALL the minimal inductive validity cores, we can use the following flags:

```
kind2 <lustre_file> --ivc true --ivc_all true
```

- `--ivc_all true`: specify that we want to compute all the IVCs

28   Minimal Cut Set

The minimal cut set generation is a special mode where Kind 2 computes a minimal subset of the model elements (assumptions, guarantees, stateful equations, or node calls) whose no satisfaction leads to the violation of a property.

To enable minimal cut set generation, run

```
kind2 <lustre_file> --enable MCS
```

28.1 Options

- `--mcs_category {annotations|node_calls|contracts|equations|assertions}` (default: annotations) – Consider only a specific category of elements, repeat option to consider multiple categories
- `--mcs_only_main_node <bool>` (default `false`) – Only elements of the main node are considered in the computation
- `--mcs_all <bool>` (default `false`) – Specify whether all the Minimal Cut Sets must be computed or just one
- `--mcs_approximate <bool>` (default `true`) – Compute a MCS which is minimal with respect to all the counterexamples of the same length that the first counterexample found. This solution can be considered an approximation of a global one. Ignored if `--mcs_all` is `true`
- `--mcs_max_cardinality <int>` (default `-1`) – Only search for MCSs of cardinality lower or equal to this parameter. If `-1`, all MCSs will be considered
- `--mcs_per_property <bool>` (default `true`) – If true, MCSs will be computed for each property separately
- `--print_mcs <bool>` (default `true`) – Print the minimal cut set computed
- `--print_mcs_complement <bool>` (default `false`) – Print the complement of the minimal cut set computed (this is equivalent to computing a Maximal Unsafe Abstraction)
- `--print_mcs_legacy <bool>` (default `false`) – Print the minimal cut set using the legacy format
- `--print_mcs_counterexample <bool>` (default `false`) – Print a counterexample for each MCS found (ignored if `--print_mcs_legacy` is true)
- `--mcs_per_property <bool>` (default `true`) – If true, MCSs will be computed for each property separately

28.2 Example

Let's consider the following Lustre code:

```
contract spec(x,y: real) returns(z: real);
let
    weakly assume x = -y;
    weakly assume x >= 0.0;
tel;


node main(x, y : real) returns (z : real);
con
    import spec(x,y) returns (z) ;
noc
  var P : bool;
let
    z = x + y;
    P = z = 0.0;
    --%MAIN;
    --%PROPERTY P;
tel;
```

If you are interesting in determining a minimal set of the weak assumptions of the contract `fSpec` whose no satisfaction leads to the violation of P, you can run this command:

```
kind2 <lustre_file> --enable MCS --mcs_category annotations
```

Note that `--mcs_category annotations` is not required since it is the default value.

The following minimal cut set is printed:

```
MCS (1 elements) for property P:
  Node main
    Assumption spec[l9c12].weakly_assume[l4c4][1] at position [l4c4]
```

In the example above, the `weakly` keywork is used to annotate the assumptions and guarantees to consider for the MCS computation (Kind2 will only try to remove these assumptions and guarantees, all the others will be kept).

Alternatively, if we want to compute a MCS over all the assumptions and guarantees, we can change the category to `contracts`:

```
kind2 <lustre_file> --enable MCS --mcs_category contracts
```

29   Contract Check

Kind 2 provides an option to check the realizability of contracts and refinement types. When an input model includes imported nodes or refinement types, it is particularly important to verify that their associated contracts are realizable, i.e., a component can be constructed such that, for any input satisfying the contract assumptions, there exists some output value that the component can produce to meet the contract guarantees.

To check the contracts of nodes and functions, run:

```
kind2 --enable CONTRACTCK <lustre_file>
```

You can specify a particular node or function to analyze using `--lus_main <node_name>`, and a specific refinement type using `--lus_main_type <type_name>`.

If Kind 2 is able to prove some contract unrealizable and the `--print_deadlock` flag is true, Kind 2 will show a deadlocking trace such that all states except the last one satisfy the contract constraints. If the trace only has one state, the state shows input values such that no initial state values satisfy the contract constraints (including the state values chosen as sample). For traces with more than one state, the trace is such that no next state values satisfy the contract constraints from the second-to-last state giving the input values of the last state. Kind 2 will also show a set of conflicting constraints for the last state in the trace.

When the `--check_contract_is_sat` flag is true, Kind 2 will also check whether the unrealizable contract is at least satisfiable, i.e., it is possible to construct a component such that for at least one input sequence allowed by the contract assumptions, there is some output value that the component can produce that satisfies the contract guarantees.

In addition, Kind 2 will check the realizability of the component's environment. This check is also important for the top-level contract, as an unrealizable environment specification can lead to the same flawed compositional proof arguments as an unrealizable leaf-level component contract. You can disable this check by passing `--check_environment false`.

30   Assumption Generation

In the early stages of model development and analysis, properties of system components often fail to hold because the assumptions made about a component's environment are insufficient to guarantee these properties, even when component's behavior is correctly specified. When this happens, the system designer must study the counterexample provided by Kind 2, pinpoint the cause, and identify possible restrictions on the environment that the properties need in order to hold — which were perhaps assumed by the designer but were not made explicit.

For instance, consider the following Lustre program:

```
node Arbiter (s1,s2: bool; e1,e2:int) returns(o: int);
con
  guarantee "G1" s1 => o=e1;
  guarantee "G2" s2 => o=e2;
noc
let
  if s1 and s2 then
    o = any { o:int | o = e1 or o = e2 };
  elsif s1 then
    o = e1;
  else
    o = e2;
  fi
tel
```

If we run Kind 2 to check guarantees `G1` and `G2`, Kind 2 determines the properties are invalid, providing a counterexample for each of them. In the first counterexample, `s1` and `s2` are true initially, and the output is equal to the value of `e2`, which falsifies `G1`. In the second counterexample, `s1` and `s2` are true initially, and the output is equal to the value of `e1`, which falsifies `G2`.

From the description of the counterexamples, it is evident that one potential missing assumption is that `s1` and `s2` are never simultaneously true. If that is indeed the case, explicitly stating this assumption in the contract of the node, allows Kind 2 to prove both properties valid.

Generating the missing assumptions for straightforward examples like the one above is not very difficult. However, in more realistic scenarios, this task can become quite challenging. To help system designers in those situations, Kind 2 offers a post-analysis that can be enabled by passing the command-line option `--assumption_gen true`. When this option is enabled, Kind 2 will automatically generate assumptions that are strong enough to prove the set of falsified properties in the verification analysis while not being overly restrictive. Note that just finding sufficient assumptions is not challenging. The challenge is to find minimally restrictive assumptions which can then be recognized as realistic by the designer.

For the example above, Kind 2 generates the assumption: `(not s2) or (not s1) or (e1 =`

`e2`). Notice that this assumption is a weaker version of the one mentioned above, as it considers a third case where the inputs `e1` and `e2` equal.

The functionality generates one-state constraints on a node's environment, but it currently lacks the capability to generate two-state properties, which presents a significantly more complex challenge.

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